



# Motor Control for Electrified Transportation Systems

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# Outline

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- Adjustable Speed Drives (ASD) in electrified transportation systems
- Electric motor torque control
- Indirect torque control: current control
- Pulse-Width Modulators
- Motor Drives
- Conclusion and challenges

# Electrified Transportation Systems



## Tesla Model S:

Traction Motor:

**3 $\phi$  Induction  
Machine**

$$P_{\max} = 310 \text{ kW}$$



## Citroen C0

Traction Motor:

**PM Synchronous  
Machine**

$$P_{\max} = 49 \text{ kW}$$

## Lexus RX 450h:

Traction Motor:

**PM Synchronous  
Machine**

$$P_{\max} = 130 \text{ kW}$$



## RENAULT Zoe

Traction Motor:

**Wound Rotor  
Synchronous  
Machine**

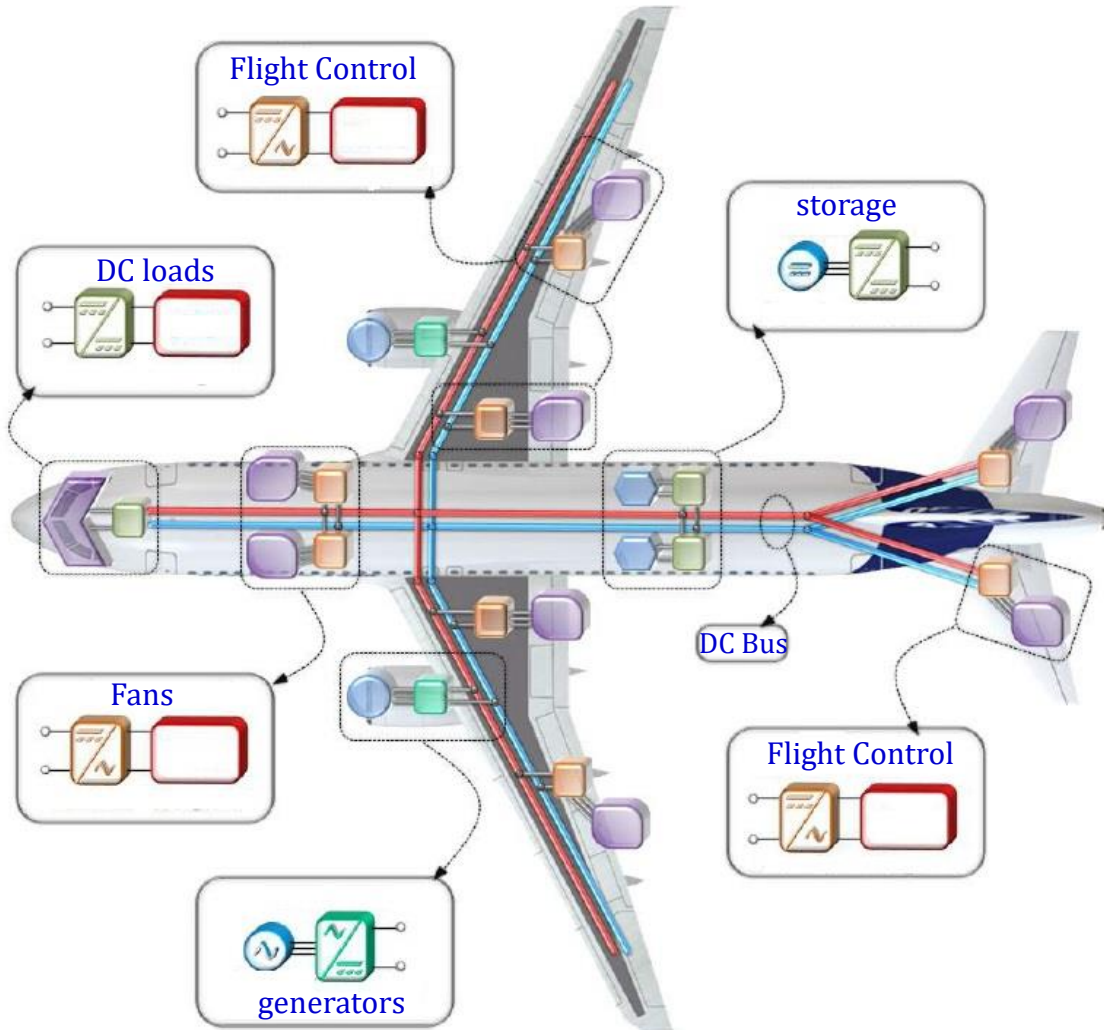
$$P_{\max} = 65 \text{ kW}$$



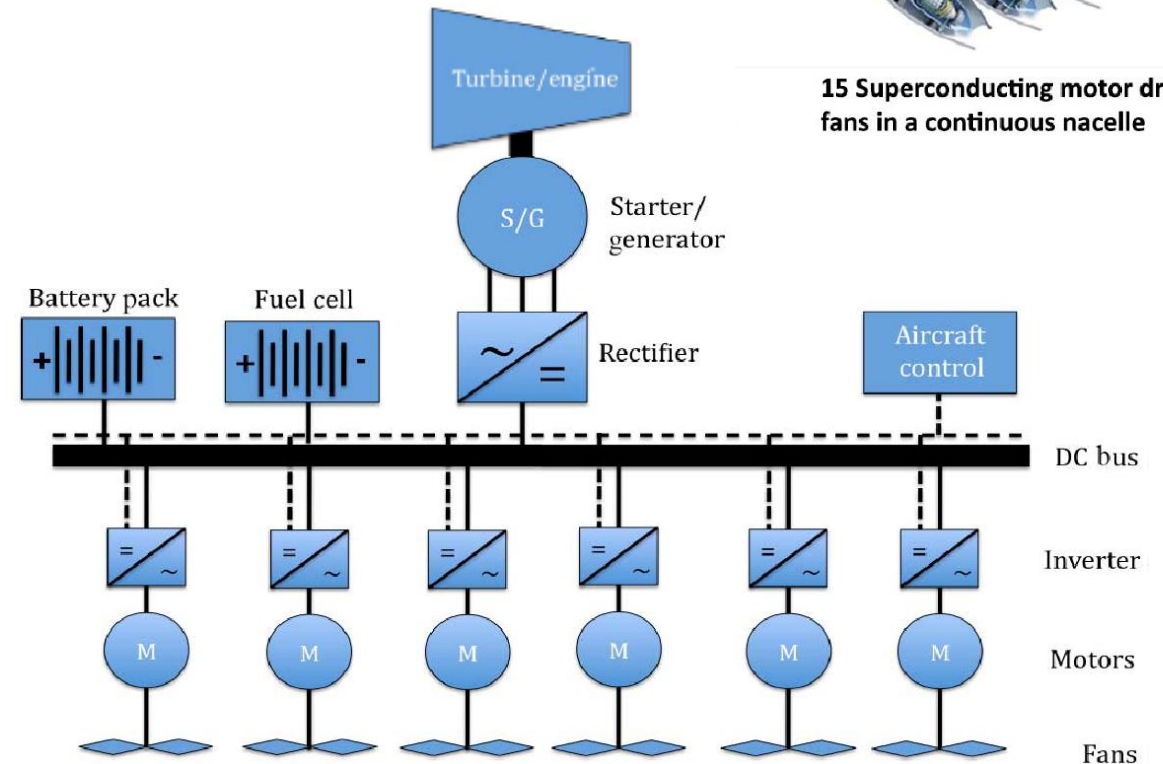
# Electrified Transportation Systems

Power-by-wire: More Electric Aircraft (MEA)  
replacing hydraulic actuators by electric actuators

NASA N3-X HWB:  
Series hybrid Electric Propulsion Aircraft (EPA)

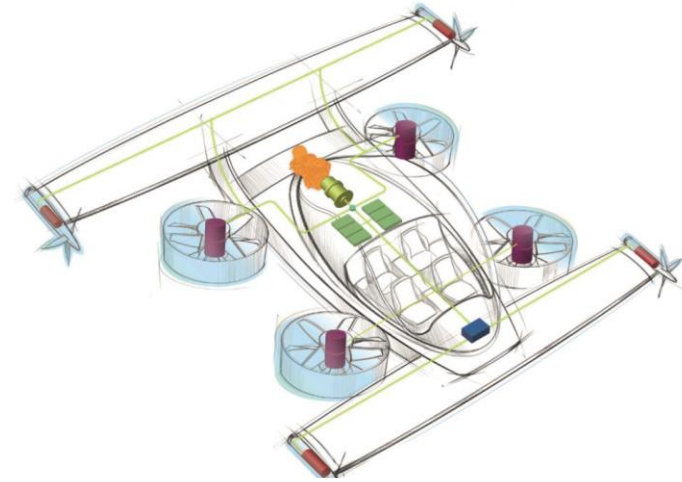


15 Superconducting motor driven fans in a continuous nacelle

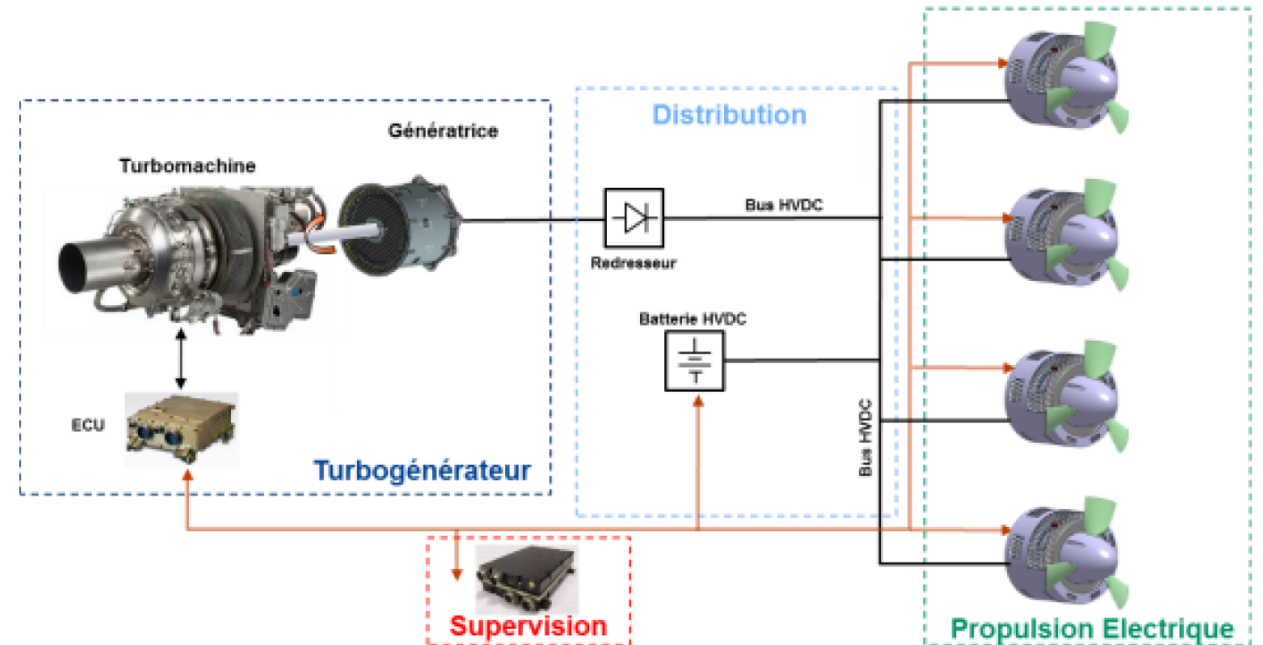


# Electrified Transportation Systems: Flying Cars

## Vertical Take-Off and Landing (VTOL)

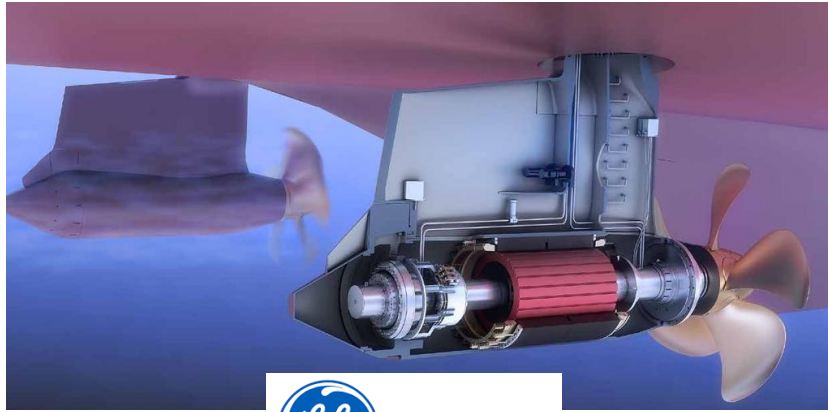


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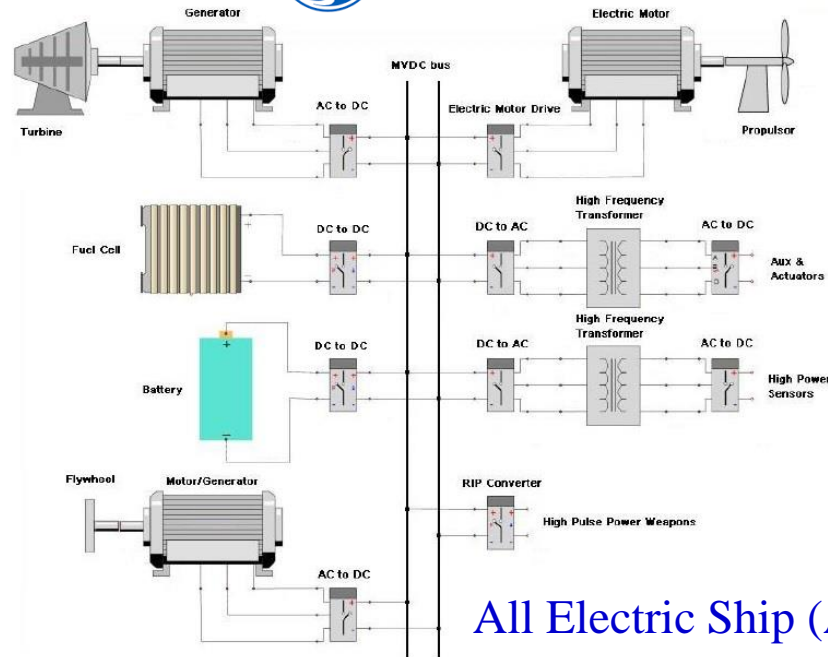
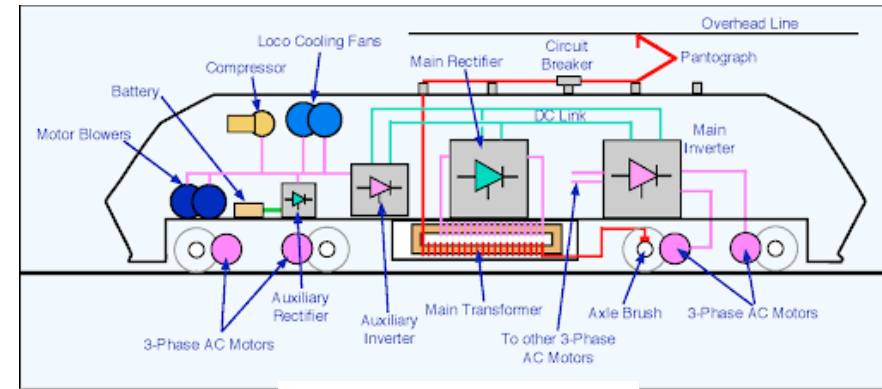


# Other Examples of Electrified Transportation Systems

Sea: oil & gas offshore platforms



Rail: electric locomotive

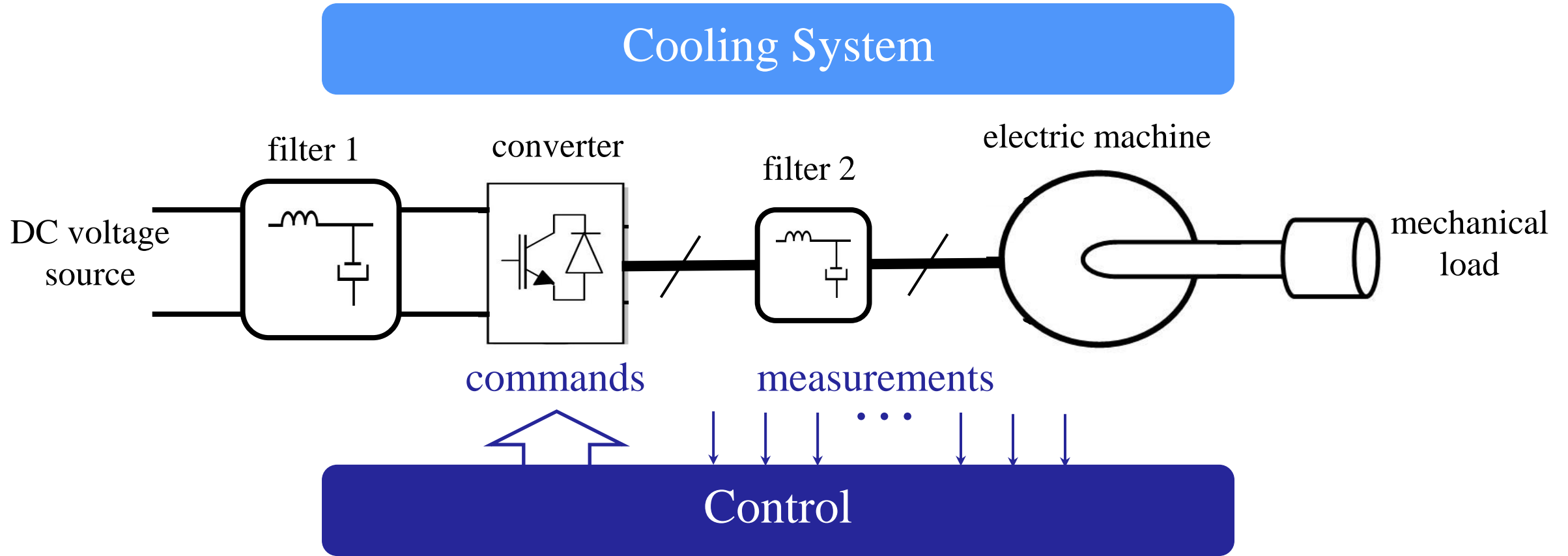


All Electric Ship (AES)

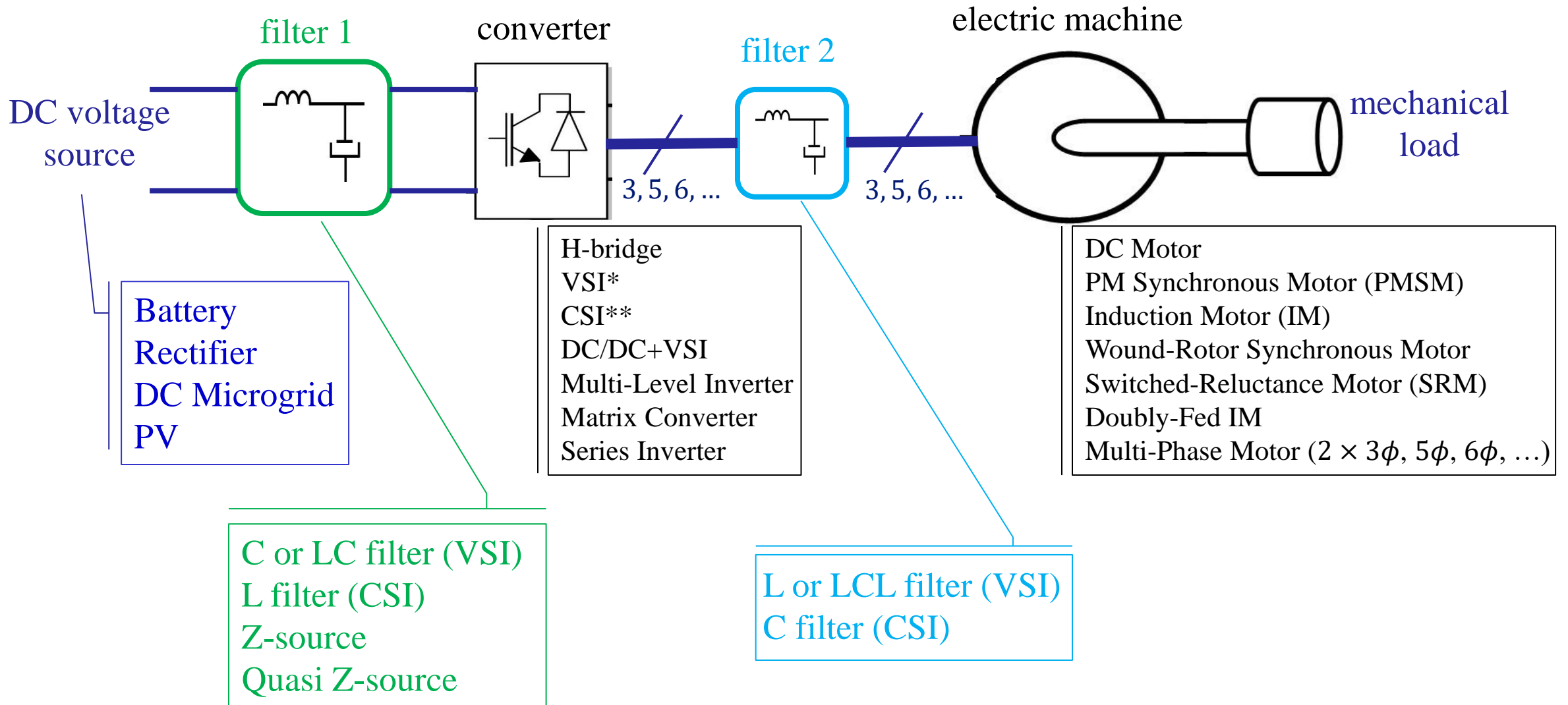
Automated manufacturing



# Structure of Adjustable Speed Drives



# Topologies for Adjustable Speed Drives



\* Voltage-Source Inverter  
 \*\* Current-Source Inverter



# Control of Adjustable Speed Drives

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- **No unique approach** for drives with power range going from **Watt to 100+ kW**
- Main control techniques for AC drives:
  - 1) **Open-loop control:**
    - **Control law:** very simple, pulse trains generated using a look-up table or a simple equation
    - **Sensors:** generally no sensor required
    - **Applications:** mostly low power - low cost applications
    - **Drawbacks:** accuracy, efficiency
  - 2) **Scalar control (V/f or V/Hz):**
    - **Control law:** simple relation between stator voltage magnitude and rotor speed (often under look-up table form)
    - **Sensors:** mechanical sensor (or speed estimator) required
    - **Applications:** mostly low power - low cost applications
    - **Drawbacks:** accuracy, efficiency

# Control of Adjustable Speed Drives

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## 3) Vector control:

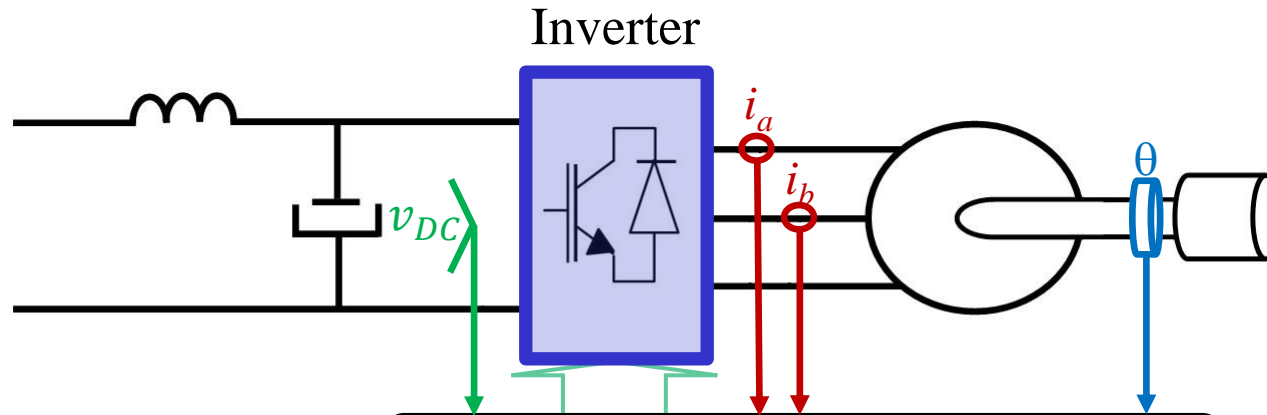
- **Direct Torque Control (DTC):**

- **Control law:** torque and flux estimators AND switch pattern selection OR current regulators + modulator
- **Sensors:** phase current sensors and mechanical sensor, DC-link voltage sensor optional
- **Applications:** widely applied to motor control
- **Drawbacks:** noise, torque ripples, cost

- **Indirect Torque Control or Field-Oriented Control (FOC):**

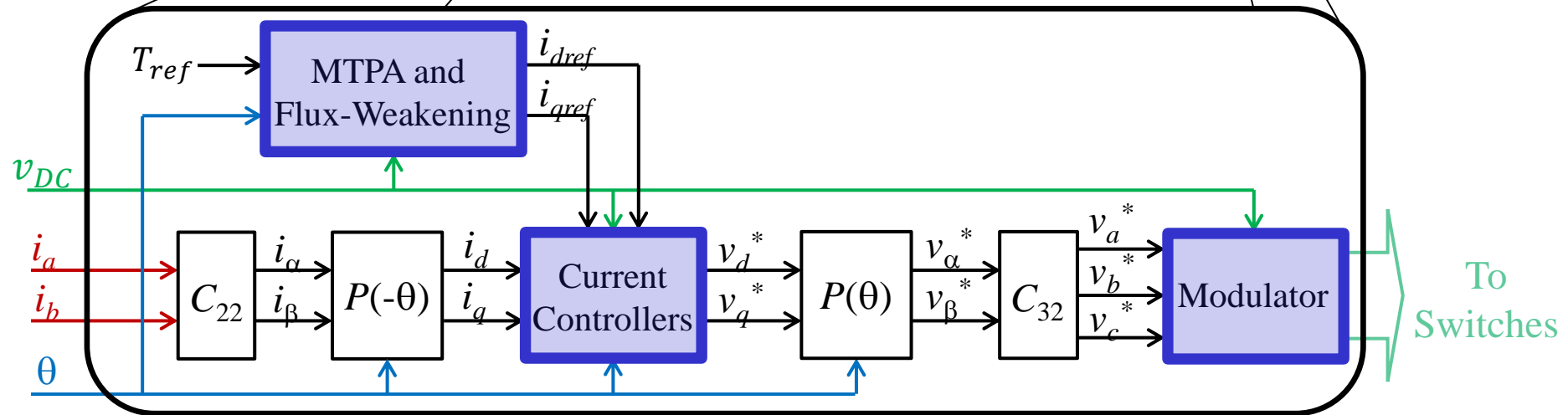
- **Control law:** Park transformation + current regulators + modulator OR switch pattern selection, flux estimator in some variants
- **Sensors:** phase current sensors and mechanical sensor, DC-link voltage sensor optional
- **Applications:** very widely applied to motor and generator control
- **Drawbacks:** cost

# Vector Control of Adjustable Speed Drives



control card

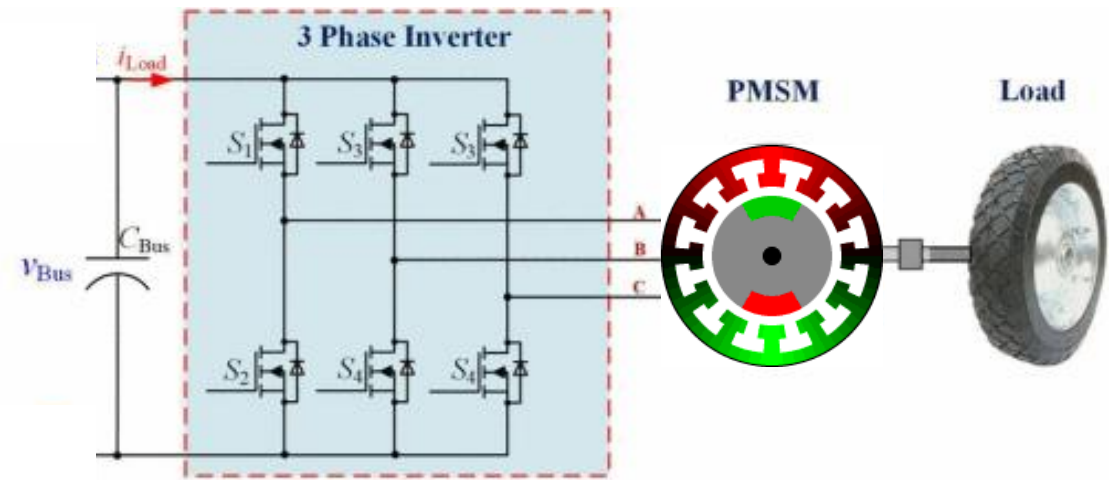
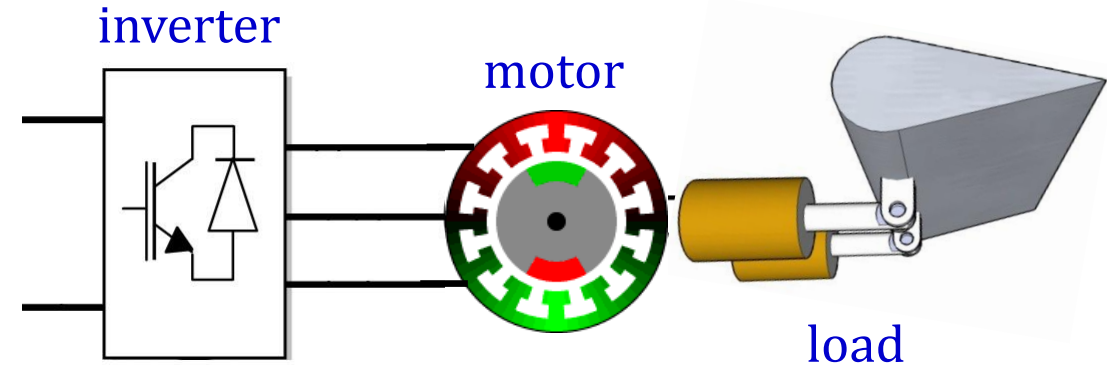
Indirect torque control:



# Motor Drives in Electrified Transportation Systems

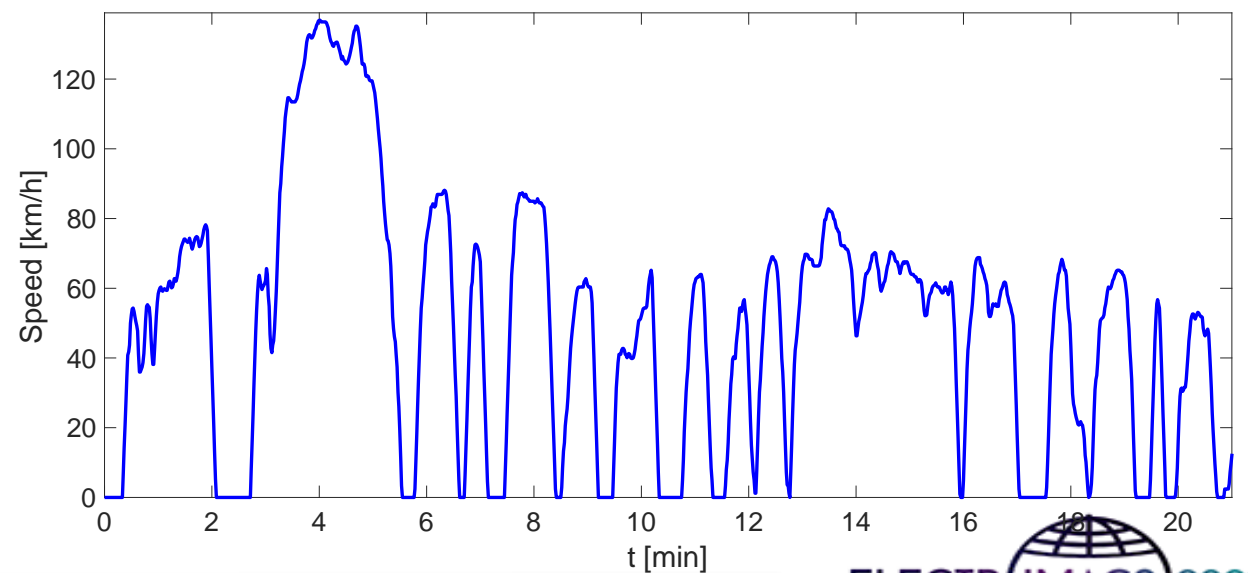
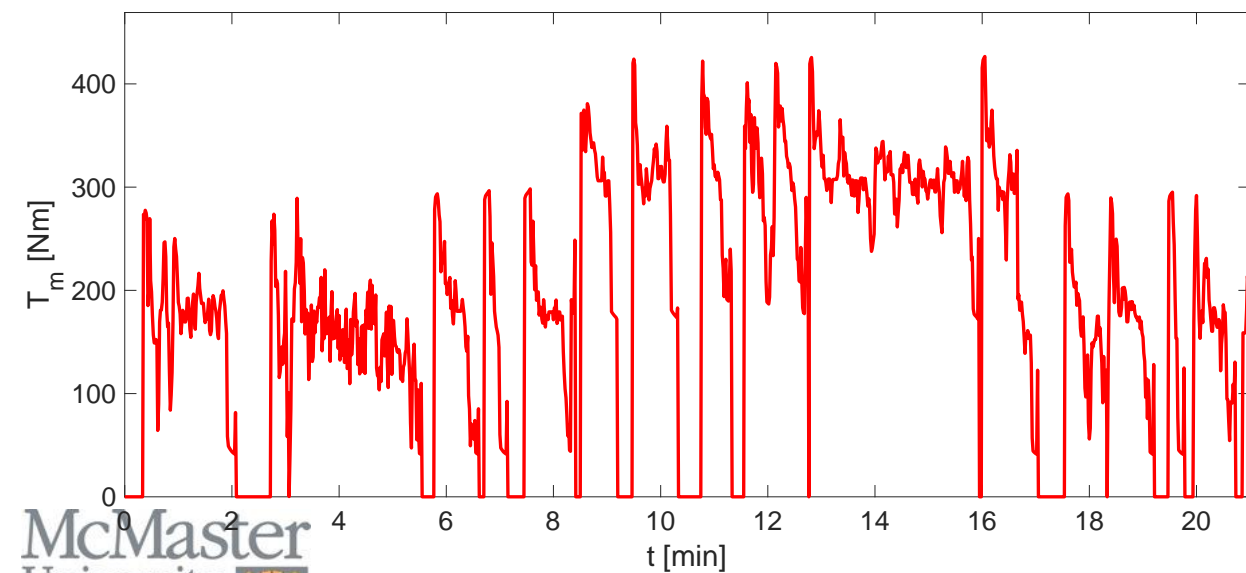
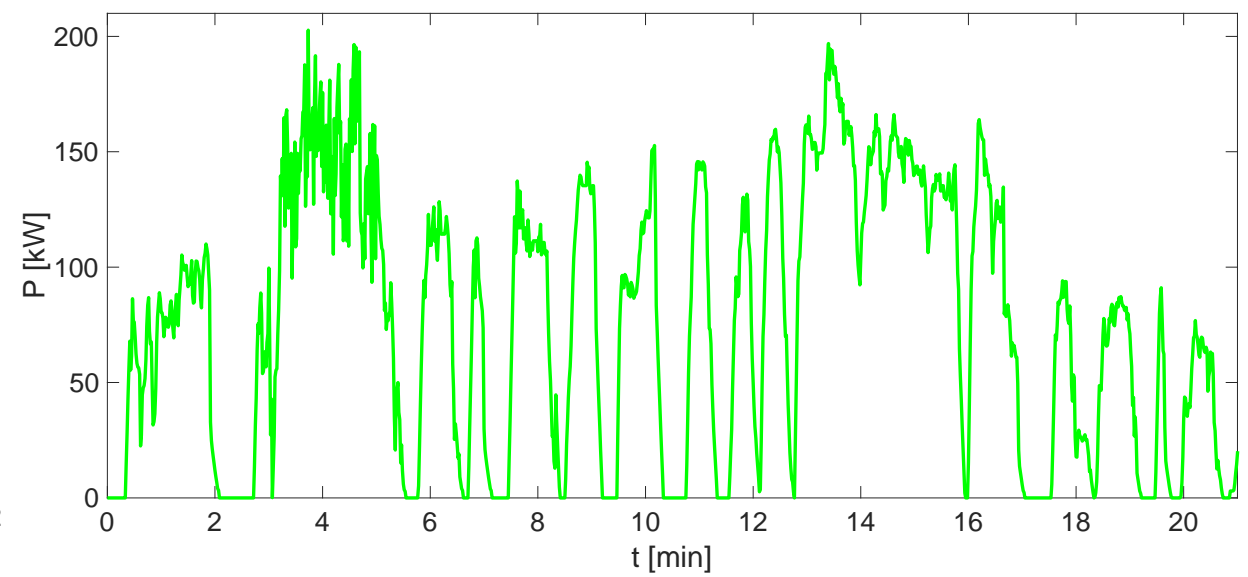
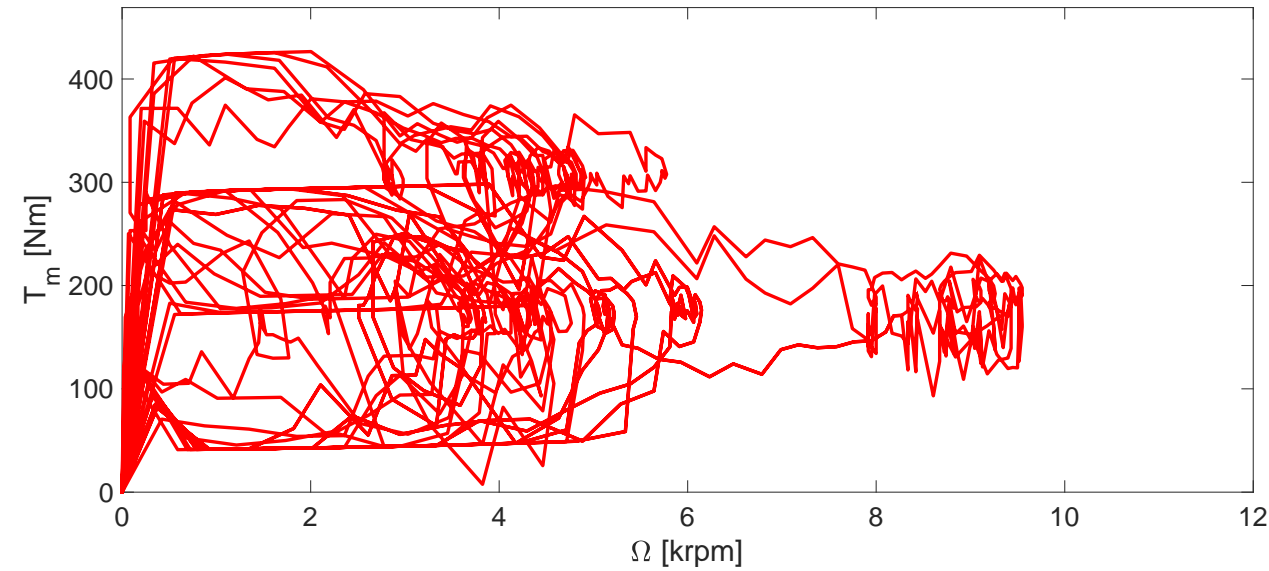
## Missions:

- Electromechanical actuators (EMA):
  - few Watts to kW motor drives
  - fixed or adjustable speed drives
- Pumps and fans:
  - hundreds of Watts to tens of kW
  - mainly adjustable speed drives
- Electric motors for propulsion/traction:
  - few kW to hundreds of kW
  - adjustable speed drives



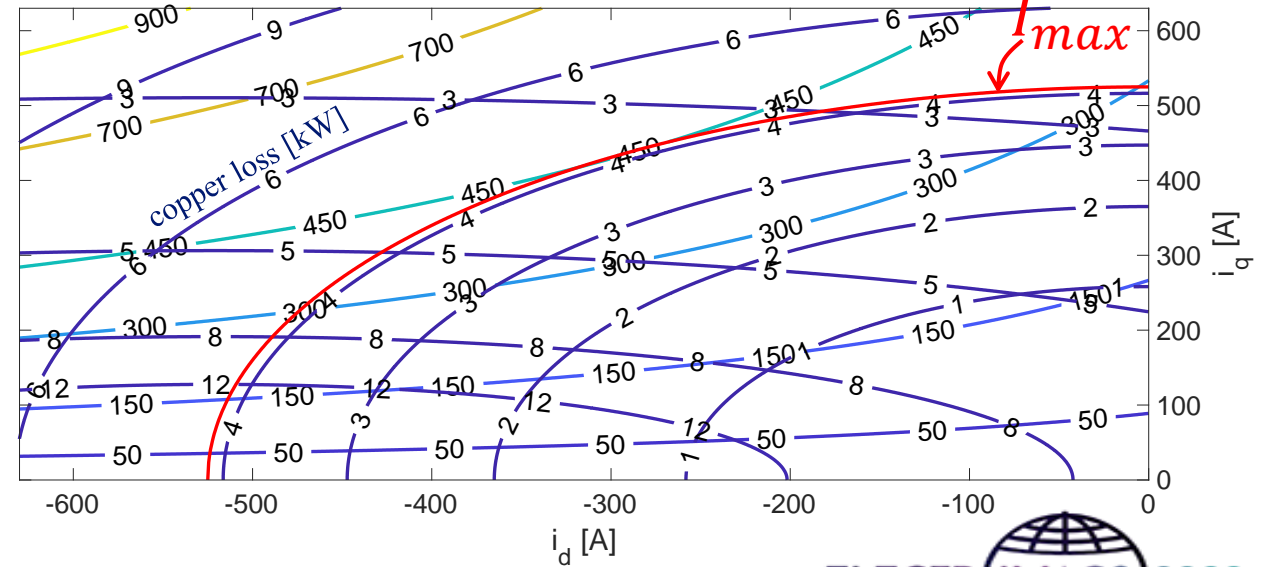
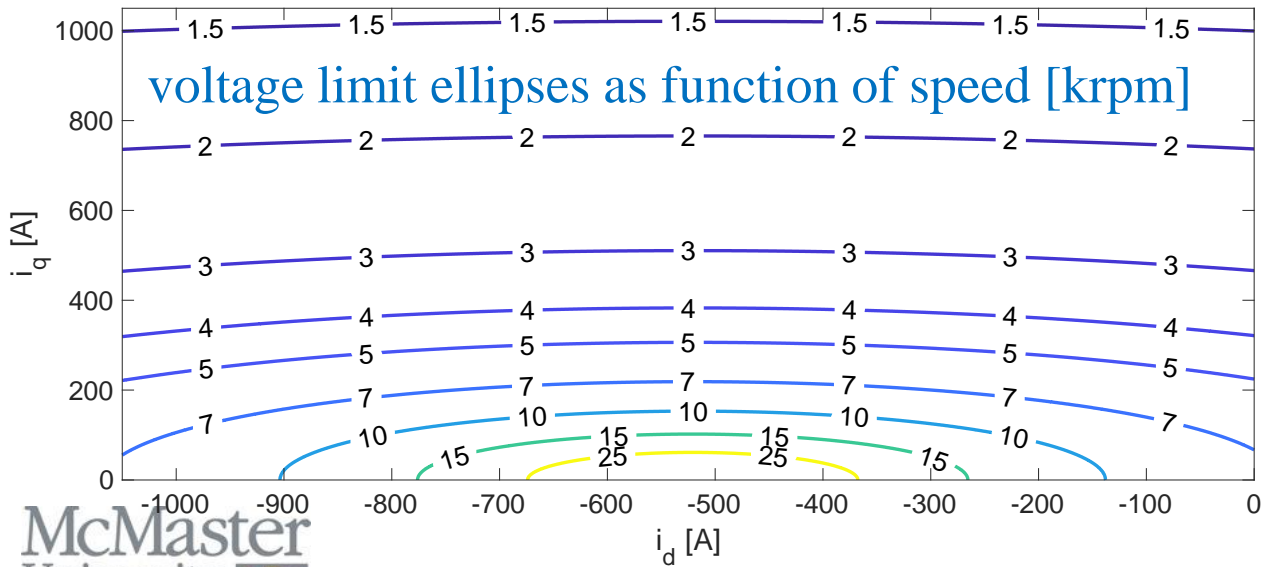
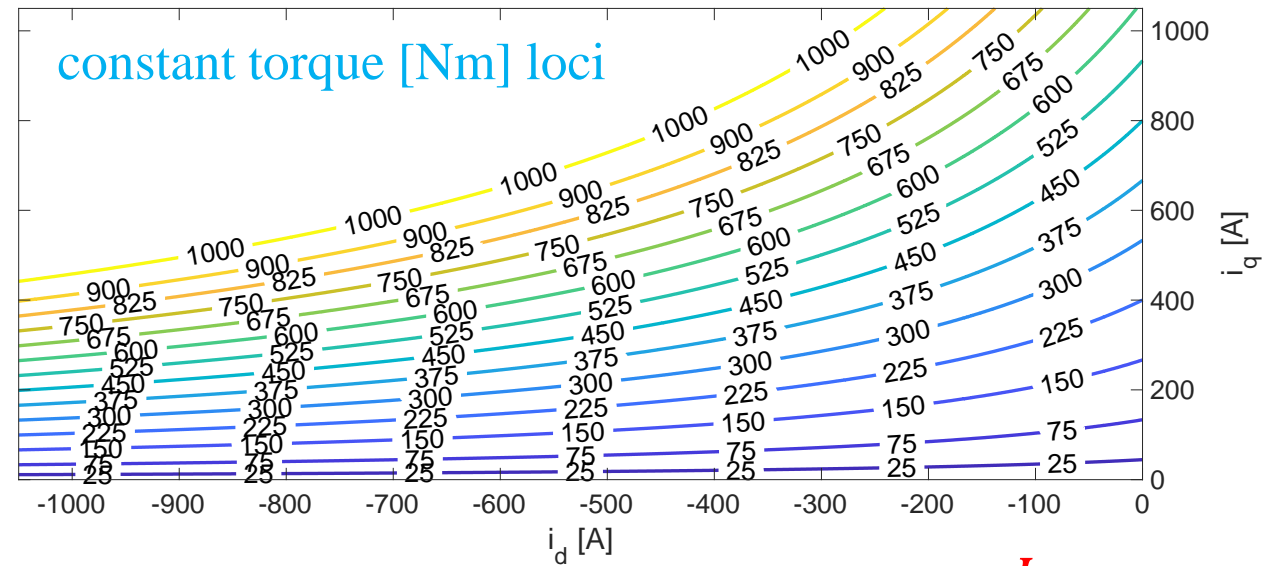
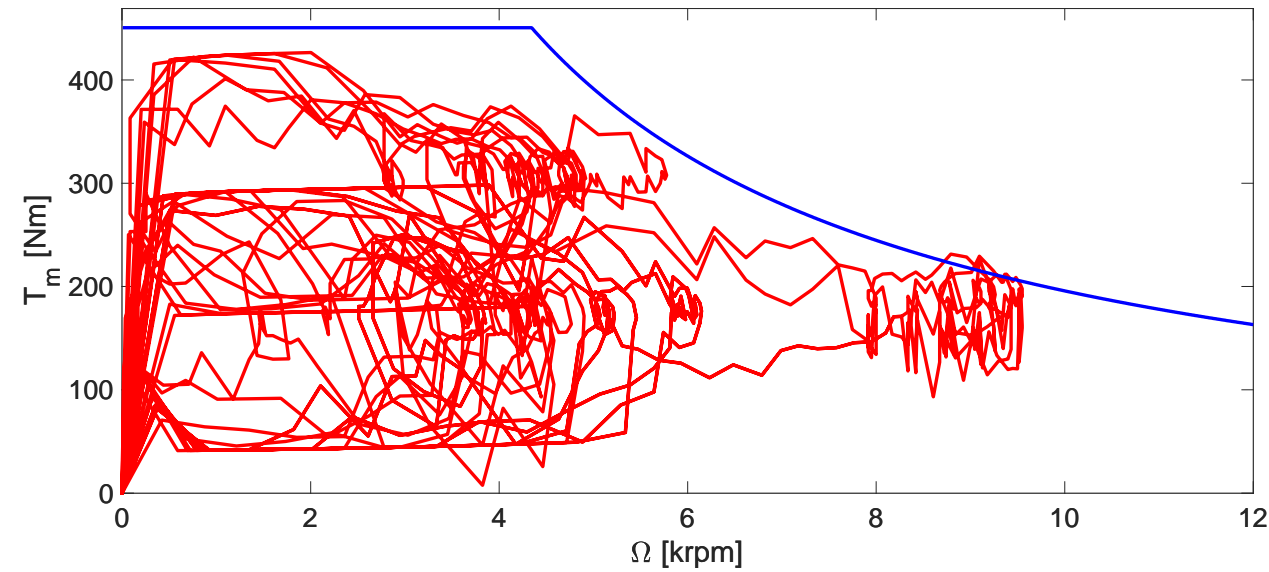
# Mission Profile: Electric Vehicle

## Urban/extra-urban vehicle

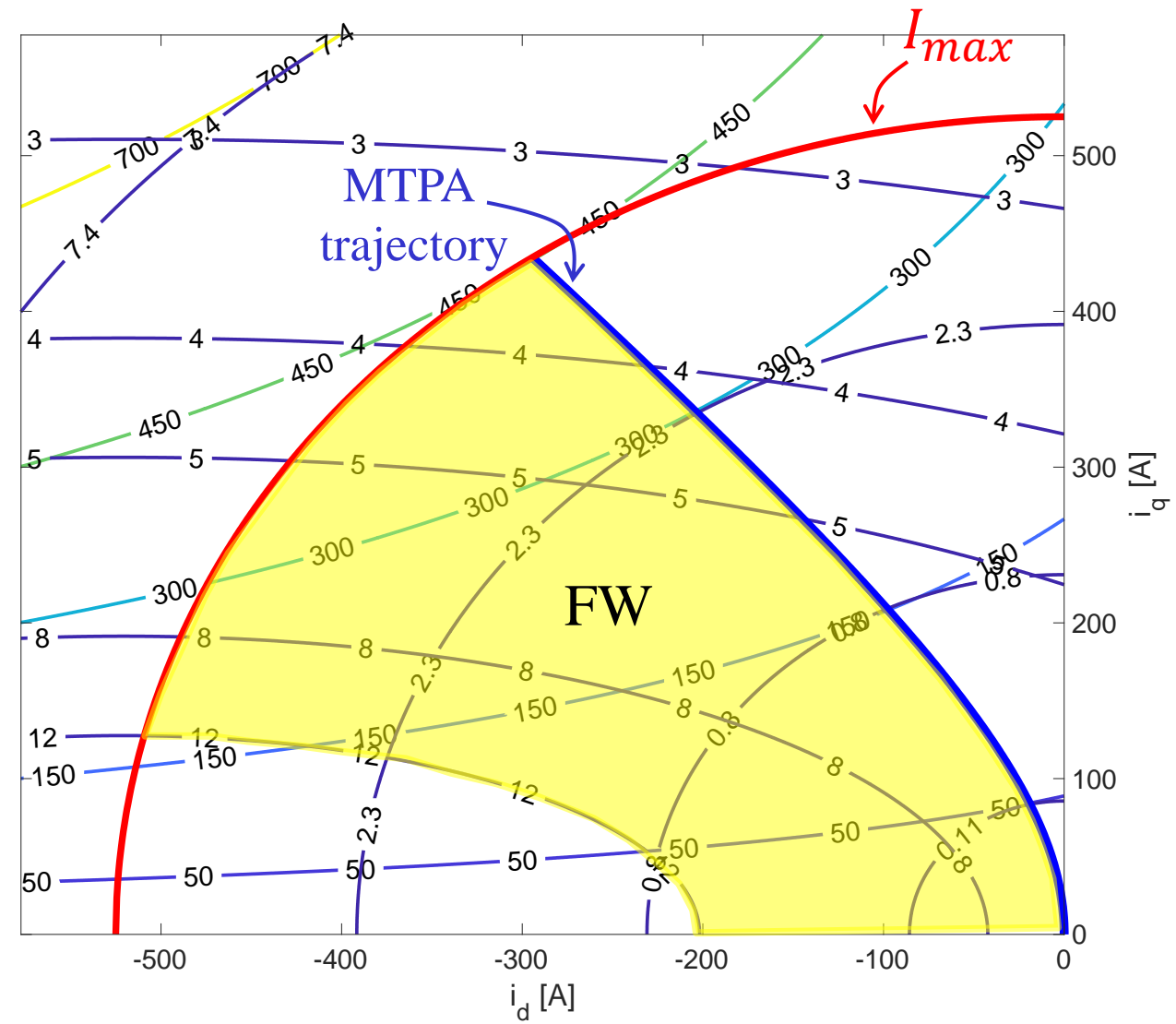
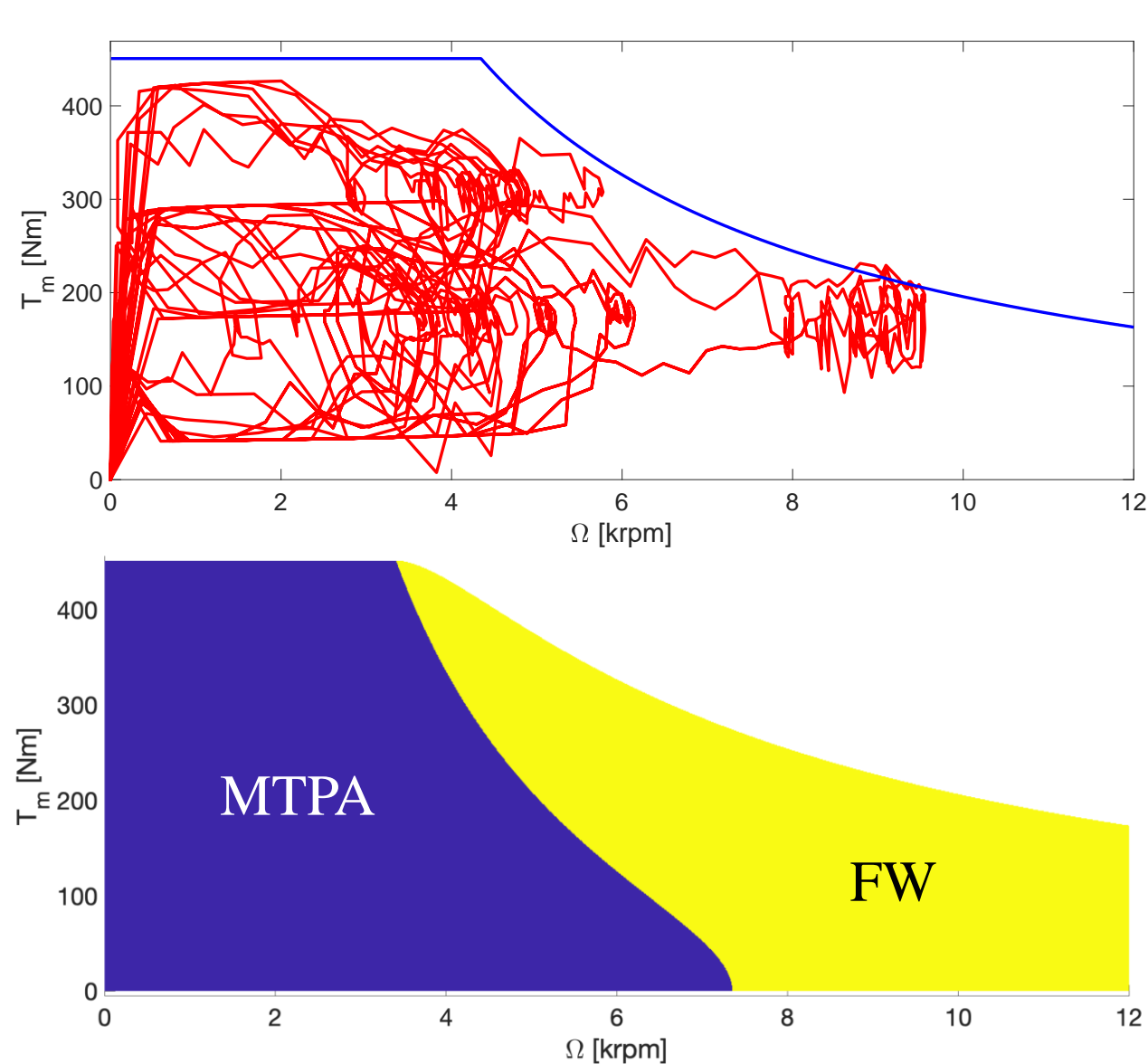


## Electric Motor Torque Control

# Adjustable Speed Drives: Torque Control Problem



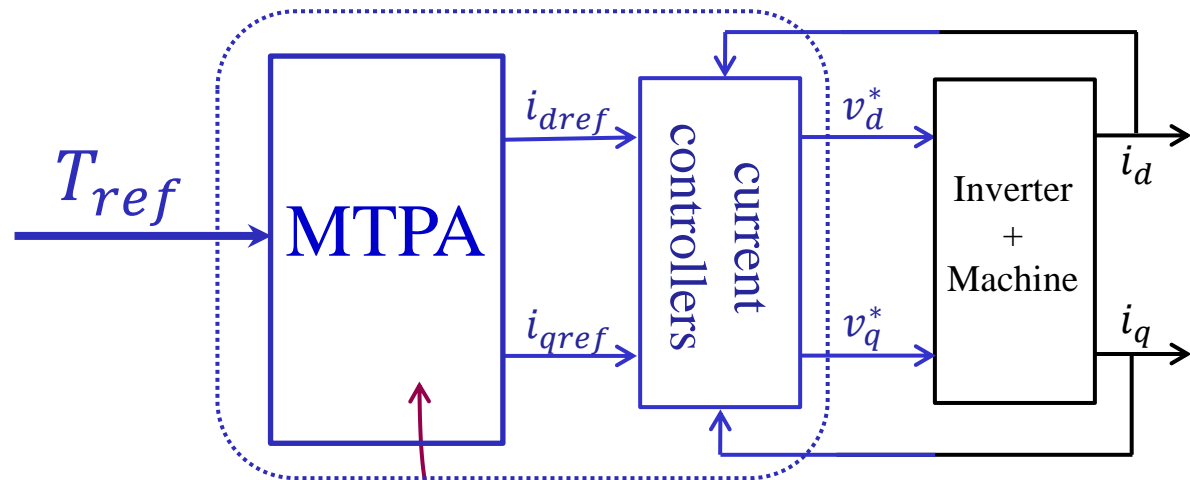
# Maximum Torque Per Ampere (MTPA) and Flux-Weakening (FW)



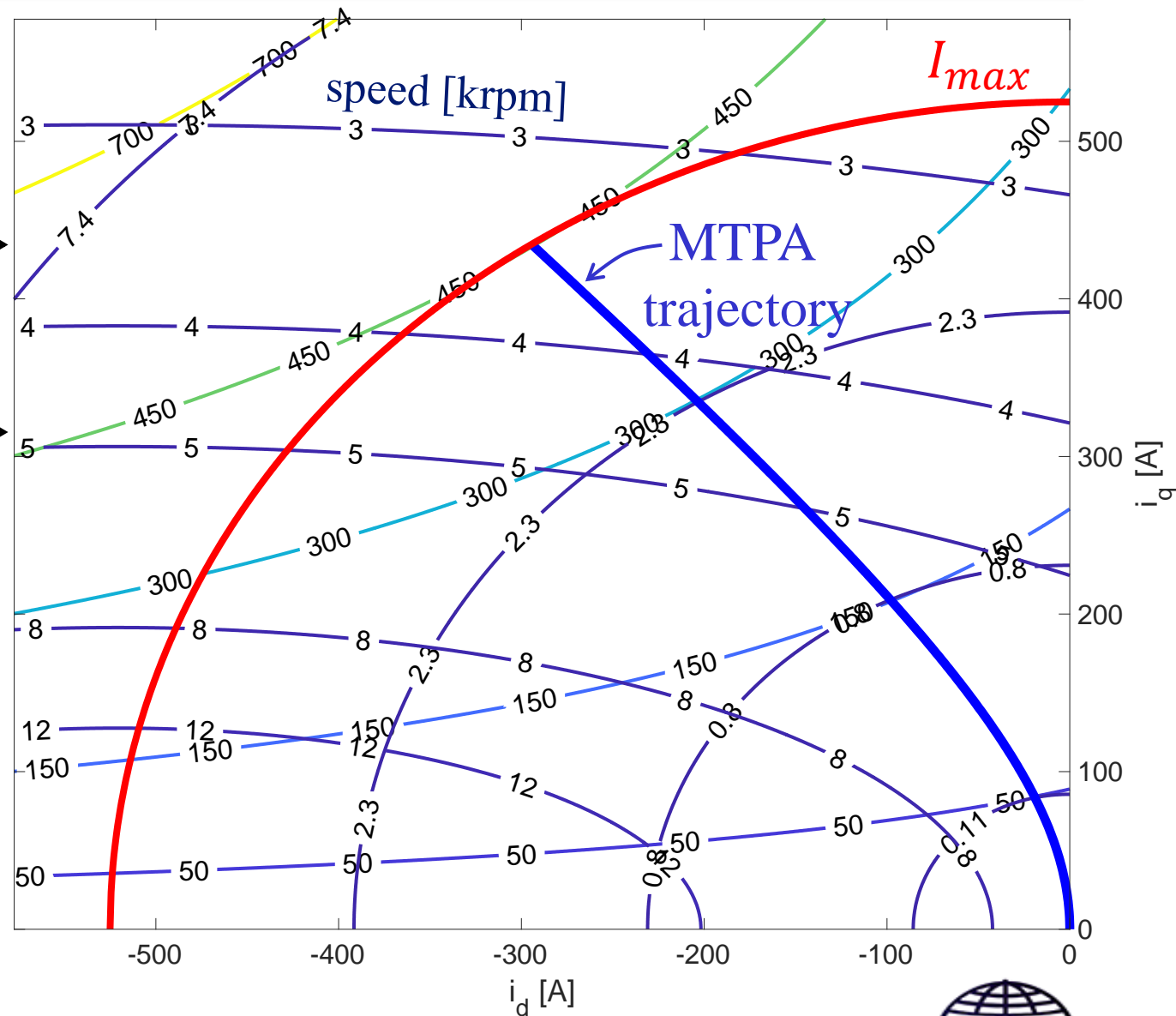


# Adjustable Speed Drives: Torque Control Strategy

## Indirect Torque Control:

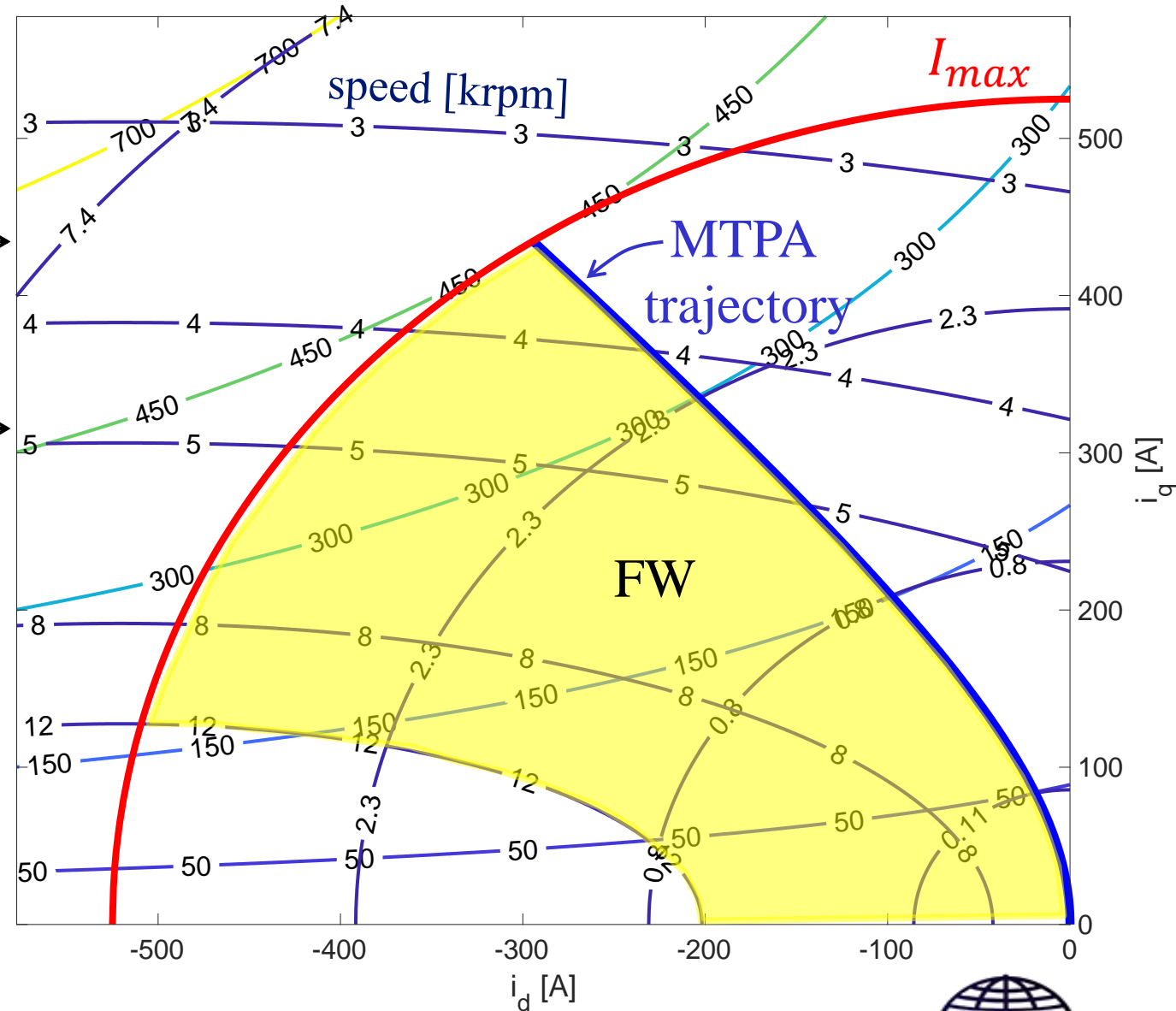
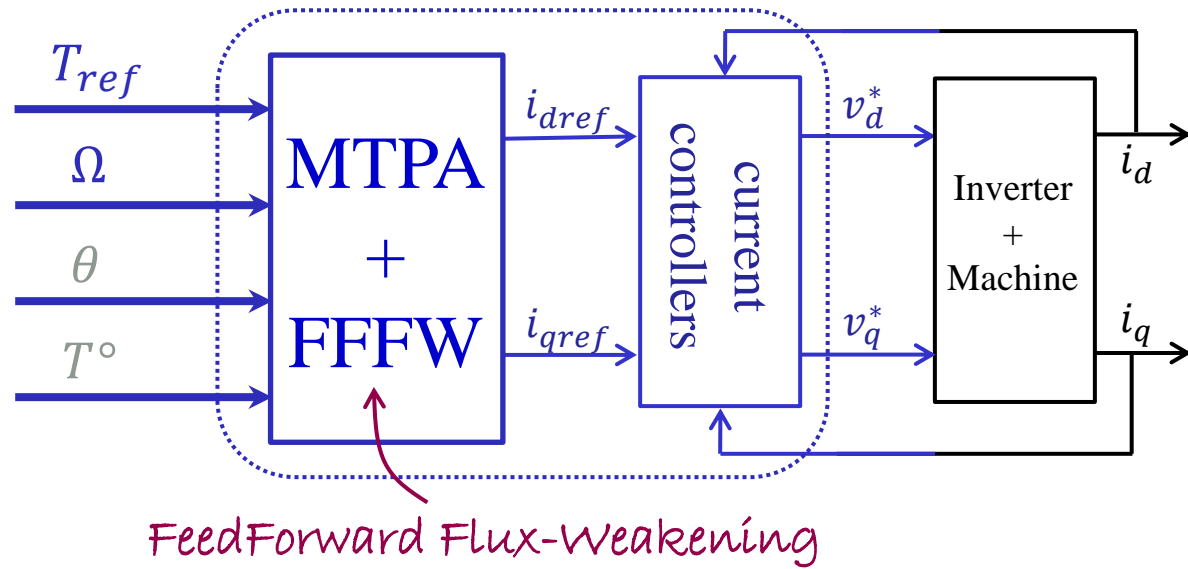


Look-up Table (LUT) for Maximum Torque Per Ampere (MTPA)



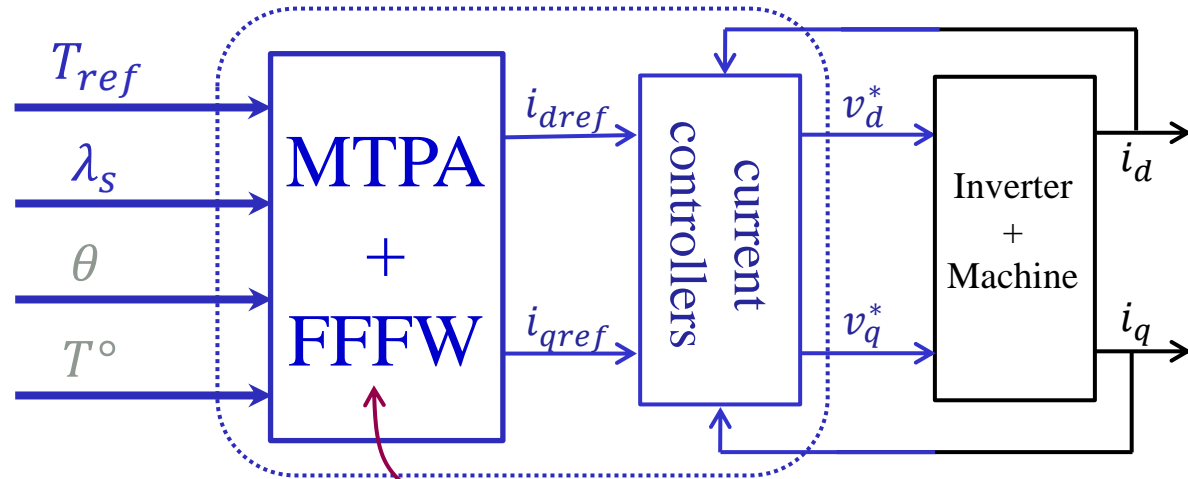
# Adjustable Speed Drives: Torque Control Strategy + FW

Indirect Torque Control:



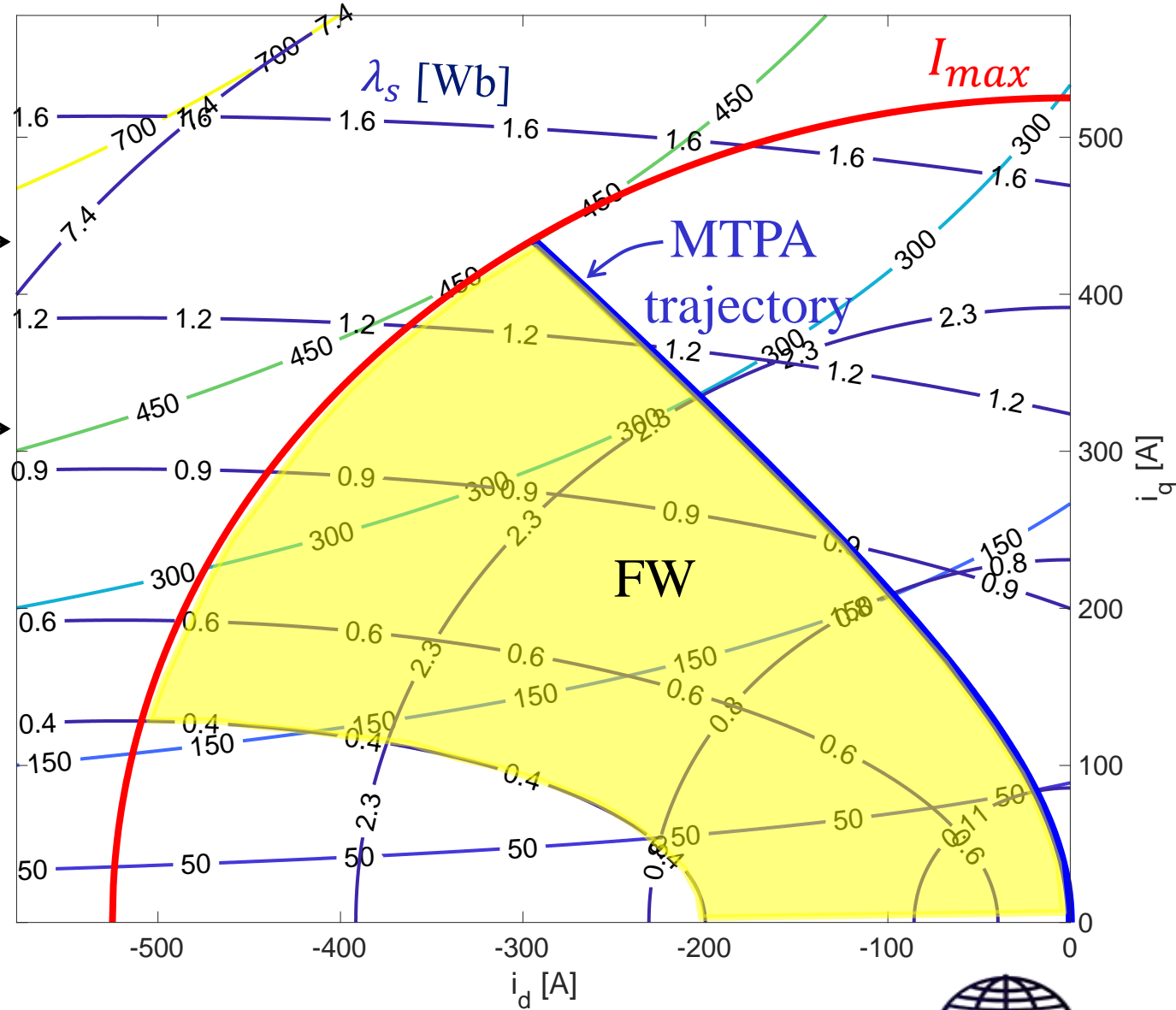
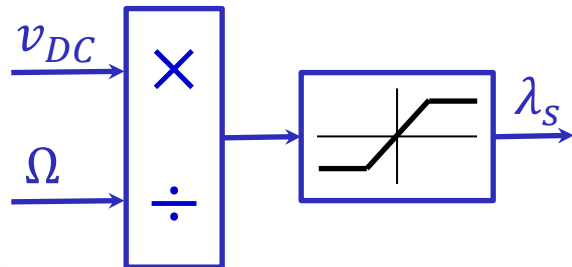
# Adjustable Speed Drives: Torque Control Strategy + FW

Indirect Torque Control:



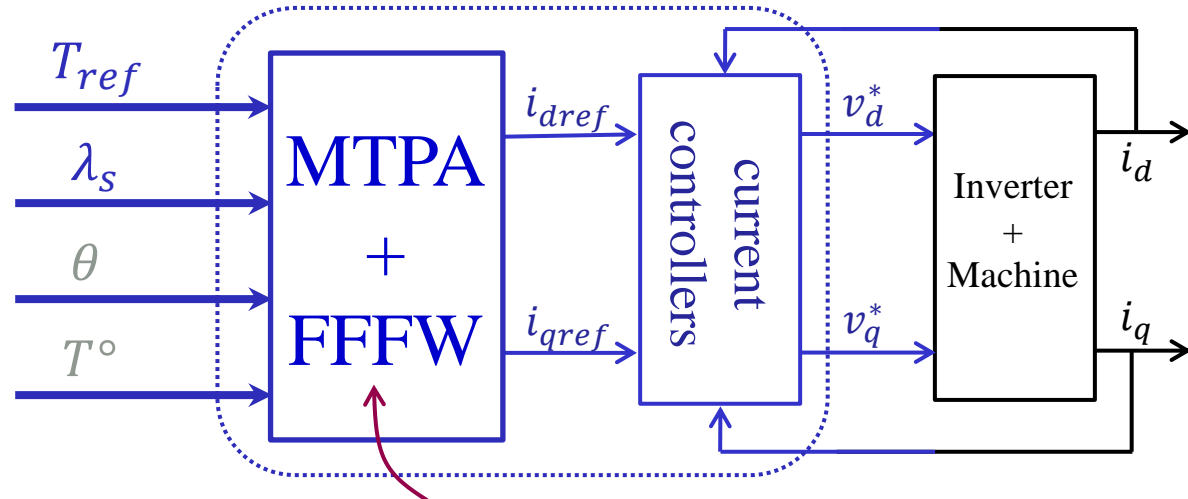
FeedForward Flux-Weakening

Advantage: Taking  $v_{DC}$  into account



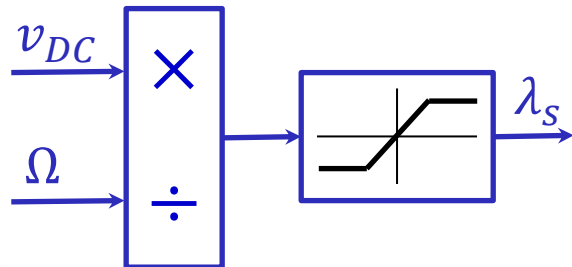
# Adjustable Speed Drives: Torque Control Strategy + FW

Indirect Torque Control:

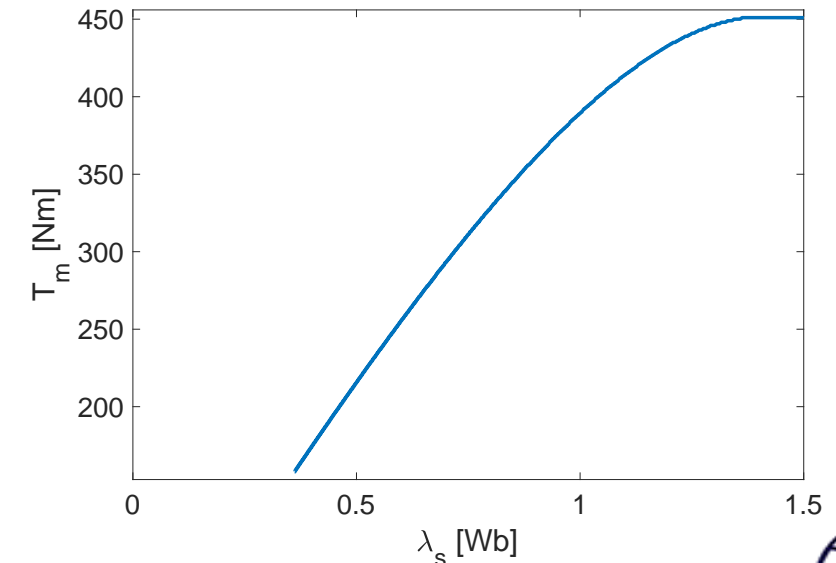
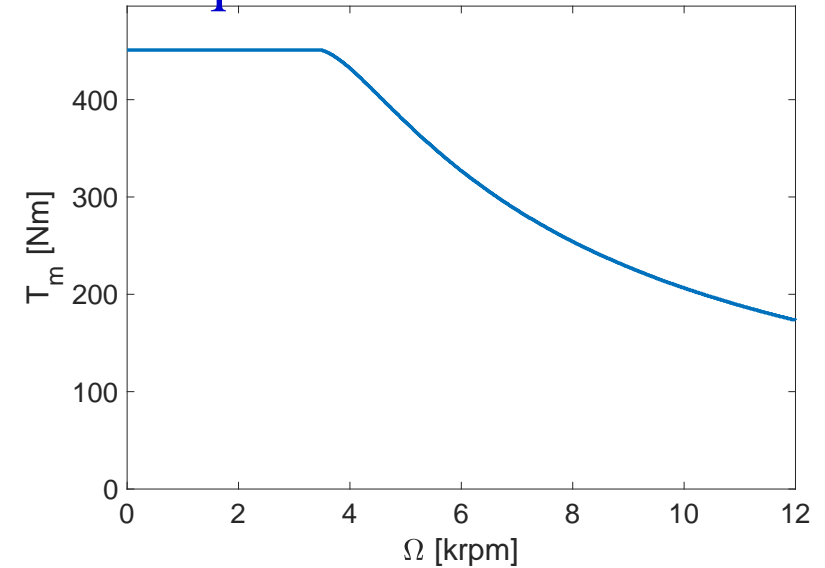


FeedForward Flux-Weakening

Advantage: Taking  $v_{DC}$  into account

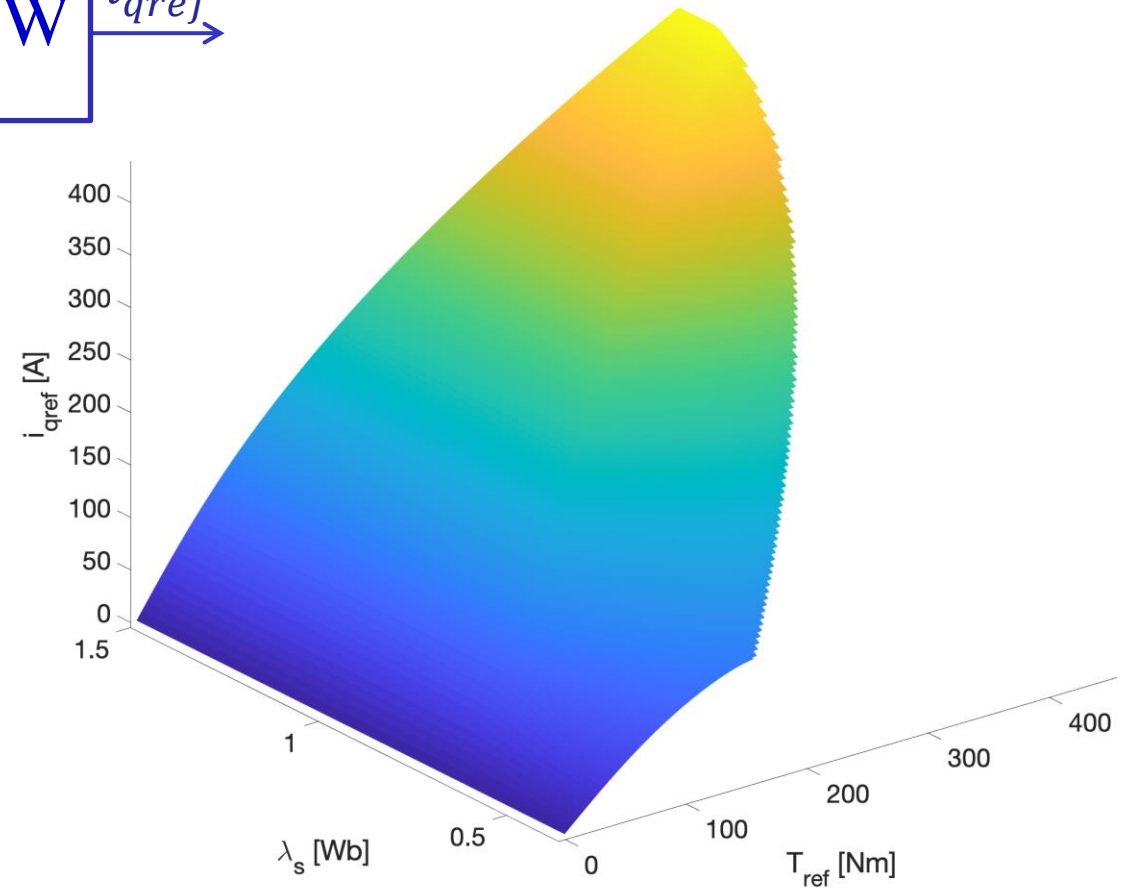
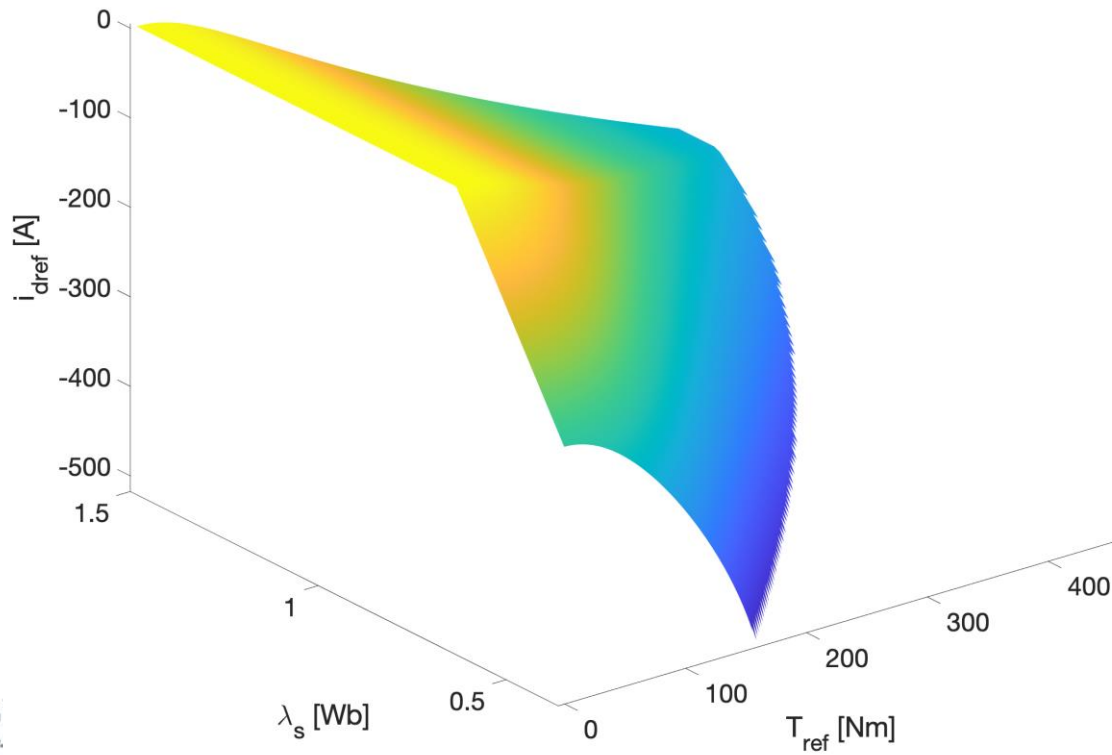
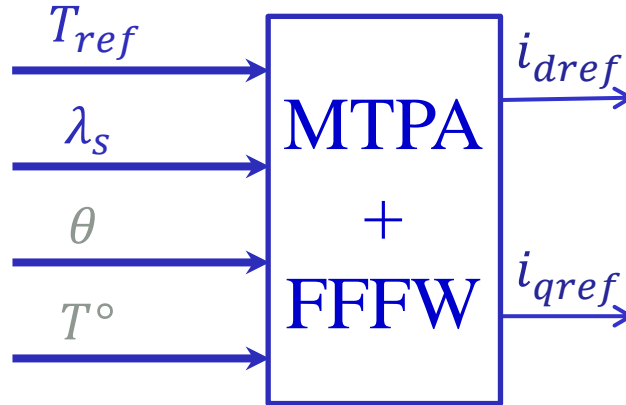


Maximum torque:



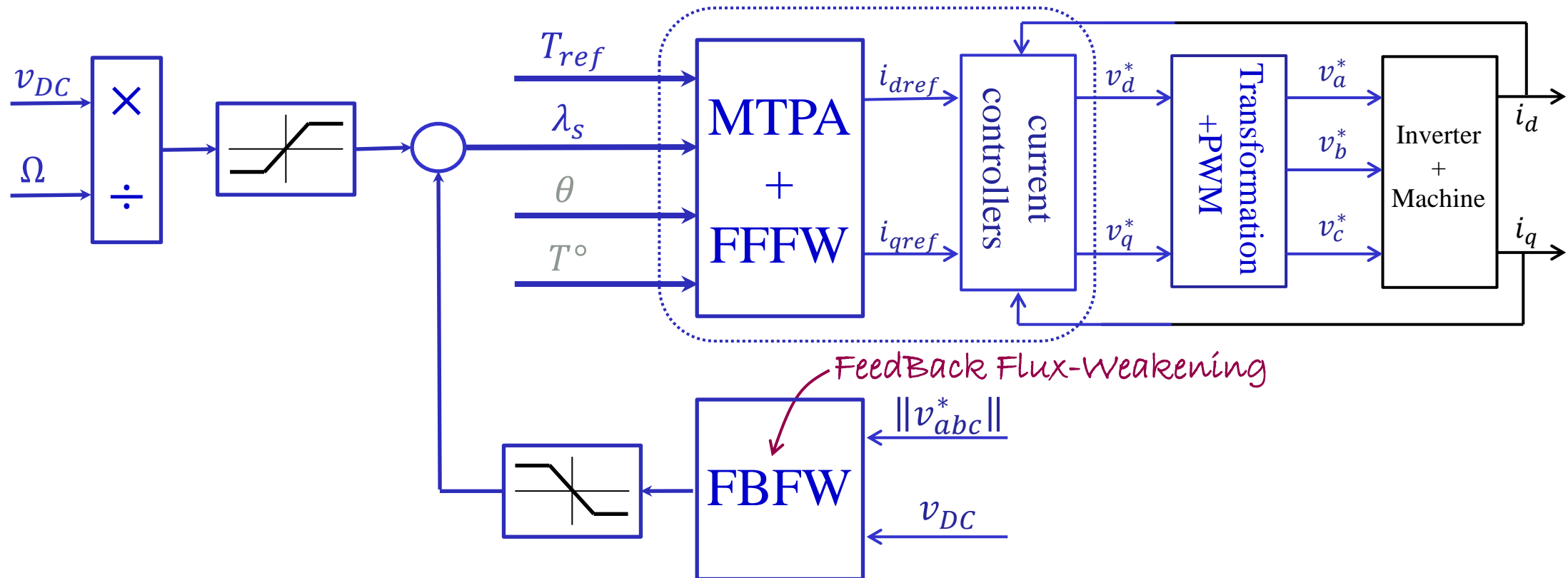
# Torque Control Strategy + FW: Current References

Look-UP Table (LUT) for torque control:



# Adjustable Speed Drives: Feedback Flux-Weakening

Torque Control Strategy:



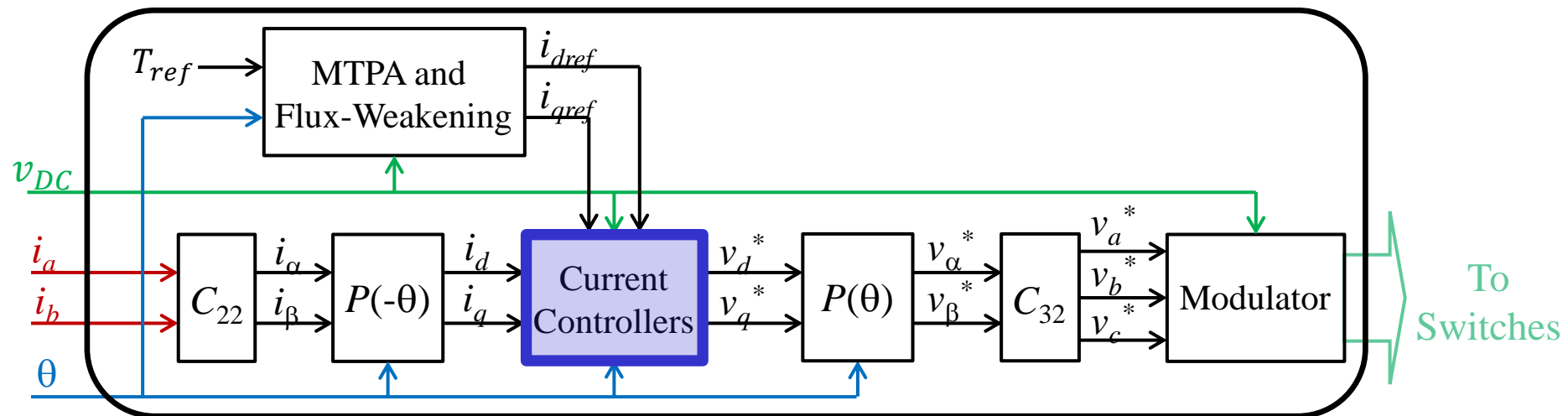
Advantage: Improvement of robustness with respect to model uncertainties

Challenges: Tuning of FBFW, anti wind-up if integral action, fast dynamic

# Electric Motor Torque Control for Electrified Transportation Systems

## Indirect Torque Control: Torque control through current control

- **Advantage:** smooth current (so torque) control
- **Challenges:** accurate model, DC-link voltage utilization, efficiency, sensorless control (cost/reliability)
- **Requirements:** look-up tables (or functions) relating torque to currents in MTPA and FW regions, current controllers



## Current Control



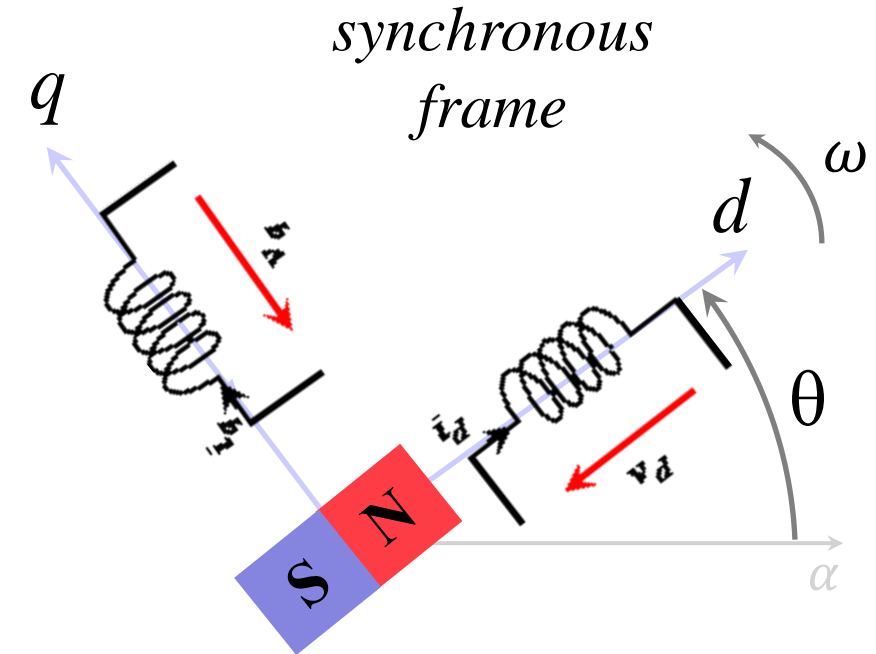
# Current Control: PMSM Model

Park model of PMSM:

$$\begin{bmatrix} v_d^* \\ v_q^* \end{bmatrix} = R_s \cdot \begin{bmatrix} i_d \\ i_q \end{bmatrix} + \frac{d}{dt} \begin{bmatrix} \psi_d \\ \psi_q \end{bmatrix} + \omega \cdot \begin{bmatrix} 0 & -1 \\ 1 & 0 \end{bmatrix} \cdot \begin{bmatrix} \psi_d \\ \psi_q \end{bmatrix} + \begin{bmatrix} \Delta v_d \\ \Delta v_q \end{bmatrix}$$

with: 
$$\begin{cases} \psi_d = L_d(i_d, i_q, \theta, T^\circ) \cdot i_d + \Psi_f(i_d, i_q, \theta, T^\circ) \\ \psi_q = L_q(i_d, i_q, \theta, T^\circ) \cdot i_q \end{cases}$$

and inverter nonlinearities: 
$$\begin{cases} \Delta v_d = \Delta V \cdot f_d(\theta) \\ \Delta v_q = \Delta V \cdot f_q(\theta) \end{cases}$$



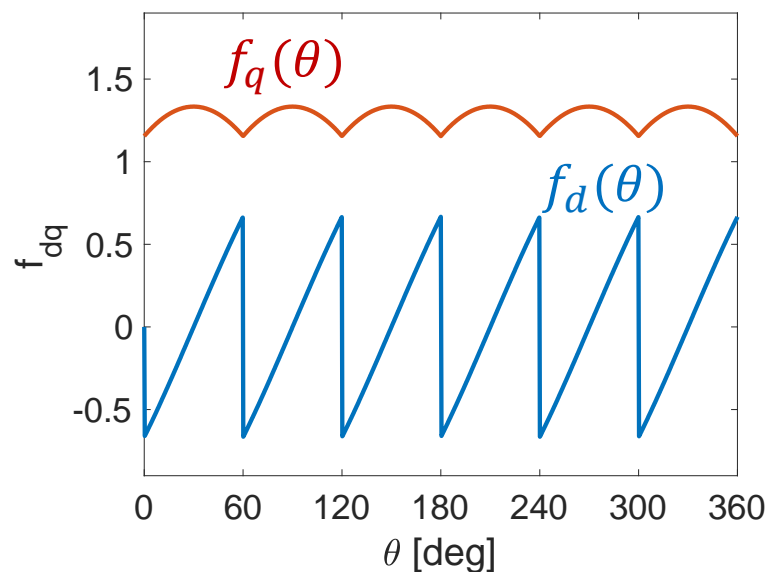
**Motor torque (Clarke transformation):**

$$T_m = \frac{3}{2} \cdot P \cdot (\psi_d \cdot i_q - \psi_q \cdot i_d) = \frac{3}{2} \cdot P \cdot [\Psi_f + (L_d - L_q) \cdot i_d] \cdot i_q$$

# Current Control: PMSM Model

Modeling: voltage drops in the inverter

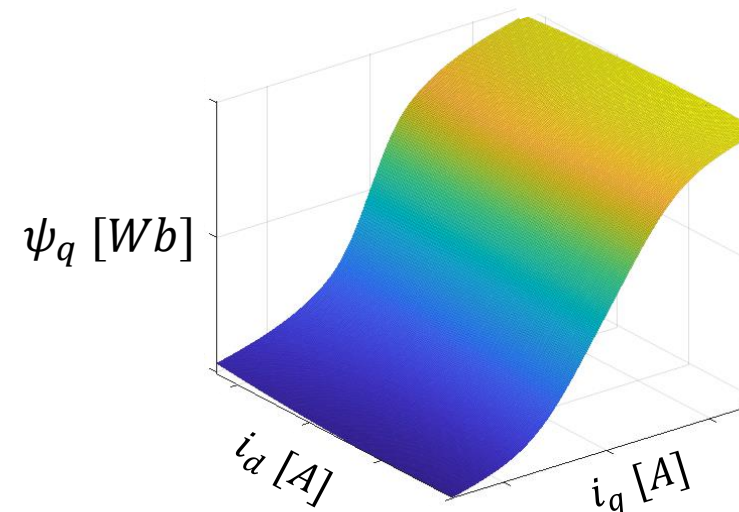
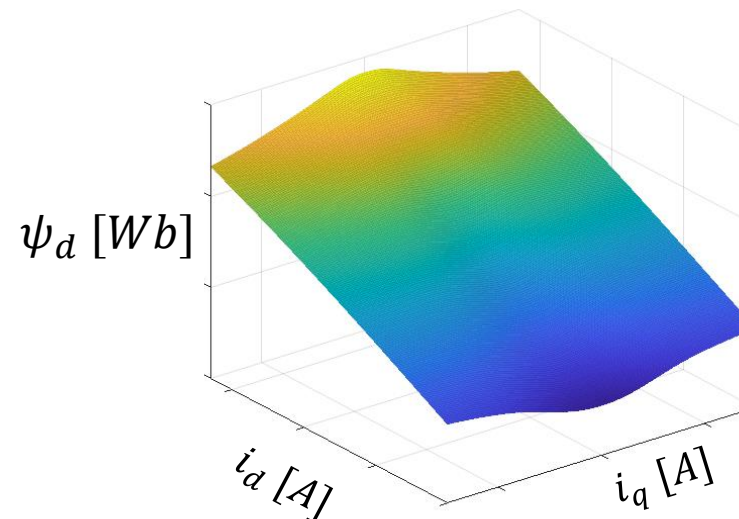
$$\begin{cases} \Delta v_d = \Delta V \cdot f_d(\theta) \\ \Delta v_q = \Delta V \cdot f_q(\theta) \end{cases}$$



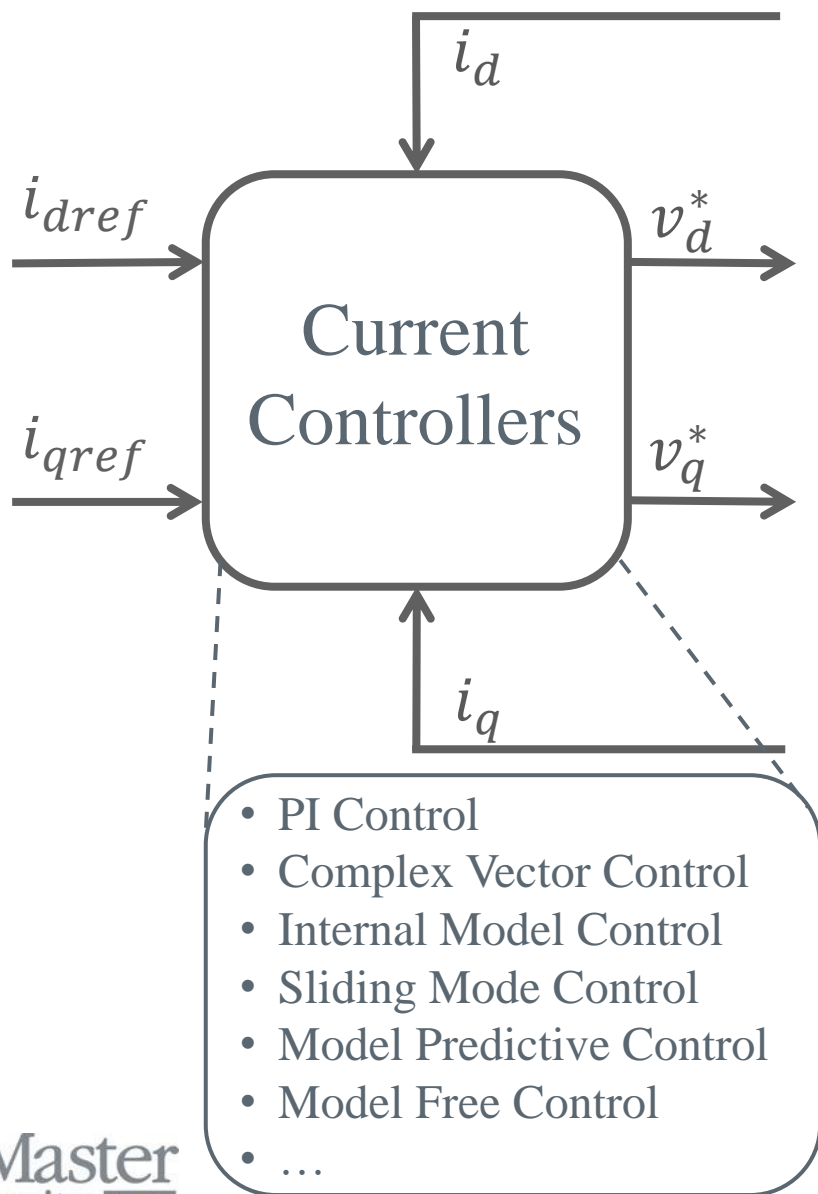
Self-commissioning:

- Estimation of  $R_s$
- Estimation of  $\Delta V$
- Estimation of  $\Psi_f$

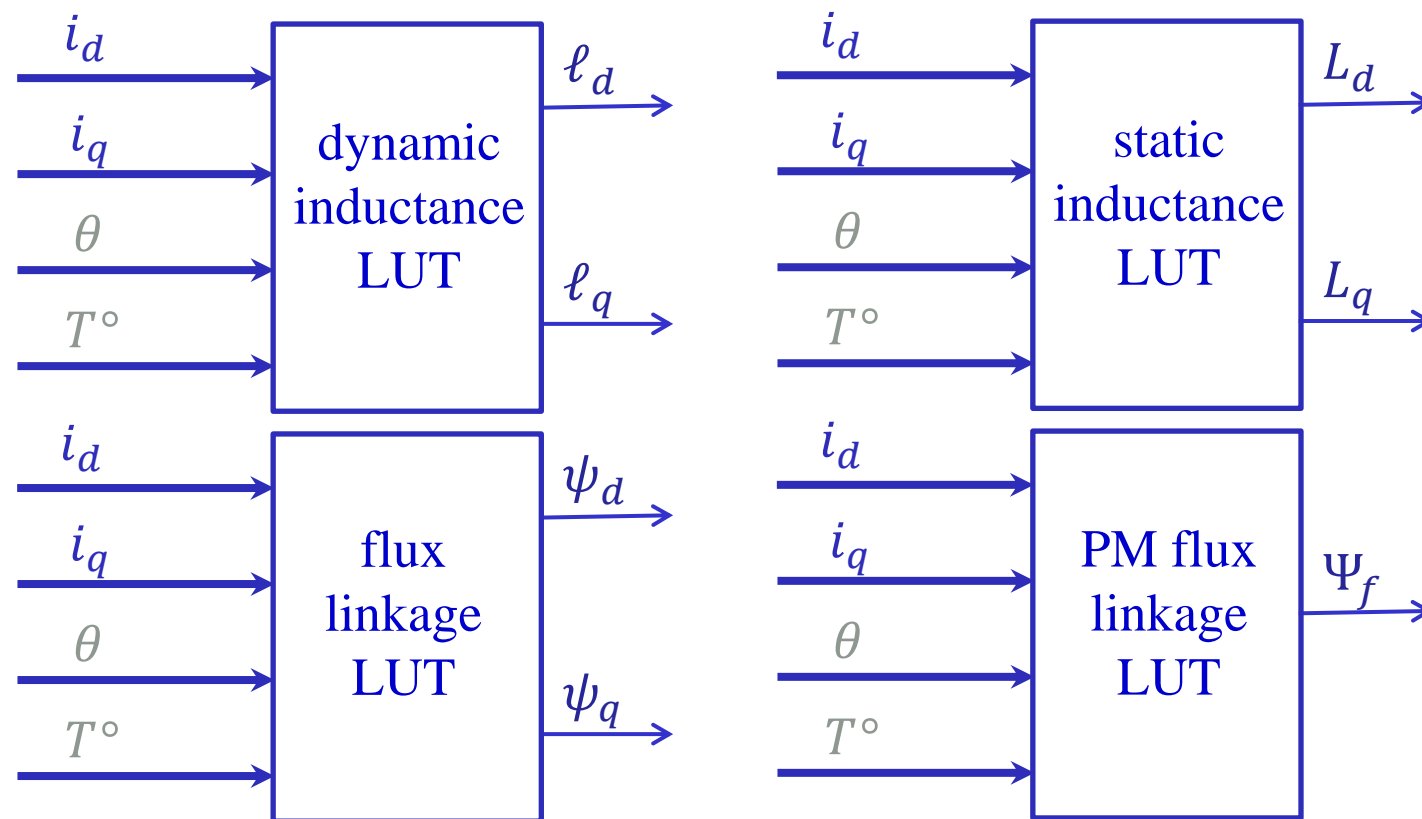
Modeling: mapping flux linkages



# PMSM Current Control

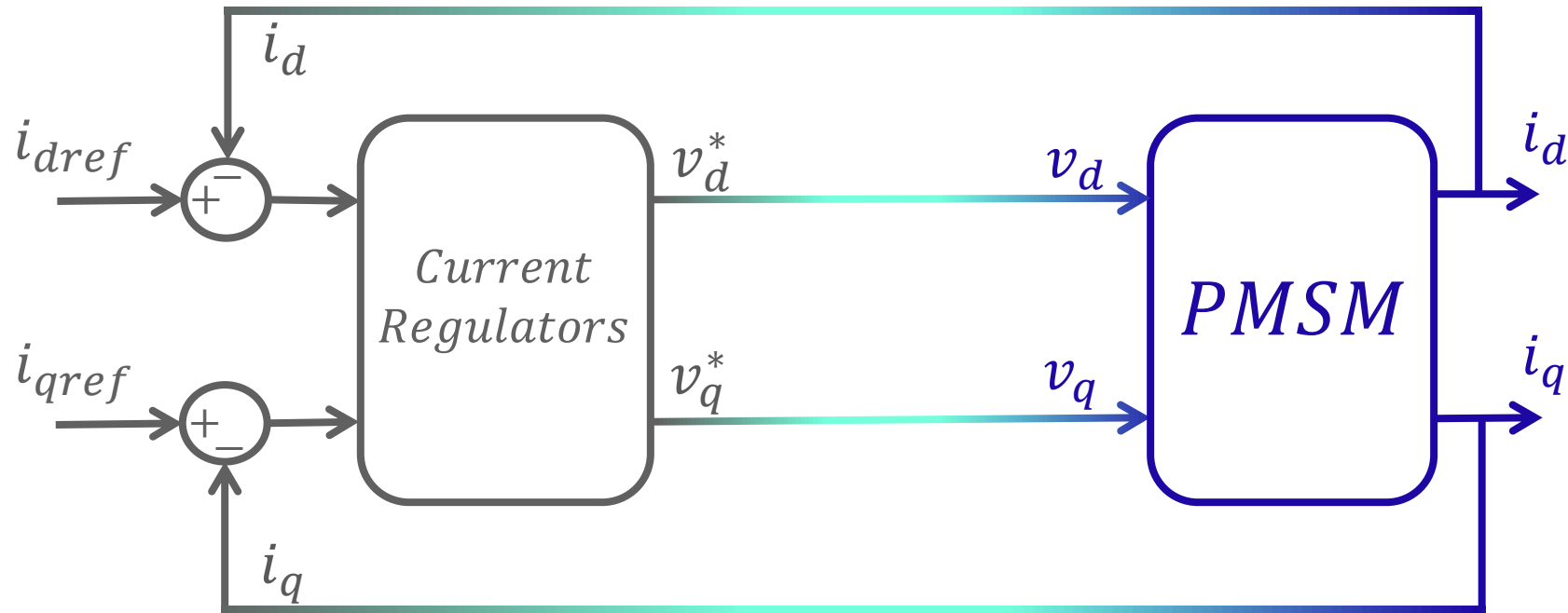


Model-based control: available knowledge on the model under look-up table (LUT) form



Definition:  $\ell_d = \frac{\partial \psi_d}{\partial i_d}$ ,  $\ell_q = \frac{\partial \psi_q}{\partial i_q}$ ,  $L_d = \frac{\psi_d - \Psi_f}{i_d}$ ,  $L_q = \frac{\psi_q}{i_q}$

# PMSM Current Control: Design and Analysis



## Current control objectives:

- Zero steady-state error:  $\lim_{t \rightarrow \infty} i_{dq}(t) = i_{dqref}$
- No overshoot (or overshoot  $< 5\% \sim 10\%$ )
- Requested response time  $t_r$  (in  $ms$ ) or current (torque) control bandwidth (in Hz or rad/s)
- Fast set-point tracking with small tracking error

# PI Current Control: Design

Current controller transfer function:

$$\begin{bmatrix} \tilde{v}_d^* \\ \tilde{v}_q^* \end{bmatrix} = C(s) \cdot \left\{ \begin{bmatrix} \tilde{i}_{dref} \\ \tilde{i}_{qref} \end{bmatrix} - \begin{bmatrix} \tilde{i}_d \\ \tilde{i}_q \end{bmatrix} \right\}$$

Controller transfer function **without decoupling**:

$$C(s) = \begin{bmatrix} K_{pd} \frac{1 + \tau_{id} \cdot s}{\tau_{id} \cdot s} & 0 \\ 0 & K_{pq} \frac{1 + \tau_{iq} \cdot s}{\tau_{iq} \cdot s} \end{bmatrix}$$

$$K_{id} = R_s \cdot \omega_{BWd}$$

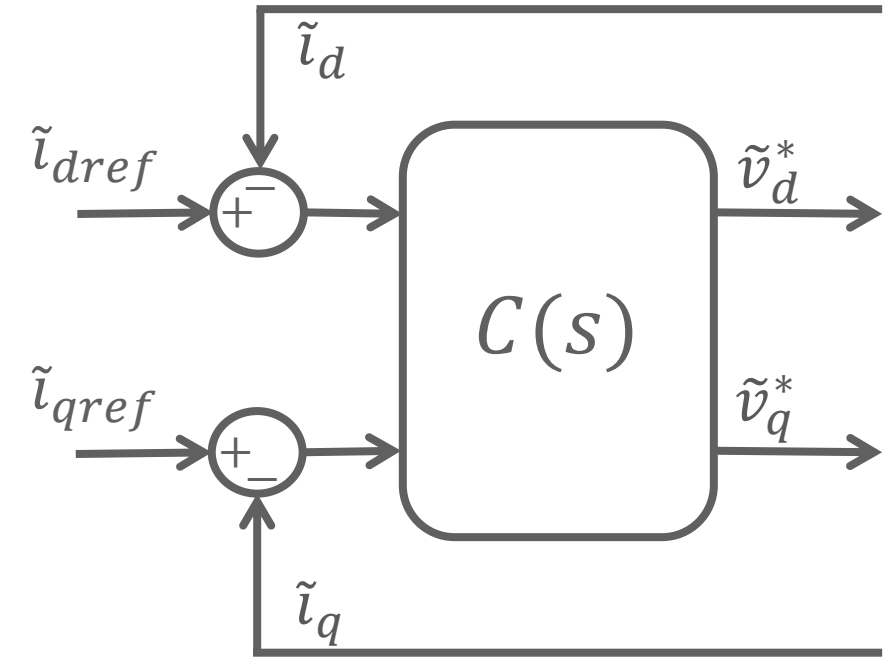
$$K_{pd} = \ell_d \cdot \omega_{BWd} \quad \text{desired bandwidth of } d \text{ - current control loop}$$

$$\tau_{id} = K_{pd} / K_{id}$$

$$K_{iq} = R_s \cdot \omega_{BWq} \quad \text{desired bandwidth of } q \text{ - current control loop}$$

$$K_{pq} = \ell_q \cdot \omega_{BWq}$$

$$\tau_{iq} = K_{pq} / K_{iq}$$



# PI Current Control: Analysis

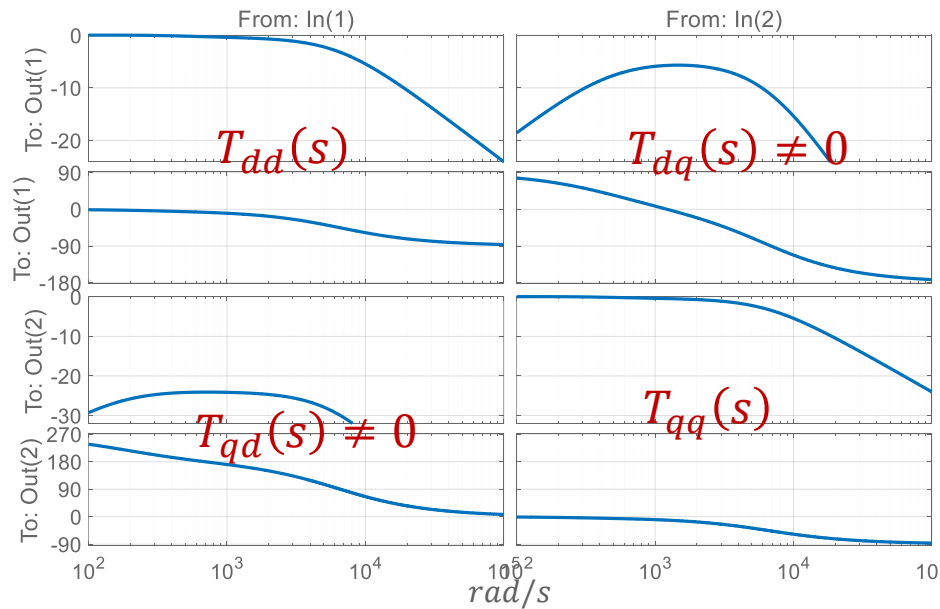
## Closed-loop transfer function: **without decoupling**

$$\begin{bmatrix} \tilde{i}_d \\ \tilde{i}_q \end{bmatrix} = [I + Y(s) \cdot C(s)]^{-1} \cdot Y(s) \cdot C(s) \cdot \begin{bmatrix} \tilde{i}_{dref} \\ \tilde{i}_{qref} \end{bmatrix} = \begin{bmatrix} T_{dd}(s) & T_{dq}(s) \\ T_{qd}(s) & T_{qq}(s) \end{bmatrix} \cdot \begin{bmatrix} \tilde{i}_{dref} \\ \tilde{i}_{qref} \end{bmatrix}$$

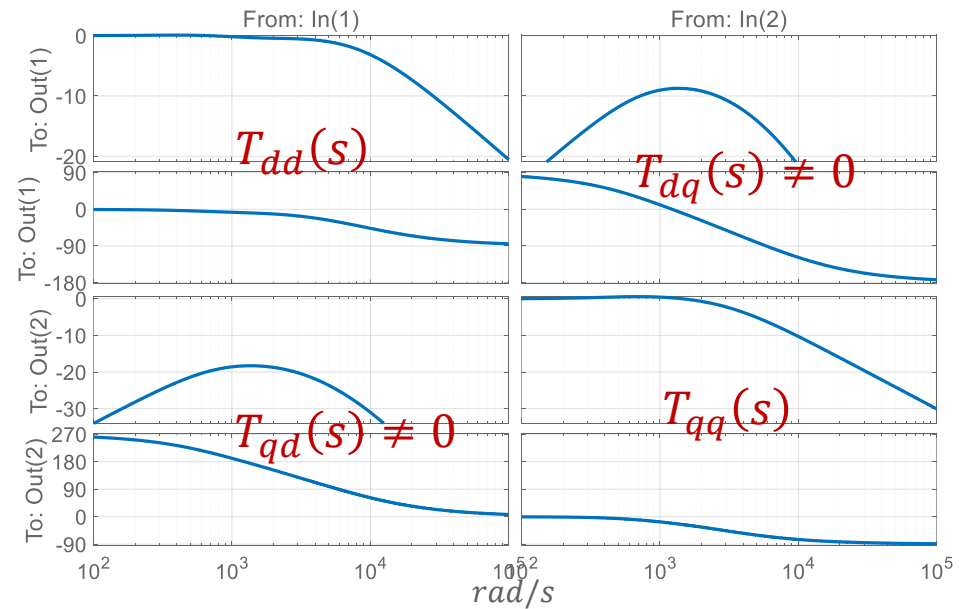
*identity matrix*

$$\Rightarrow \begin{cases} \tilde{i}_d = T_{dd}(s) \cdot \tilde{i}_{dref} + T_{dq}(s) \cdot \tilde{i}_{qref} \\ \tilde{i}_q = T_{qd}(s) \cdot \tilde{i}_{dref} + T_{qq}(s) \cdot \tilde{i}_{qref} \end{cases}$$

### known model



### parameters uncertainty



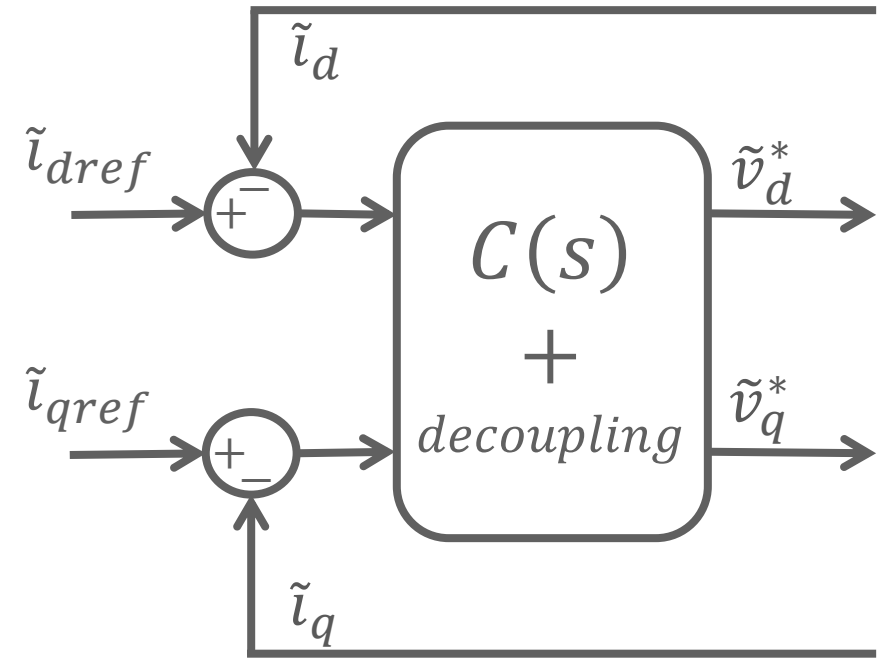
# PI Current Control + Feedforward Decoupling: Design

Current controller transfer function:

$$\begin{bmatrix} \tilde{v}_d^* \\ \tilde{v}_q^* \end{bmatrix} = C(s) \cdot \left\{ \begin{bmatrix} \tilde{i}_{dref} \\ \tilde{i}_{qref} \end{bmatrix} - \begin{bmatrix} \tilde{i}_d \\ \tilde{i}_q \end{bmatrix} \right\}$$

$$K_{pd} = \ell_d \cdot \omega_{BWd} \quad K_{pq} = \ell_q \cdot \omega_{BWq}$$

$$\tau_{id} = \ell_d / R_s \quad \tau_{iq} = \ell_q / R_s$$



With **feedforward decoupling**, it yields:

$$C(s) = \begin{bmatrix} 1 & \frac{-L_q \omega}{R_s + L_q \cdot s} \\ \frac{L_d \omega}{R_s + L_d \cdot s} & 1 \end{bmatrix} \cdot \begin{bmatrix} K_{pd} \frac{1 + \tau_{id} \cdot s}{\tau_{id} \cdot s} & 0 \\ 0 & K_{pq} \frac{1 + \tau_{iq} \cdot s}{\tau_{iq} \cdot s} \end{bmatrix}$$

# PI Current Control + Feedback Decoupling: Design

With **feedback decoupling**, it gives:

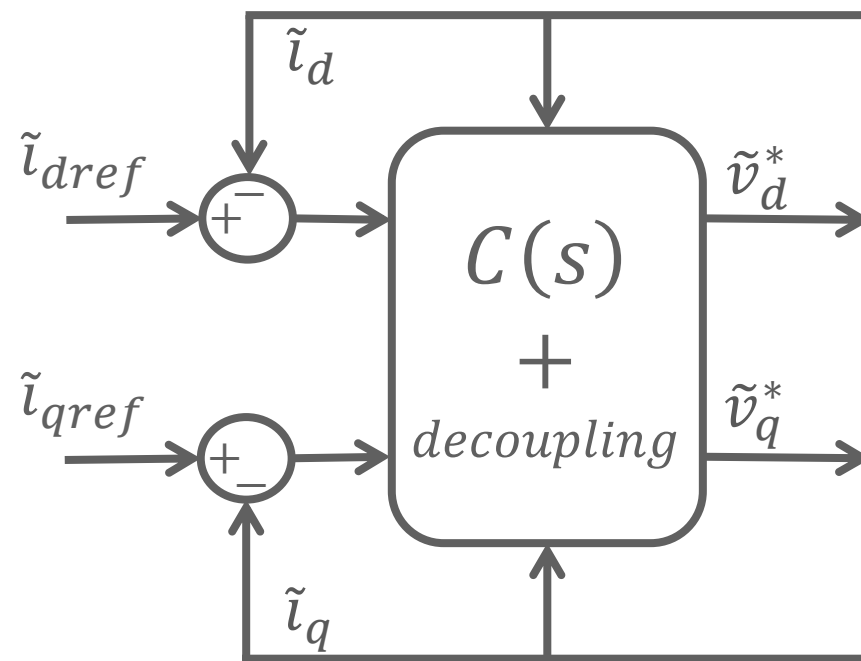
$$\begin{bmatrix} \tilde{v}_d^* \\ \tilde{v}_q^* \end{bmatrix} = C(s) \cdot \left\{ \begin{bmatrix} \tilde{i}_{dref} \\ \tilde{i}_{qref} \end{bmatrix} - \begin{bmatrix} \tilde{i}_d \\ \tilde{i}_q \end{bmatrix} \right\} + D \cdot \begin{bmatrix} \tilde{i}_d \\ \tilde{i}_q \end{bmatrix}$$

$$K_{pd} = \ell_d \cdot \omega_{BWd} \quad K_{pq} = \ell_q \cdot \omega_{BWq}$$

$$\tau_{id} = \ell_d / R_s \quad \tau_{iq} = \ell_q / R_s$$

with:

$$C(s) = \begin{bmatrix} K_{pd} \frac{1 + \tau_{id} \cdot s}{\tau_{id} \cdot s} & 0 \\ 0 & K_{pq} \frac{1 + \tau_{iq} \cdot s}{\tau_{iq} \cdot s} \end{bmatrix}, \quad D = \begin{bmatrix} 0 & -L_q \omega \\ L_d \omega & 0 \end{bmatrix}$$



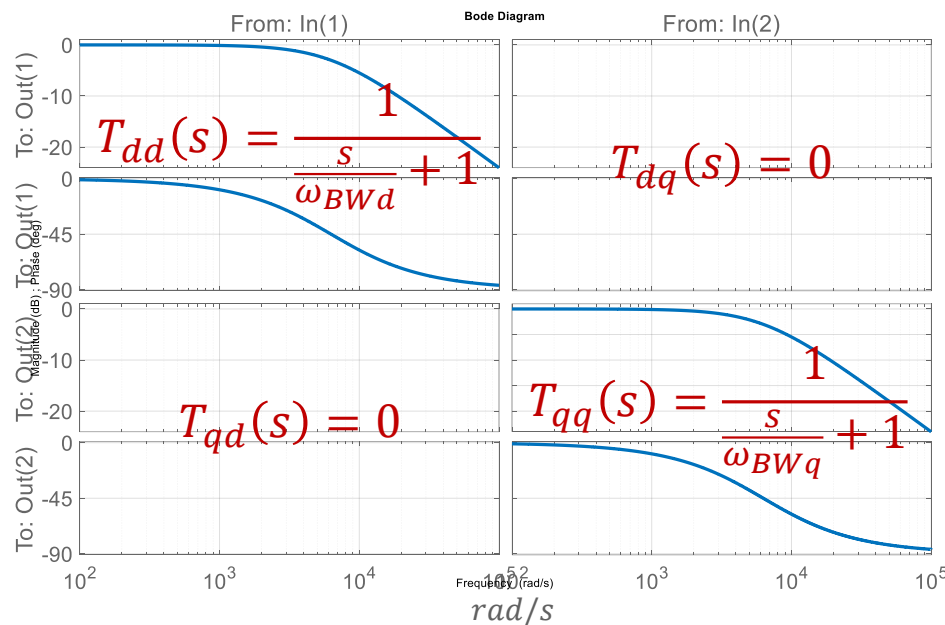


# PI Current Control + Decoupling: Analysis

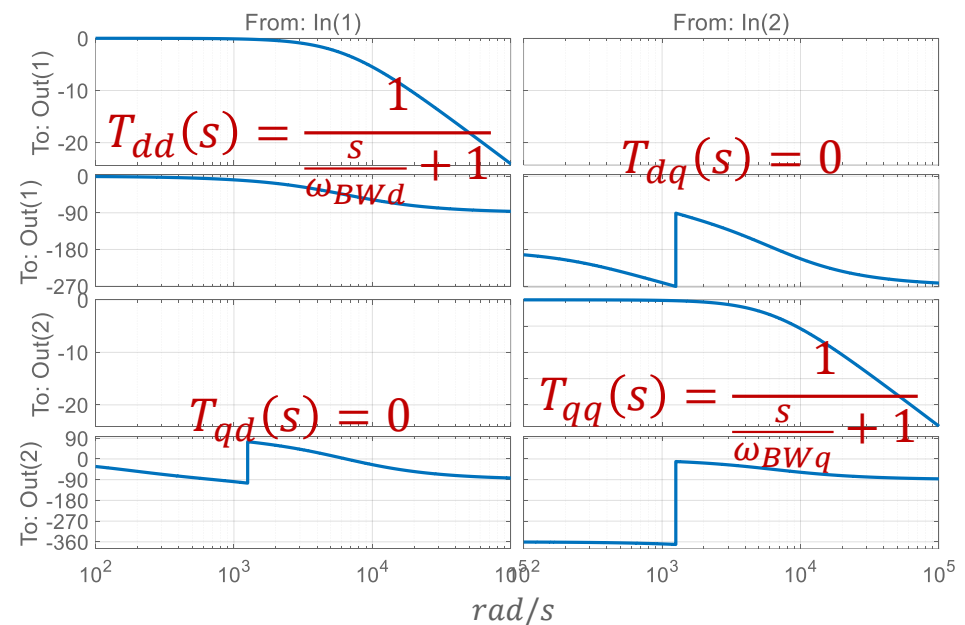
Closed-loop transfer function: **known parameters**

$$\begin{bmatrix} \tilde{i}_d \\ \tilde{i}_q \end{bmatrix} = \begin{bmatrix} T_{dd}(s) & 0 \\ 0 & T_{qq}(s) \end{bmatrix} \cdot \begin{bmatrix} \tilde{i}_{dref} \\ \tilde{i}_{qref} \end{bmatrix}$$

PI + feedback decoupling:



PI + feedforward decoupling:

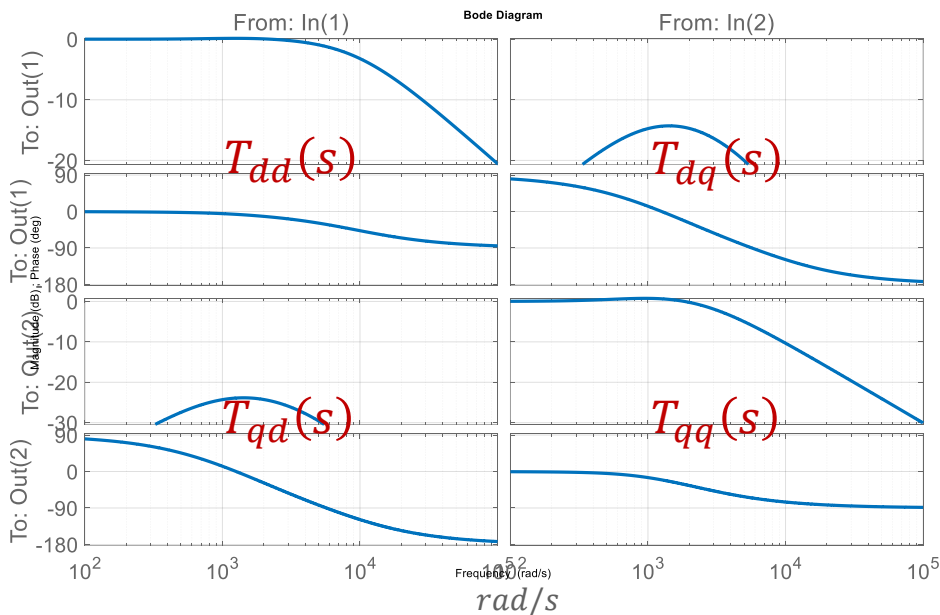


# PI Current Control + Decoupling: Analysis

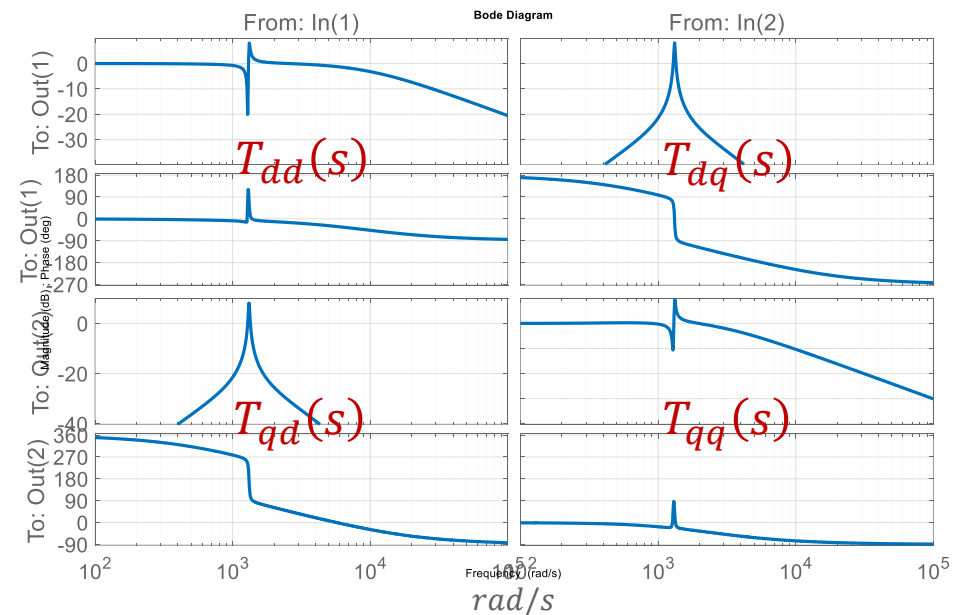
Closed-loop transfer function: **parameters uncertainty**

$$\begin{bmatrix} \tilde{i}_d \\ \tilde{i}_q \end{bmatrix} = \begin{bmatrix} T_{dd}(s) & T_{dq}(s) \\ T_{qd}(s) & T_{qq}(s) \end{bmatrix} \cdot \begin{bmatrix} \tilde{i}_{dref} \\ \tilde{i}_{qref} \end{bmatrix}$$

PI + feedback decoupling:



PI + feedforward decoupling:



# Complex Vector Current Control: Design

Current controller transfer function:

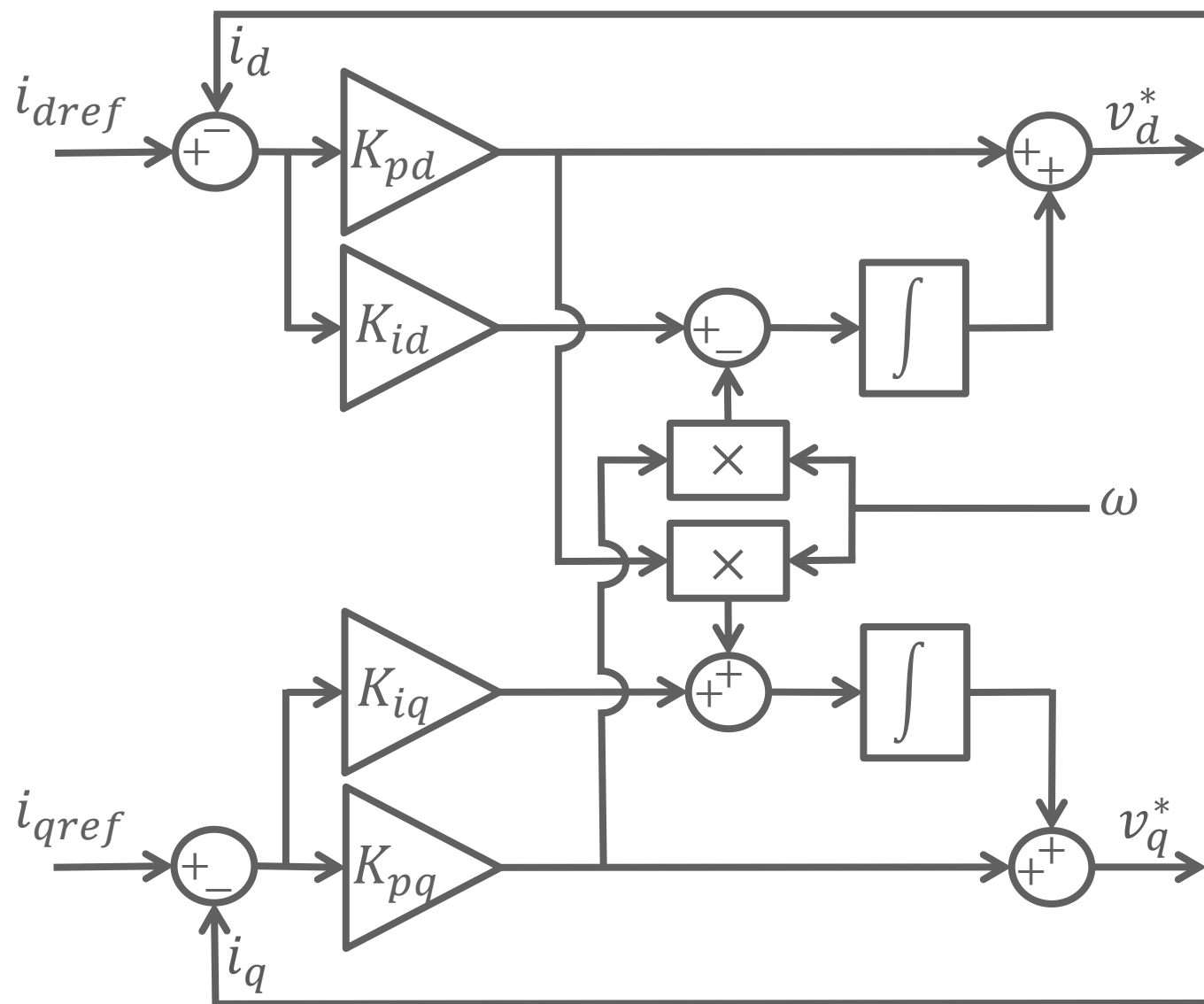
$$\begin{bmatrix} \tilde{v}_d^* \\ \tilde{v}_q^* \end{bmatrix} = C(s) \cdot \left\{ \begin{bmatrix} \tilde{i}_{dref} \\ \tilde{i}_{qref} \end{bmatrix} - \begin{bmatrix} \tilde{i}_d \\ \tilde{i}_q \end{bmatrix} \right\}$$

$$K_{pd} = \ell_d \cdot \omega_{BWd} \quad K_{pq} = \ell_q \cdot \omega_{BWq}$$

$$K_{id} = R_s \cdot \omega_{BWd} \quad K_{iq} = R_s \cdot \omega_{BWq}$$

Transfer function of complex vector current controller:

$$C(s) = \begin{bmatrix} K_{pd} \frac{1 + \tau_{id} \cdot s}{\tau_{id} \cdot s} & \frac{-K_{pq} \cdot \omega}{s} \\ \frac{K_{pd} \cdot \omega}{s} & K_{pq} \frac{1 + \tau_{iq} \cdot s}{\tau_{iq} \cdot s} \end{bmatrix}$$

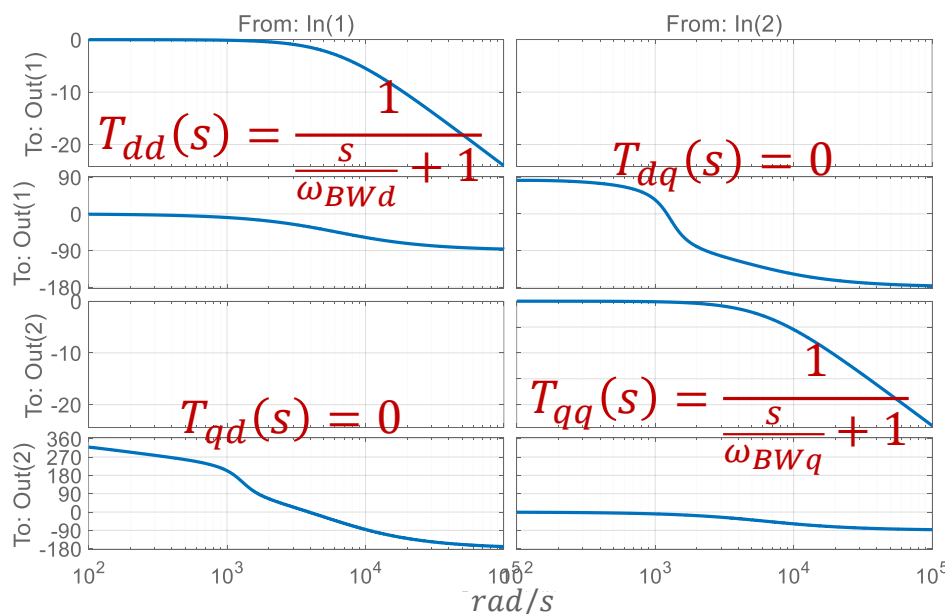


# Complex Vector Current Control: Design

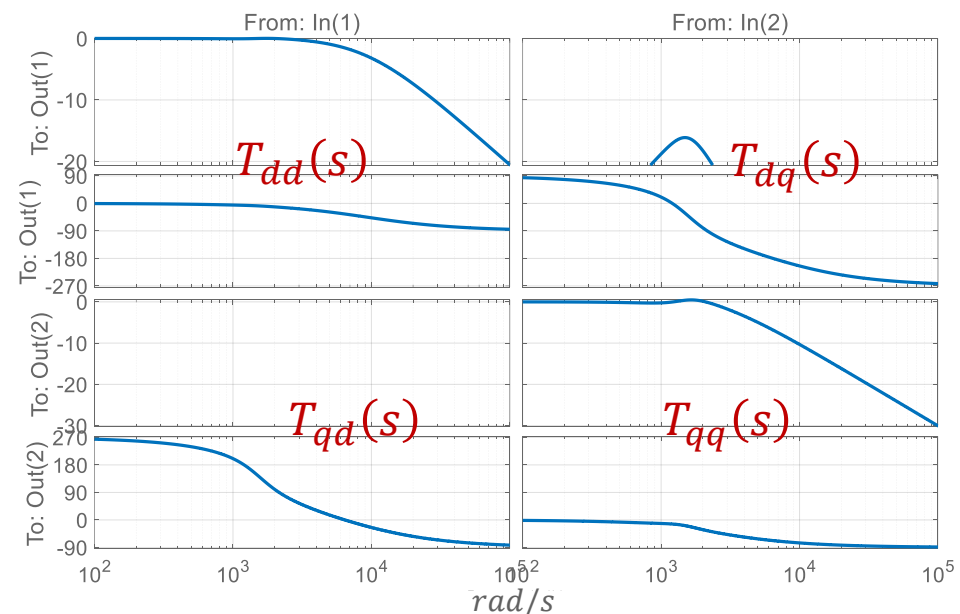
## Improved PI controller: inherent decoupling

$$\begin{bmatrix} \tilde{i}_d \\ \tilde{i}_q \end{bmatrix} = \begin{bmatrix} T_{dd}(s) & T_{dq}(s) \\ T_{qd}(s) & T_{qq}(s) \end{bmatrix} \cdot \begin{bmatrix} \tilde{i}_{dref} \\ \tilde{i}_{qref} \end{bmatrix}$$

### known parameters

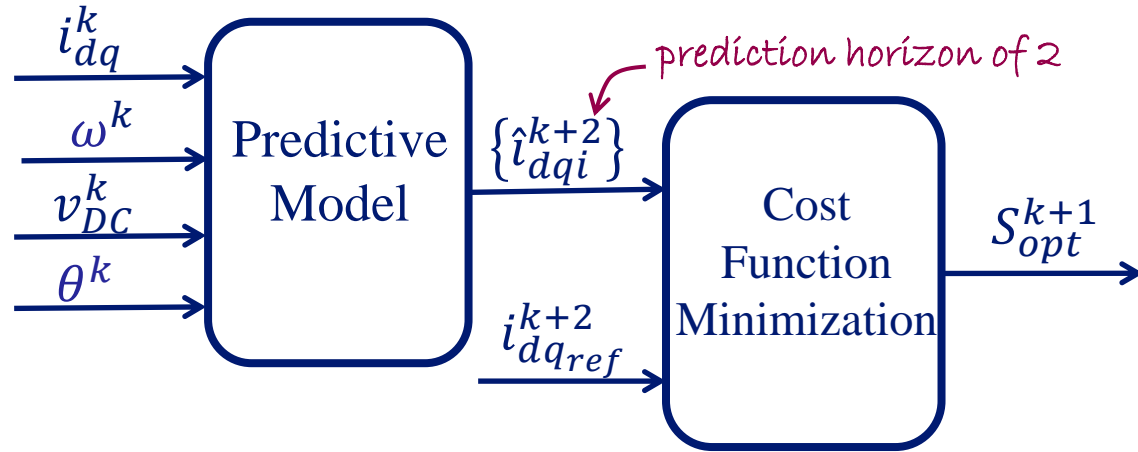


### parameters uncertainty

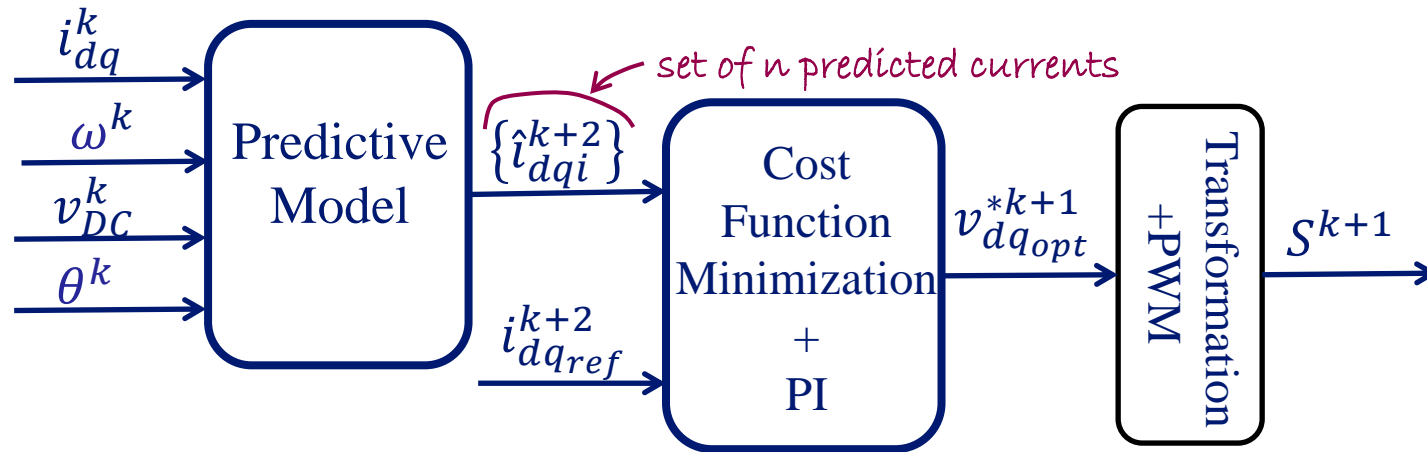


# Model-Predictive Current Control: Design

## Finite Control Set MPC (FCS-MPC):



## Continuous Control Set MPC (CCS-MPC):



## Predictive model using Euler discretization:

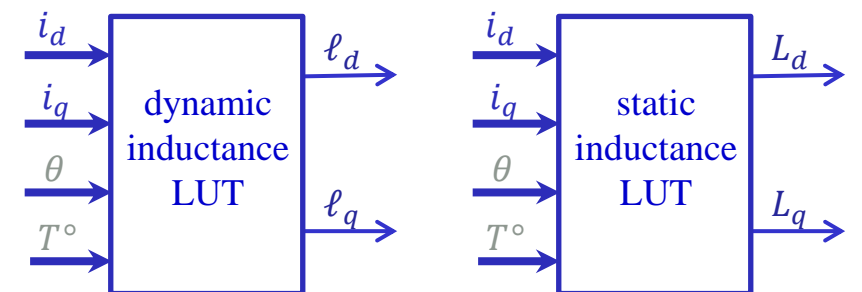
$i^{th}$  predicted currents:

$$i_{di}^{k+1} = i_d^k + \frac{T_s}{\ell_d^k} \left( v_{di}^{*k} - R_s i_d^k + \omega^k L_q^k i_q^k - \Delta V f_d(\theta^k) \right)$$

$$i_{qi}^{k+1} = i_q^k + \frac{T_s}{\ell_q^k} \left( v_{qi}^{*k} - R_s i_q^k - \omega^k (L_d^k i_d^k + \Psi_f) - \Delta V f_q(\theta^k) \right)$$

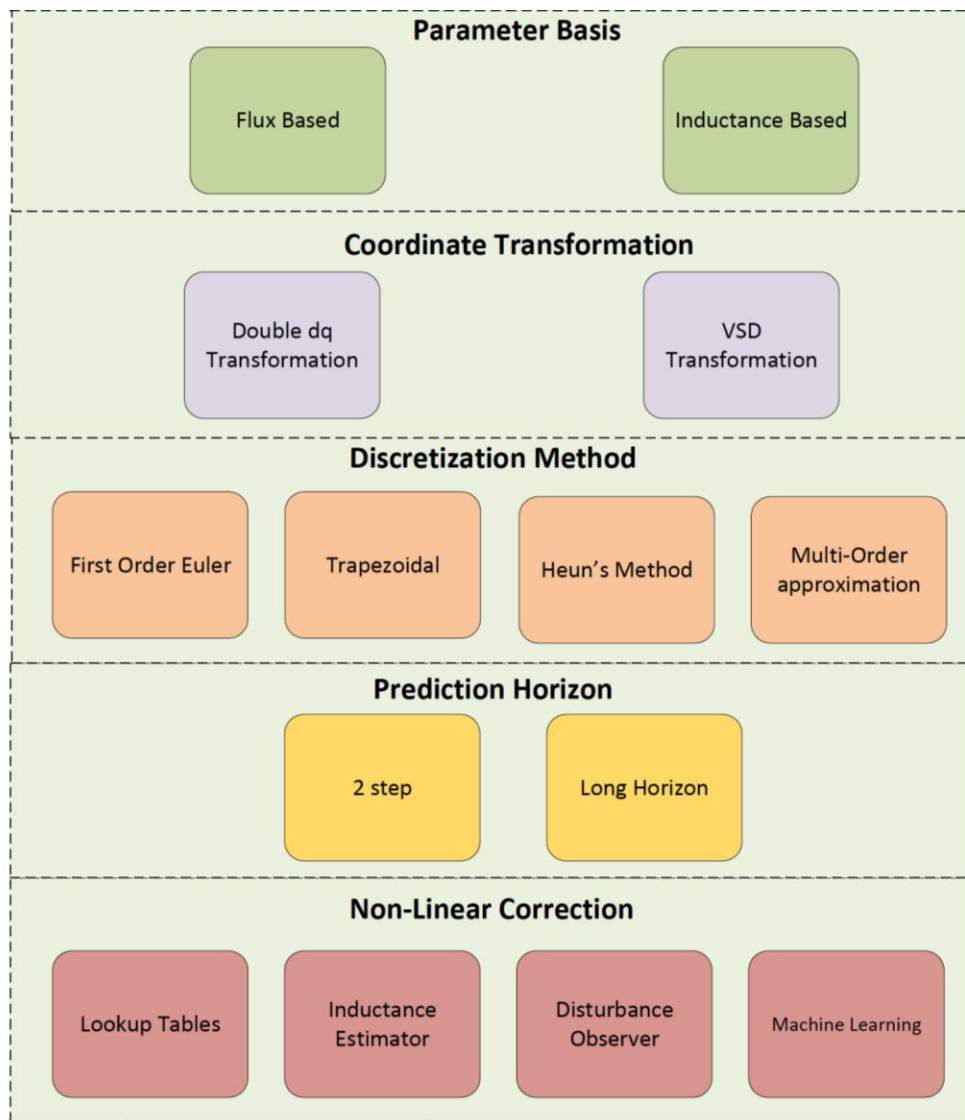
with:

$$\begin{bmatrix} v_{di}^* \\ v_{qi}^* \end{bmatrix} = \underbrace{P(-\theta)}_{\text{Park and Clarke transformation matrices}} \cdot C_{32}^{-1} \cdot \underbrace{\begin{bmatrix} S_{ai} \\ S_{bi} \\ S_{ci} \end{bmatrix}}_{i^{th} \text{ switching state}} \cdot v_{DC}$$



# Model-Predictive Current Control: Design

## Choices for predictive model:



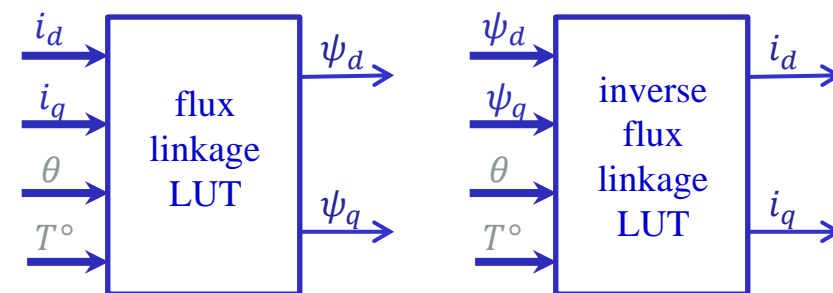
## Predictive model using Euler discretization:

$i^{th}$  predicted flux linkages:

$$\psi_{di}^{k+1} = \psi_d^k + T_s (v_{di}^{*k} - R_s i_d^k + \omega^k \psi_q^k - \Delta V f_d(\theta^k))$$

$$\psi_{qi}^{k+1} = \psi_q^k + T_s (v_{qi}^{*k} - R_s i_q^k - \omega^k \psi_d^k - \Delta V f_q(\theta^k))$$

with:



## Choices for cost function:

$$g_i = (i_{dref} - \hat{i}_d^{k+2})^2 + \lambda_q (i_{qref} - \hat{i}_q^{k+2})^2$$

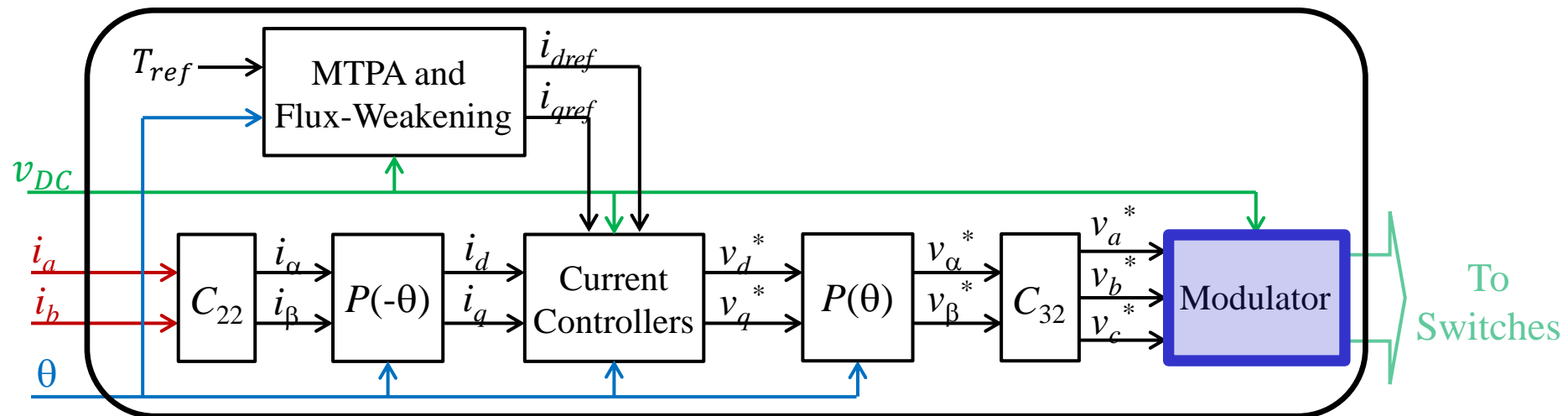
$$g_{is} = (i_{dref} - \hat{i}_d^{k+2})^2 + \lambda_q (i_{qref} - \hat{i}_q^{k+2})^2 + \lambda_s n_s$$

$$\text{with: } n_s = \sum_{i=1}^n |S_i^{k+1} - S_i^k|$$

# Electric Motor Torque Control for Electrified Transportation Systems

## Current Control: Control of $dq$ –currents for indirect torque control

- **Techniques:** many linear and nonlinear current controllers
- **Challenges:** accurate model, online parameter estimation, robustness, current sensorless control
- **Requirements:** phase current sensors and rotor angle sensor, DC-link voltage sensor (optional), current controllers, modulator (recommended)



## Pulse-Width Modulator



# Modulator: Pulse-Width Modulation (PWM)

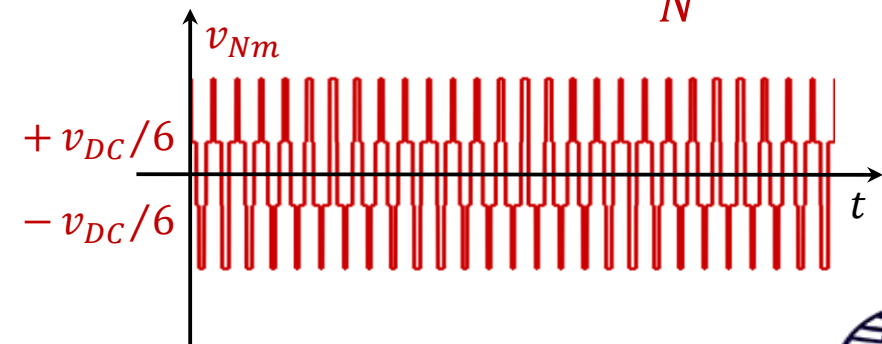
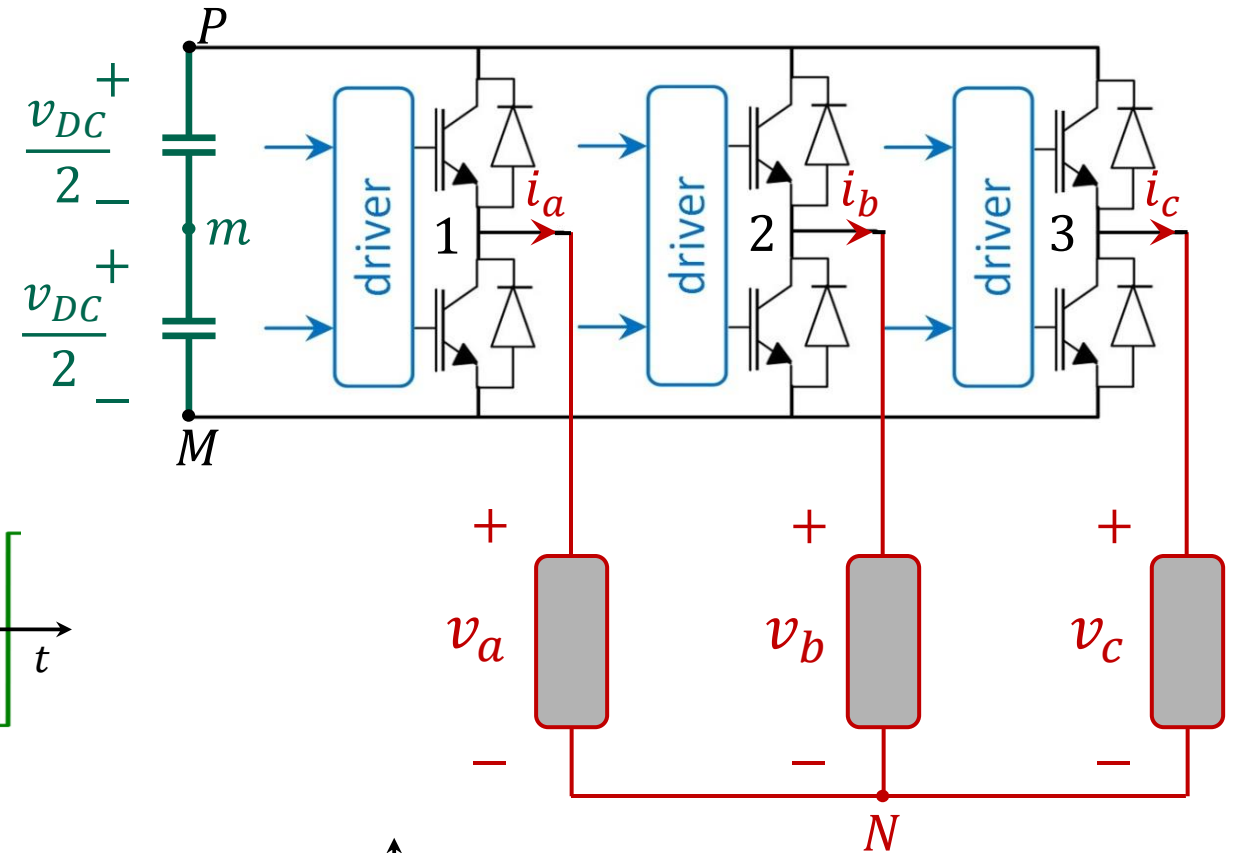
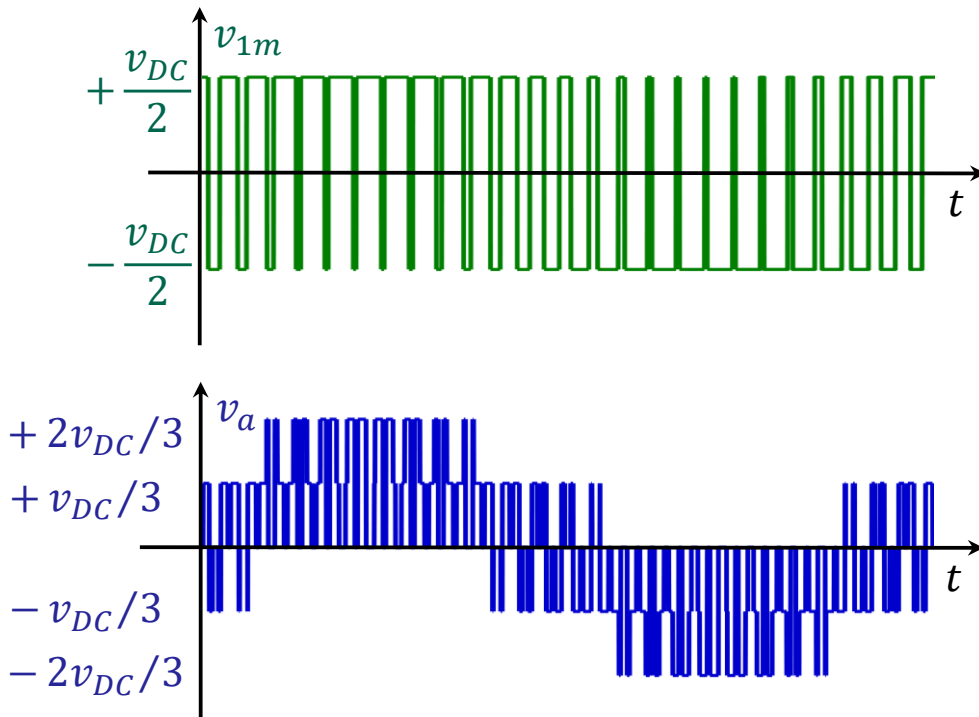
## Phase voltages:

$$v_a = v_{1m} - v_{Nm}$$

$$v_b = v_{2m} - v_{Nm}$$

$$v_c = v_{3m} - v_{Nm}$$

## Voltage waveforms:



# Sinusoidal PWM (SPWM): DC-Link Voltage Utilization

Linear modulation:

$$\text{Fundamental of } v_{abc} = G_{VSI} \cdot v_{abc}^*$$

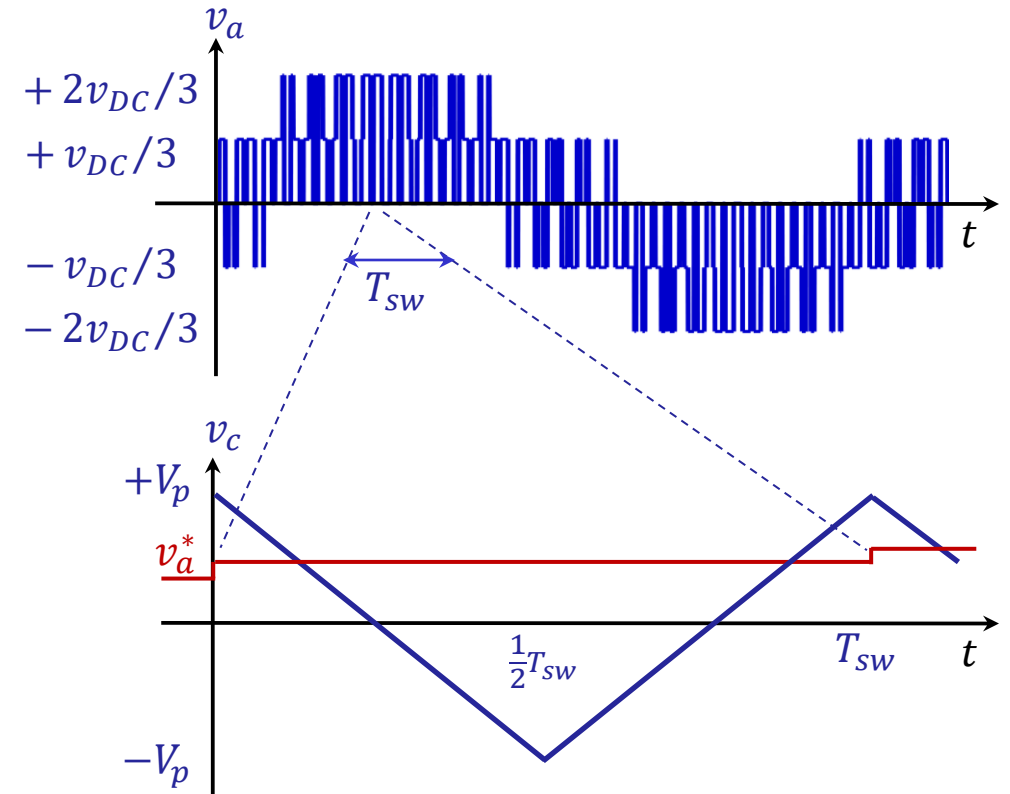
⇒ VSI being modeled as a gain

Condition for linear modulation:

$$|v_a^*| \leq V_p = \frac{v_{DC}}{2}$$

Therefore:

$$\|v_{abc}^*\| = \sqrt{v_a^{*2} + v_b^{*2} + v_c^{*2}} = \sqrt{\frac{3}{2}} V_m^* < \sqrt{\frac{3}{2}} \frac{v_{DC}}{2} \cong 0.612 v_{DC}$$



# SVM vs SPWM: DC-Link Voltage Utilization

Maximum voltage vector magnitude:

## Space-Vector Modulation (SVM) vs SPWM

Comparison in  $abc$  frame:

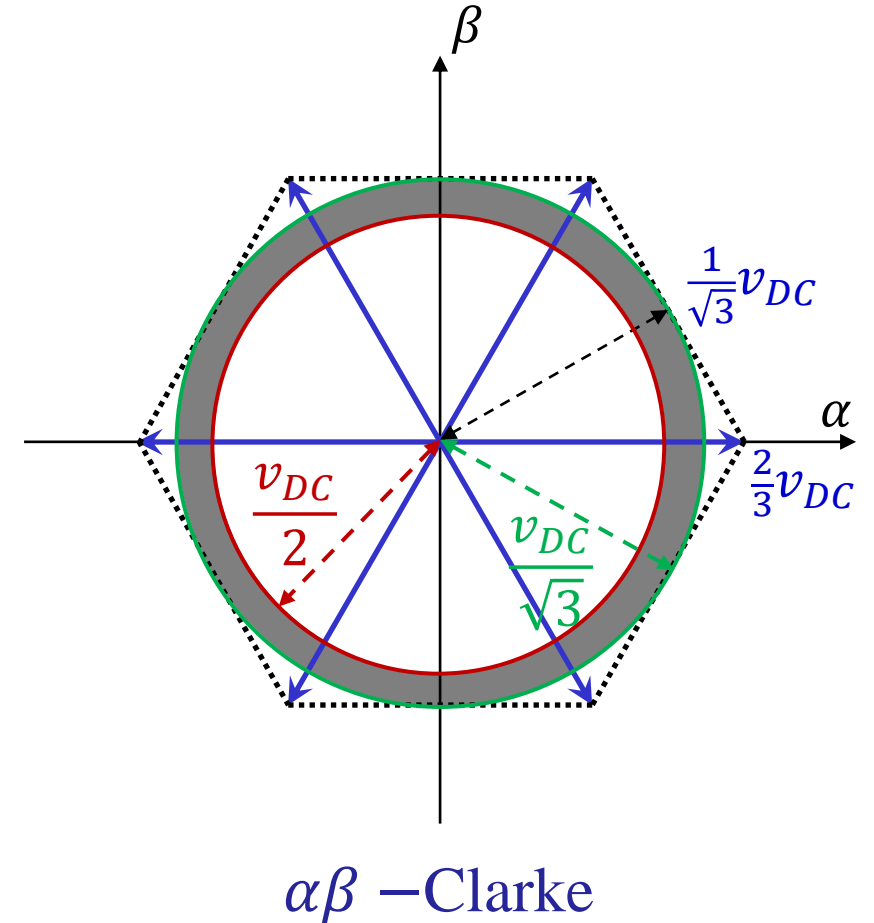
$$\|v_{abc}\|_{SPWM} \leq \sqrt{\frac{3}{2}} \frac{v_{DC}}{2}$$
$$\|v_{abc}\|_{SVM} \leq \frac{v_{DC}}{\sqrt{2}}$$

+15%

Comparison in  $\alpha\beta$  frame:  
(Clarke transformation)

$$\|v_{\alpha\beta}\|_{SPWM} \leq \frac{v_{DC}}{2}$$
$$\|v_{\alpha\beta}\|_{SVM} \leq \frac{v_{DC}}{\sqrt{3}}$$

+15%



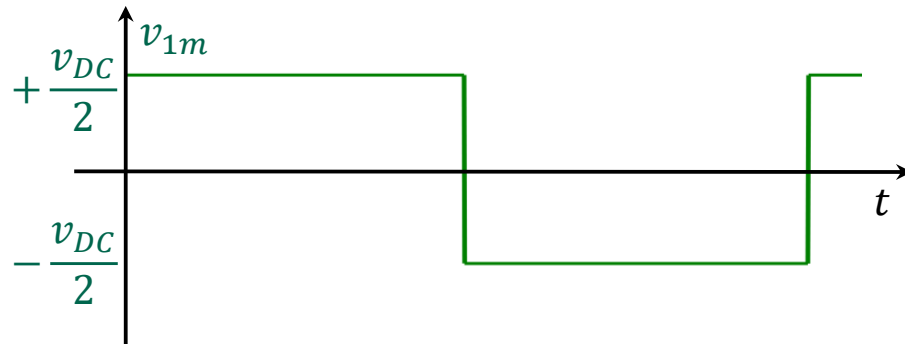
# Six-Step Operation (SSO): DC-Link Voltage Utilization

Maximum DC-link voltage utilization:

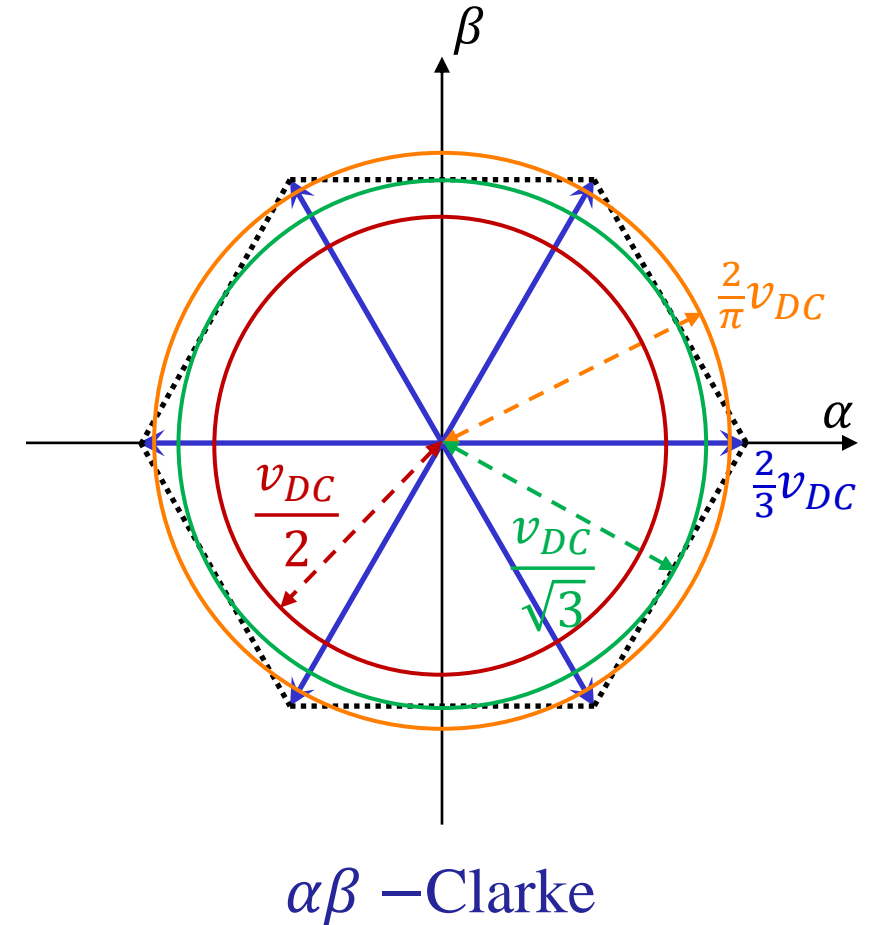
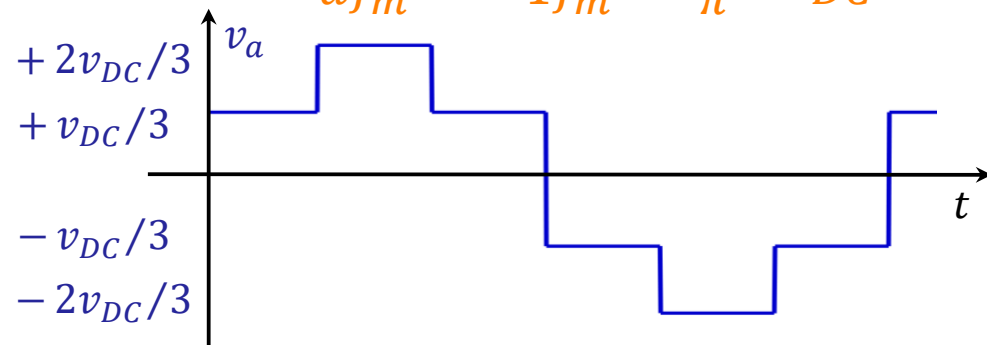
Six-step operation (SSO):

Amplitude of fundamental voltage:

$$V_{1f_m} = \frac{4}{\pi} \cdot \frac{v_{DC}}{2} = \frac{2}{\pi} \cdot v_{DC}$$



$$V_{af_m} = V_{1f_m} = \frac{2}{\pi} \cdot v_{DC}$$



# Amplitude Modulation Index (MI)

Maximum DC-link voltage utilization:

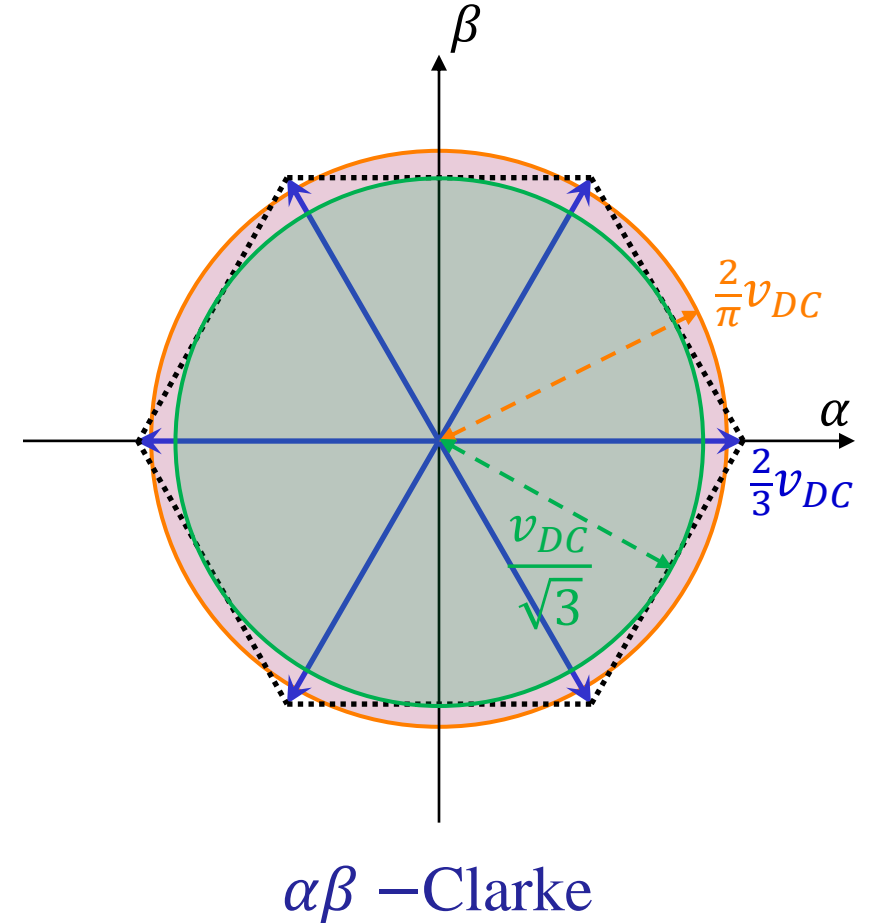
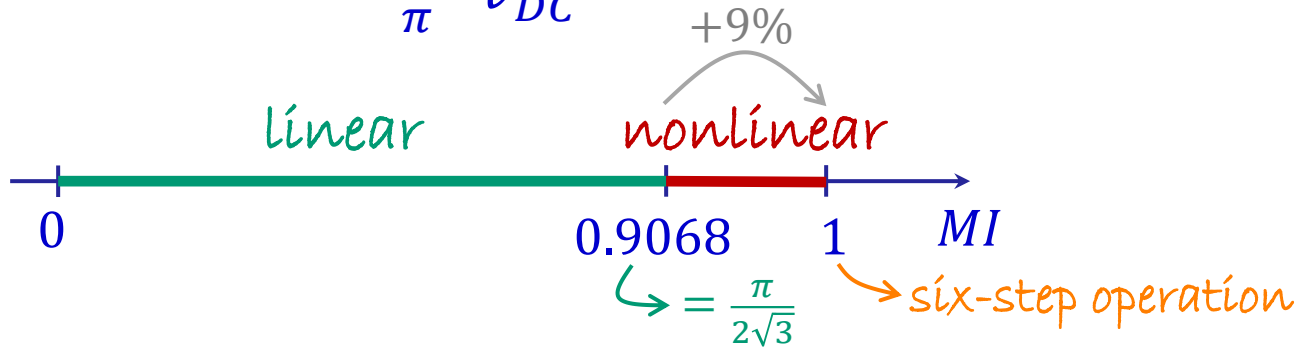
Nonlinear modulation region:

$\alpha\beta$  –Clarke:

$$\frac{1}{\sqrt{3}} \cdot v_{DC} < \|v_{\alpha\beta}\| < \frac{2}{\pi} \cdot v_{DC}$$

Modulation Index:

$$MI \triangleq \frac{\|v_{\alpha\beta}\|}{\frac{2}{\pi} \cdot v_{DC}}$$



# Nonlinear Modulation: Overmodulation (OVM)

- $MI^*$ : Modulation Index Reference

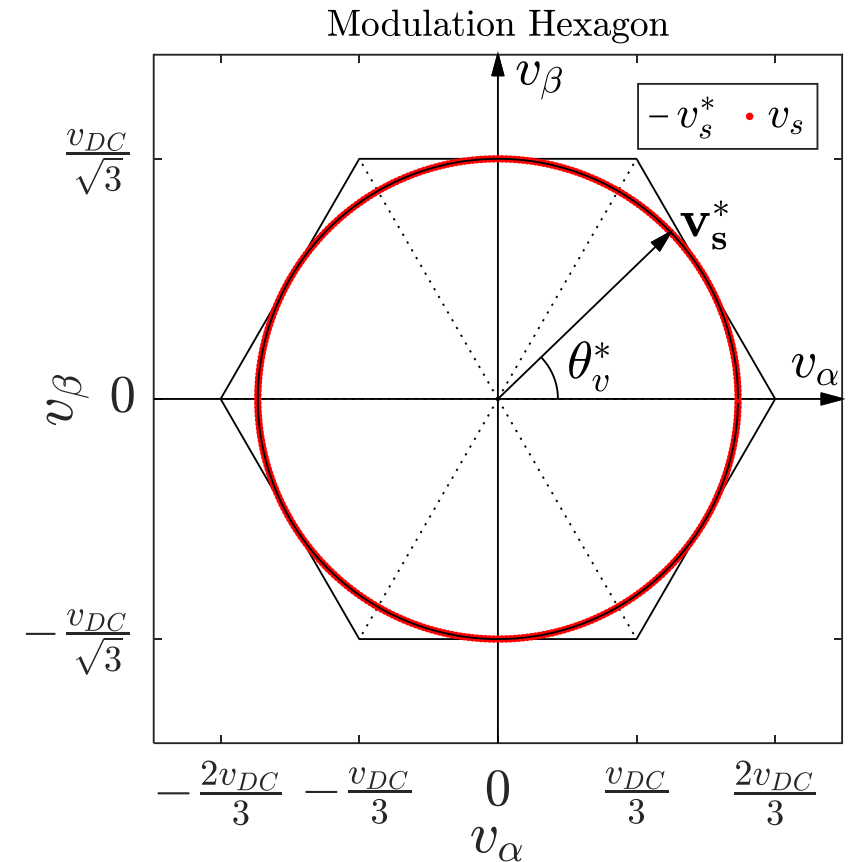
$$MI^* \triangleq \frac{\|v_{\alpha\beta}^*\|}{\frac{2}{\pi} \cdot v_{DC}}$$

- $MI$ : Actual Modulation Index

$$MI \triangleq \frac{\|v_{\alpha\beta}\|}{\frac{2}{\pi} \cdot v_{DC}}$$

MI range:

- Linear modulation:  $MI \in [0 \quad 0.9068]$
- Overmodulation:  $MI \in (0.9068 \quad 1)$
- Six-step operation:  $MI = 1$



	Magnitude	Angle
Input	$v_s^*$	$\theta_v^*$
Output	$v_s$	$\theta_v$

# Nonlinear Modulation: Overmodulation (OVM)

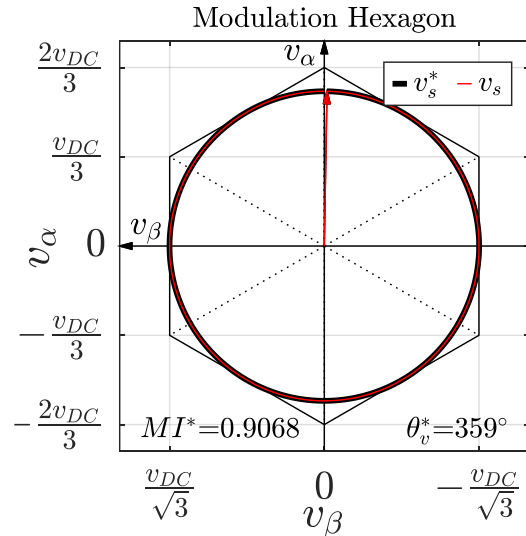
Linear modulation:

$$MI = MI^*$$

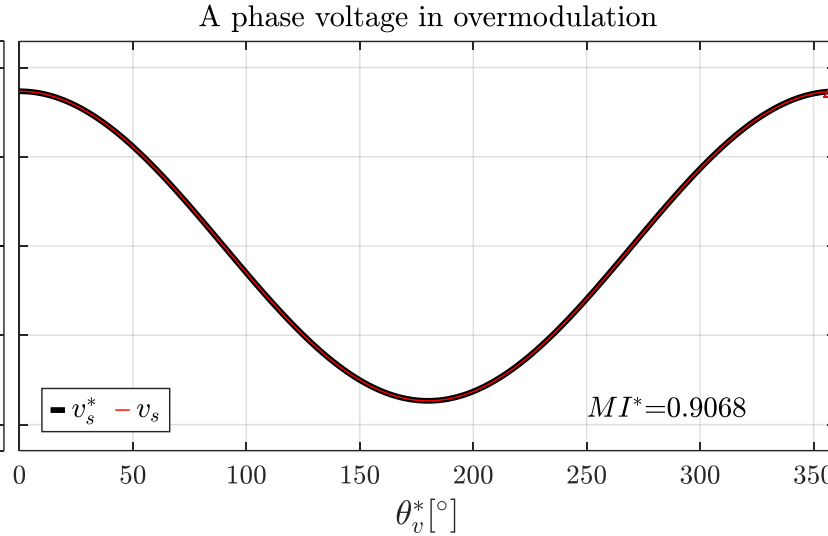
Recall:

$$0 \leq MI \leq 0.9068$$

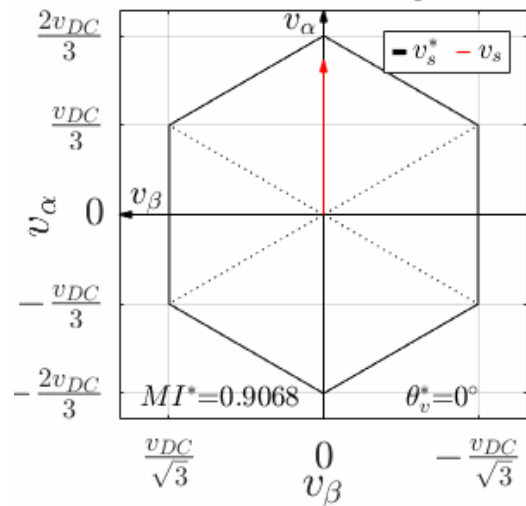
Modulation hexagon



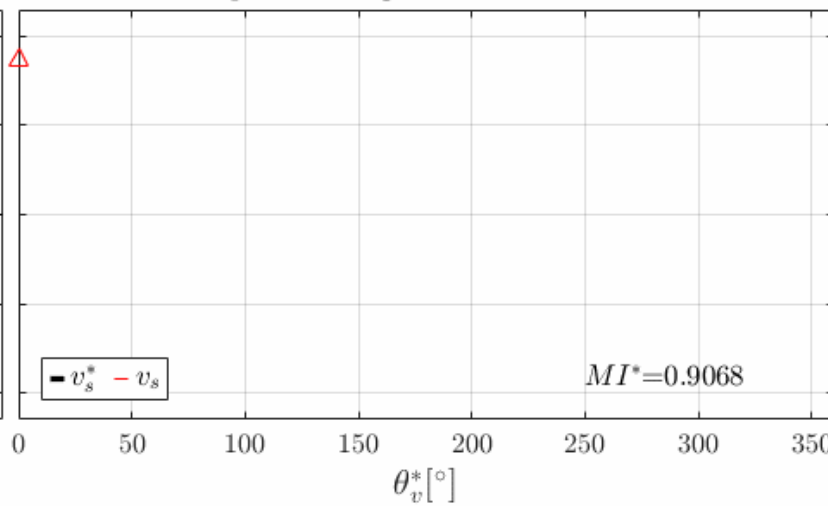
Fundamental phase voltage



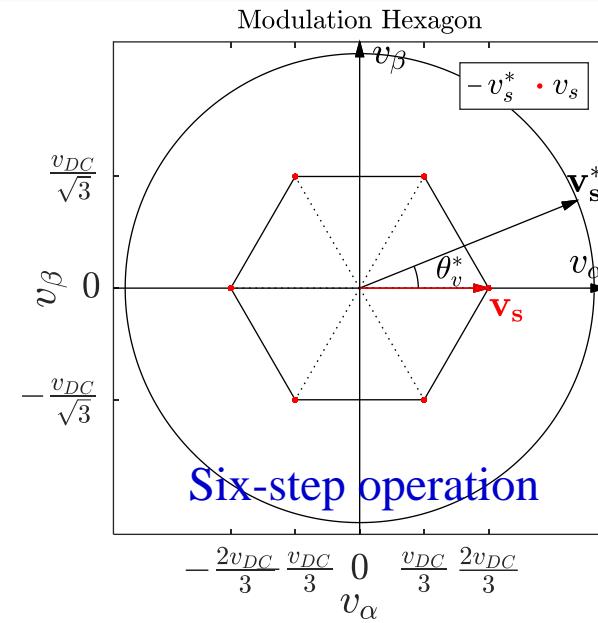
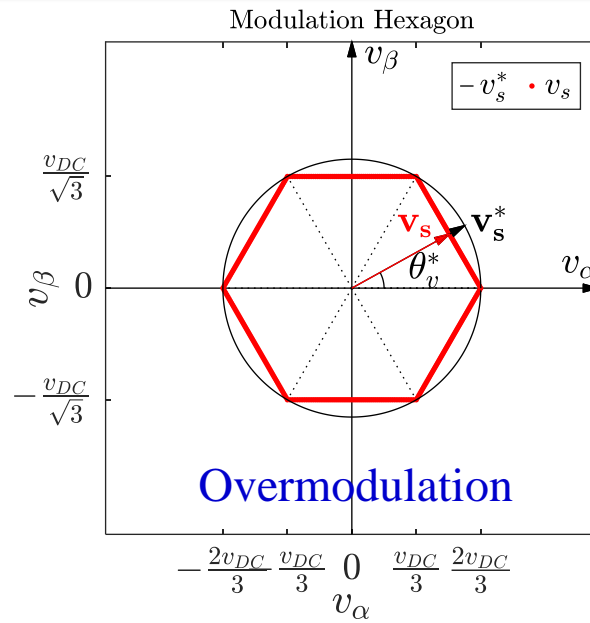
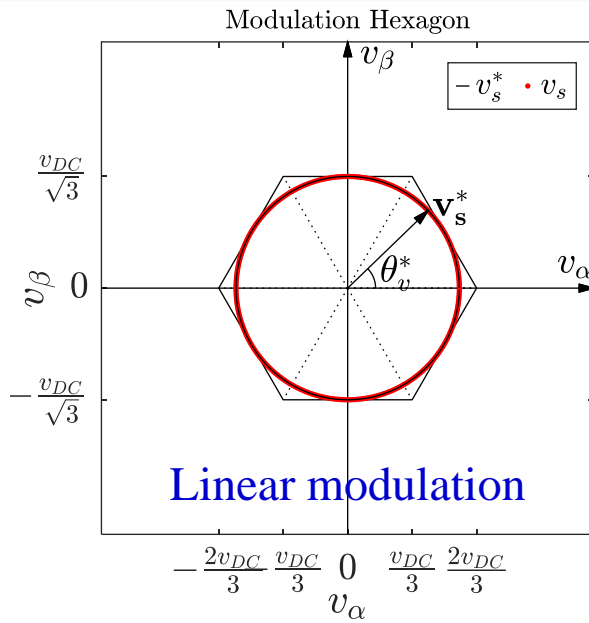
Modulation Hexagon



A phase voltage in overmodulation



# From Linear Modulation to Overmodulation and Six-Step Operation

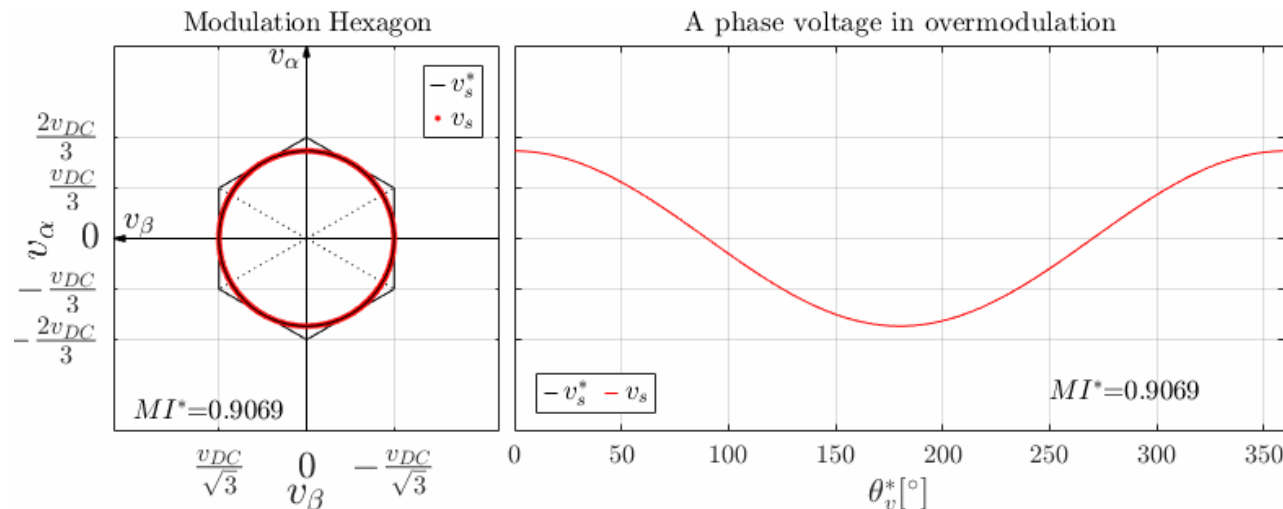


Overmodulation:

$$MI \neq MI^*$$

Recall:

$$0.9068 < MI < 1$$

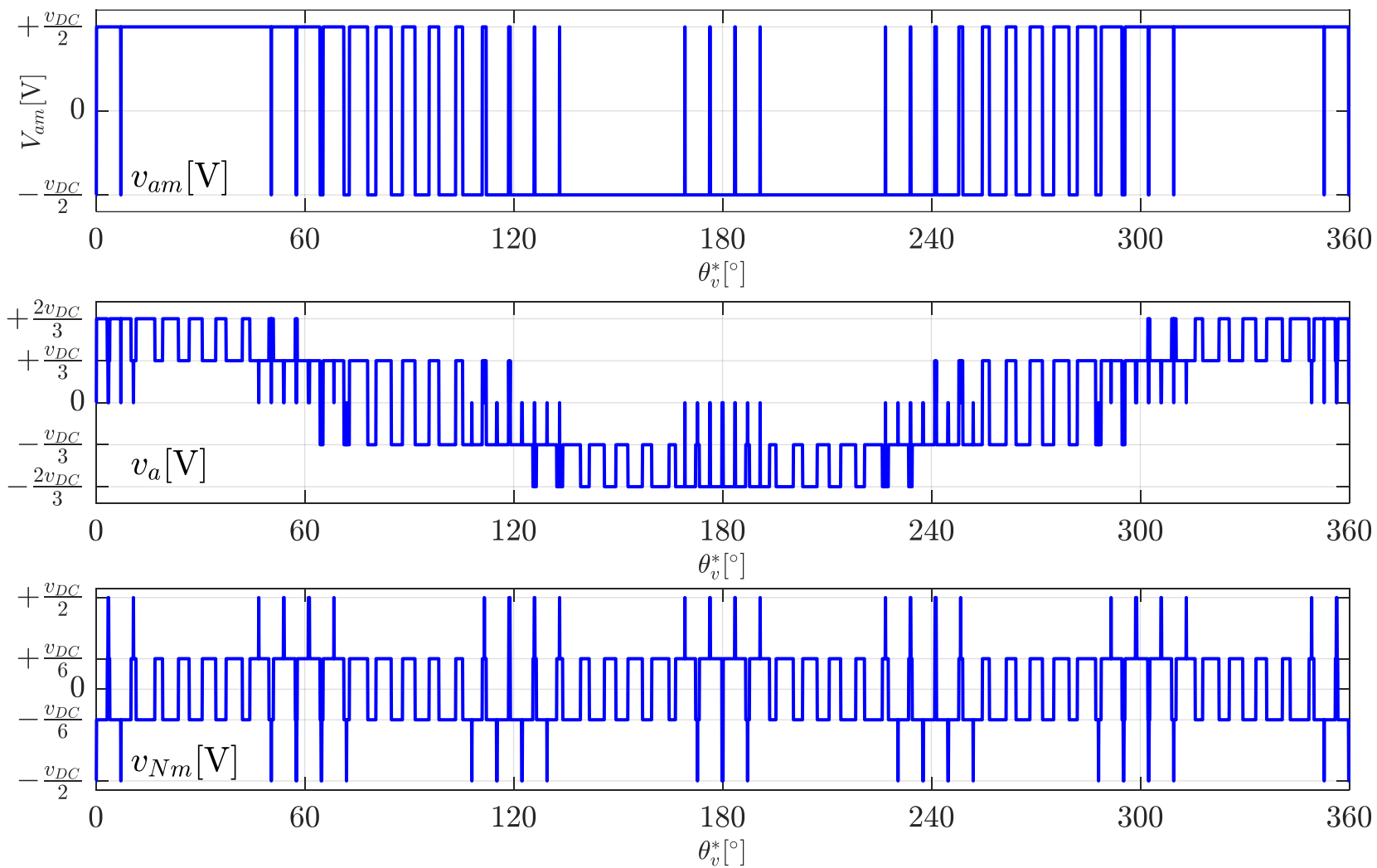


Linear modulation  $\gg$  Overmodulation  $\gg$  Six-step operation



# Overmodulation (OVM): Waveforms

Overmodulation:  $MI^* = 0.94$ ,  $M_f = f_{sw}/f_1 = 50$



# Overmodulation (OVM) Techniques

## 1. Minimum Phase Error (MPE)

-  $\theta_v^* = \theta_v$ : Phase error is **ZERO**

## 2. Minimum Distance Error (MDE)

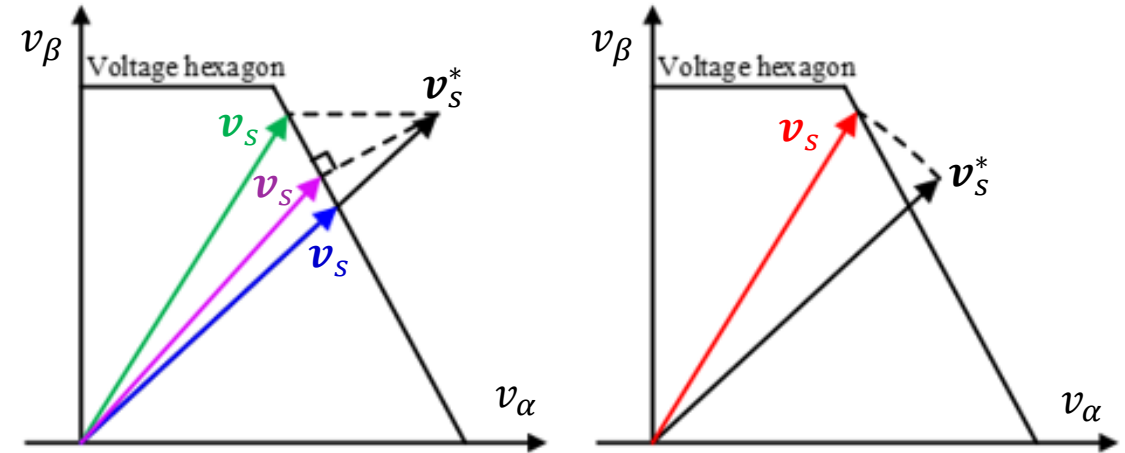
-  $\min(|v_s^* - v_s|)$ : Vector error is minimized

## 3. Keeping Switching State (SS)

- Hold on  $v_\alpha^*$  or  $v_\beta^*$

## 4. Minimum Magnitude Error (MME)

-  $v_s^* = v_s$ : Magnitude error is **ZERO**



	Input	Output
Magnitude	$v_s^*$	$v_s$
Angle	$\theta_v^*$	$\theta_v$

# Overmodulation (OVM) Techniques

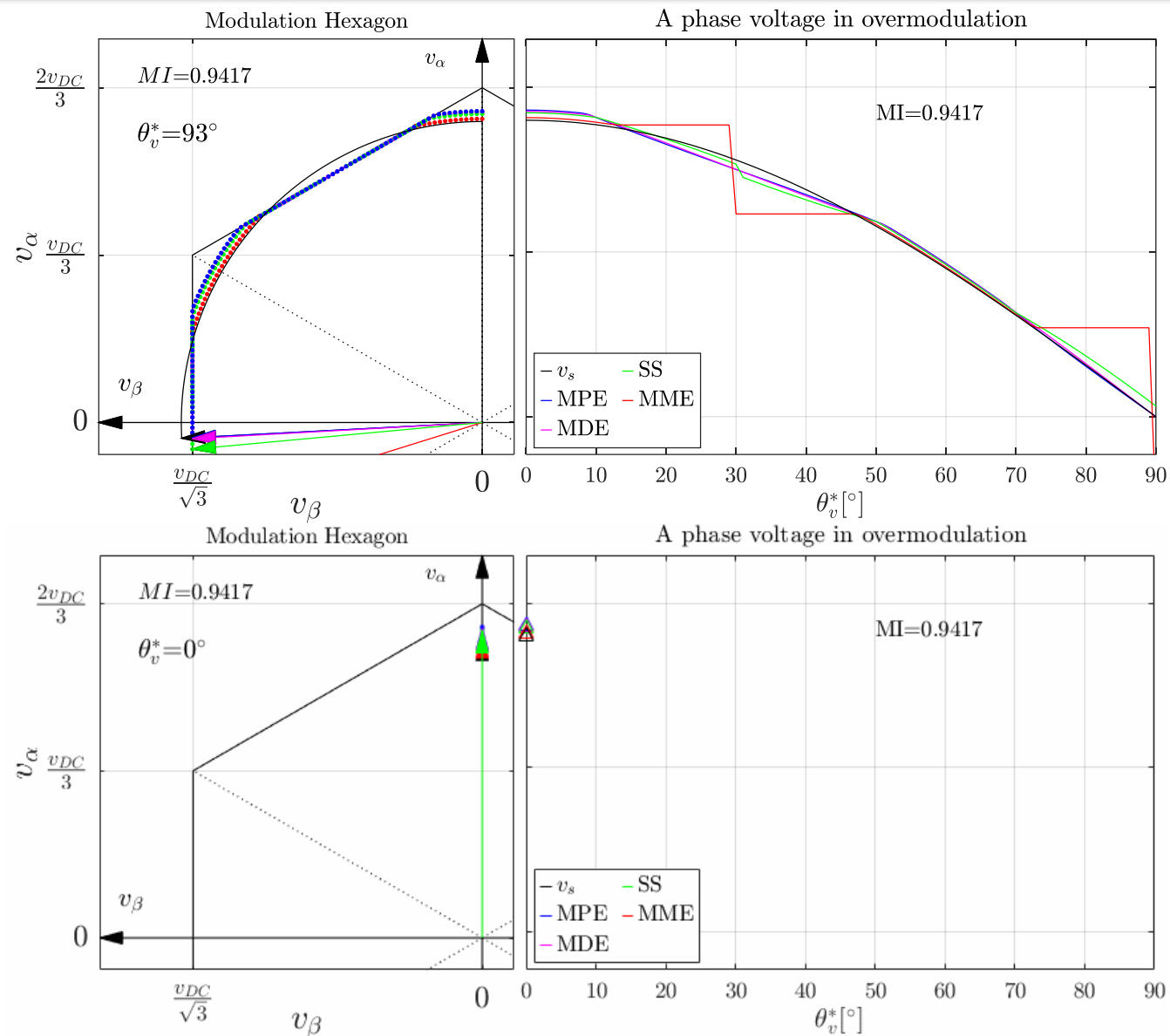
Comparison:

Minimum Phase Error (MPE)

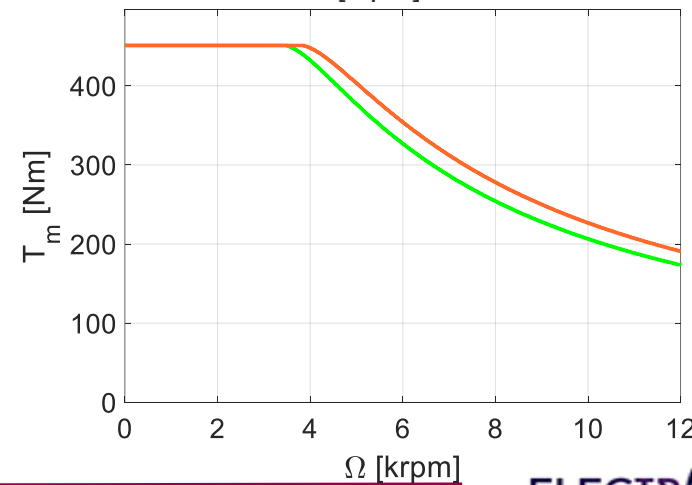
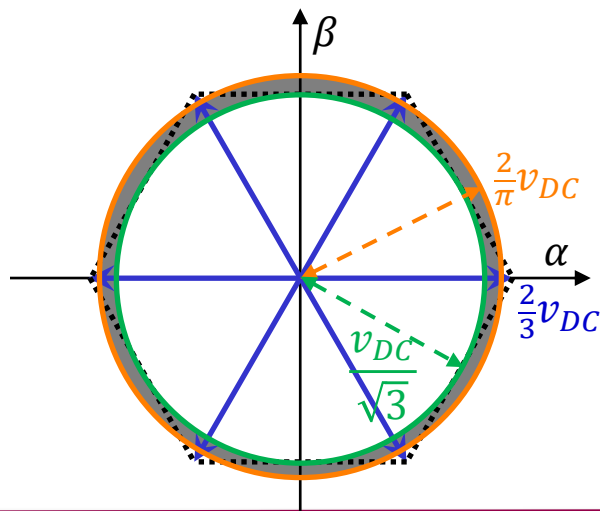
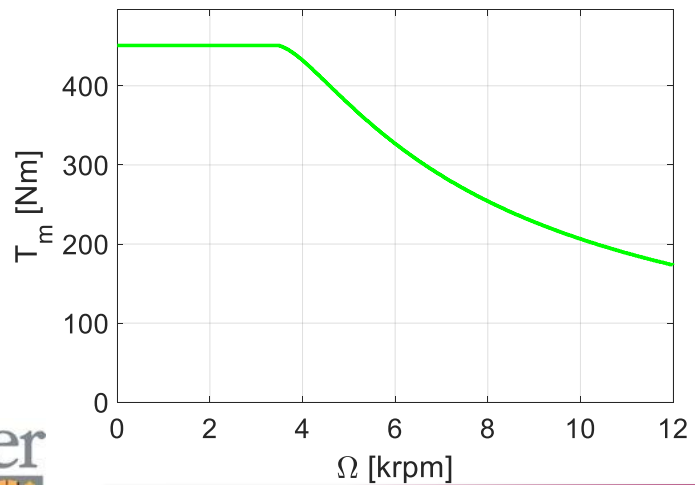
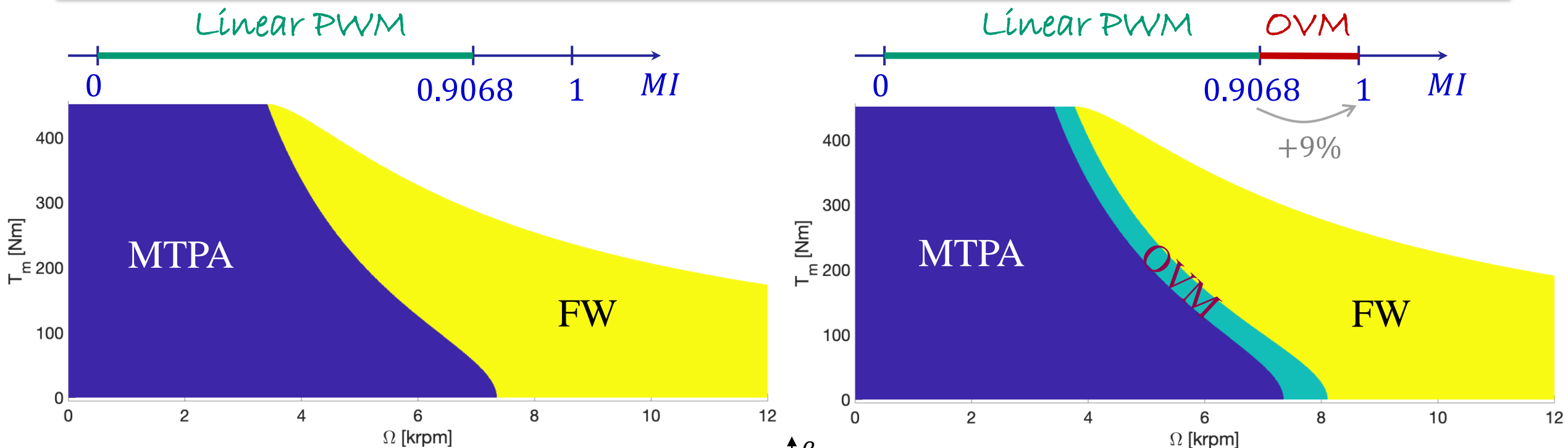
Minimum Distance Error (MDE)

Keeping Switching State (SS)

Minimum Magnitude Error (MME)



# Maximization of DC-link Voltage Utilization



# Overmodulation: Challenges

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- Harmonics of control (reference) voltages
- Nonlinear modulation index
- Effect on THD<sub>v</sub> (and so THD<sub>i</sub>)
- Performance degradation at low frequency modulation index

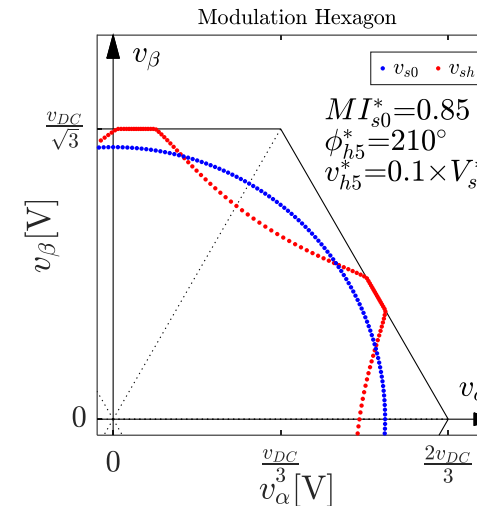
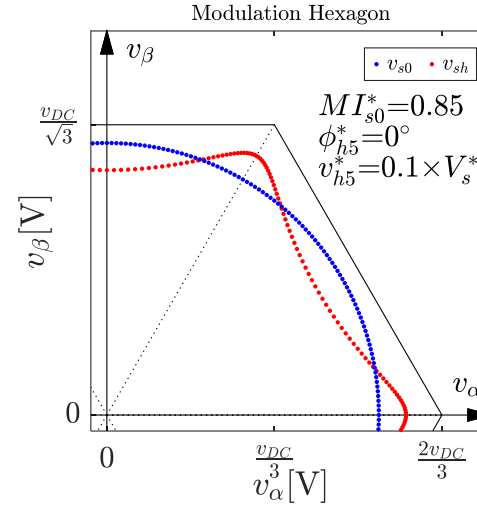
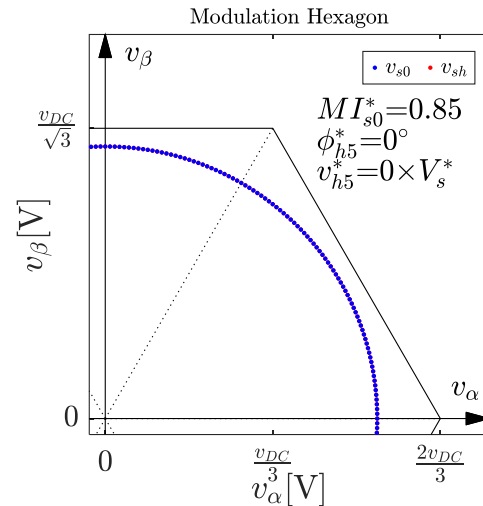
$$M_f = \frac{f_{sw}}{f_1}$$

- Transition from OVM to SSO

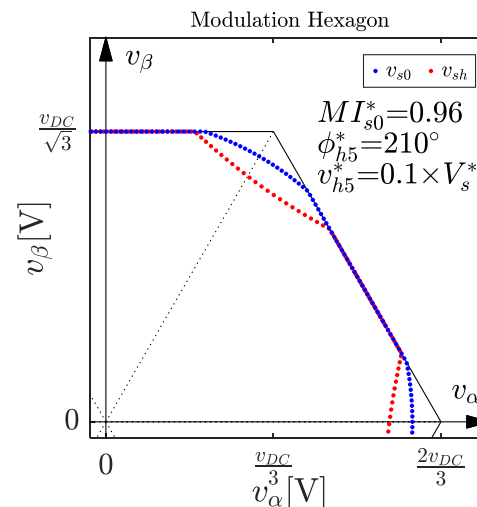
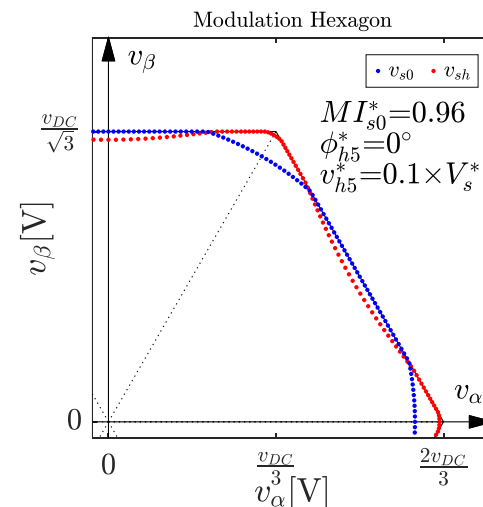
# Overmodulation Challenges: Harmonics of Control Voltages

Example: effect of 5<sup>th</sup>-harmonic:  $v_a^* = V_s^* \cos \theta_v^* + V_{h5}^* \cos(5\theta_v^* + \phi_{h5}^*)$

Linear modulation:



Overmodulation:

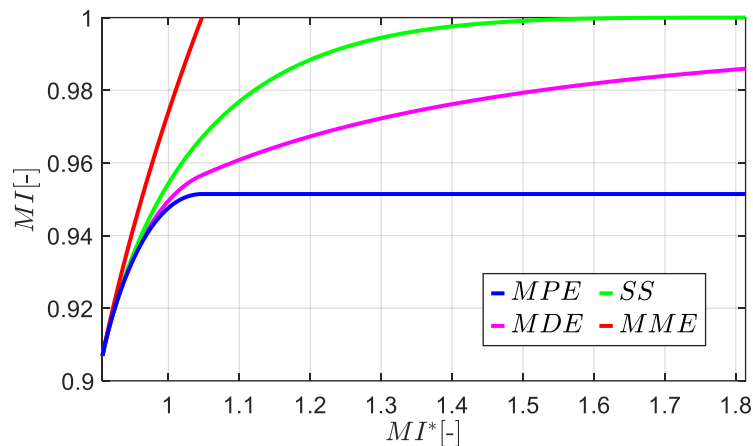


Observation:

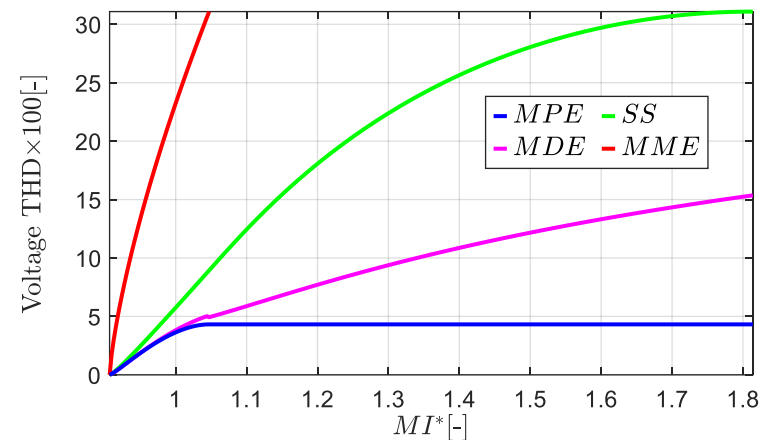
1.  $V_h^*$  : THD<sub>v</sub> ↑
2.  $\phi_h^*$  : MI ? (=, ↑, ↓)

# Overmodulation Challenges: Nonlinear Modulation Index

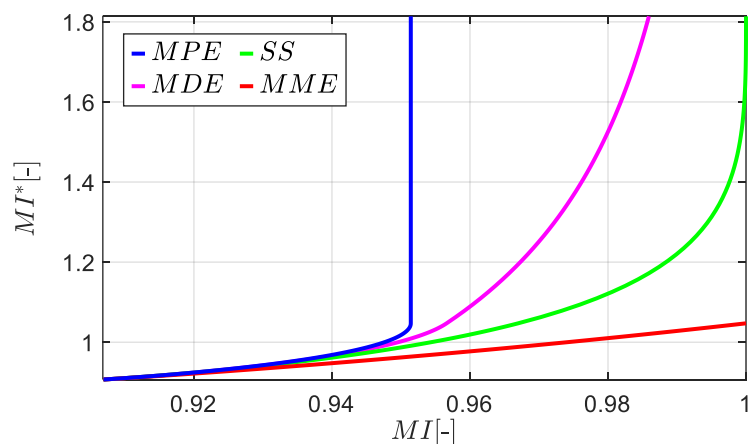
Nonlinearity due to OVM:  $\langle v_{abc} \rangle \neq G_{VSI} \cdot v_{abc}^*$



Effect of OVM on THD<sub>v</sub>:



Modulation Index Linearization (MIL):



Problem:  $MI^* \rightarrow OVM \rightarrow MI$ , then  $MI^* \neq MI$

MI linearization:  $MI^* \rightarrow MI^{**} \rightarrow OVM \rightarrow MI$

Objective:  $MI^* = MI$

Method:  $MI^{**} = f_{OVM}(MI)$

1. Polynomial function
2. LUT

# Electric Motor Torque Control for Electrified Transportation Systems

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**Modulator:** Generate command signals from continuous control voltages

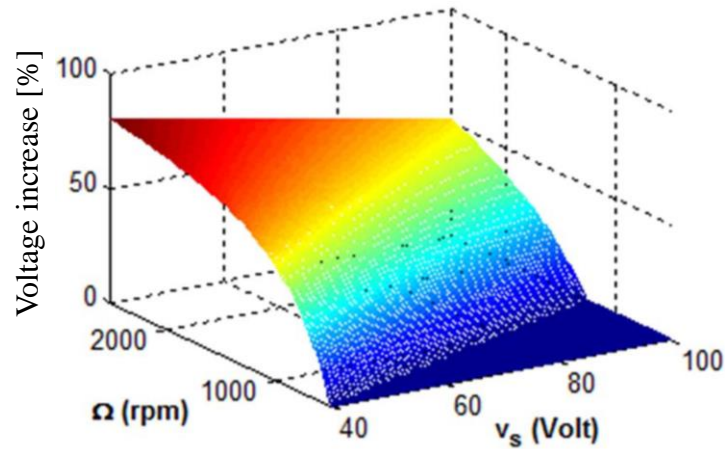
- **Advantage of linear PWM:** constant switching frequency
- **Advantage of overmodulation:** maximization of DC-link voltage utilization  
⇒ extension of speed range
- **Challenges:** harmonics of control voltages, THD<sub>v</sub> and THD<sub>i</sub>, smooth transition to six-step operation, instabilities/disturbances at low frequency modulation index
- **Other techniques:** Selected Harmonic Elimination (SHE), Selected Harmonic Mitigation (SHM), Hybrid PWM, Optimal Pulse Patterns
- **Other solutions to extend speed range:** variable DC-link voltage, Current-Source Inverter (CSI), sinus-inverter



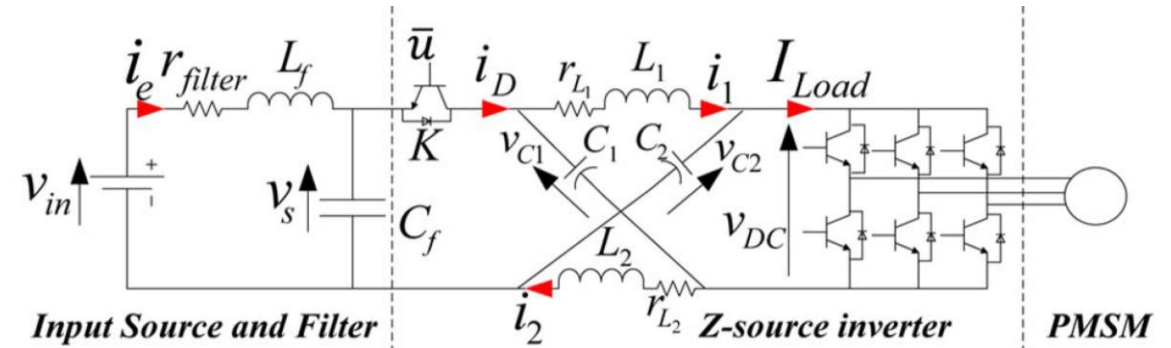
## Motor Drives

# Motor Drives for Speed Range Extension

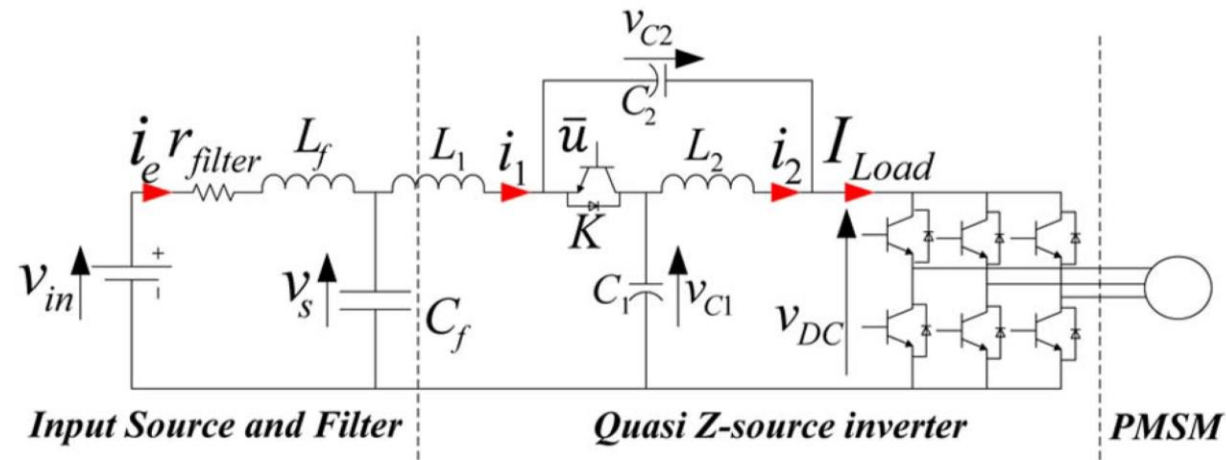
DC-link voltage adaptation for speed range extension:



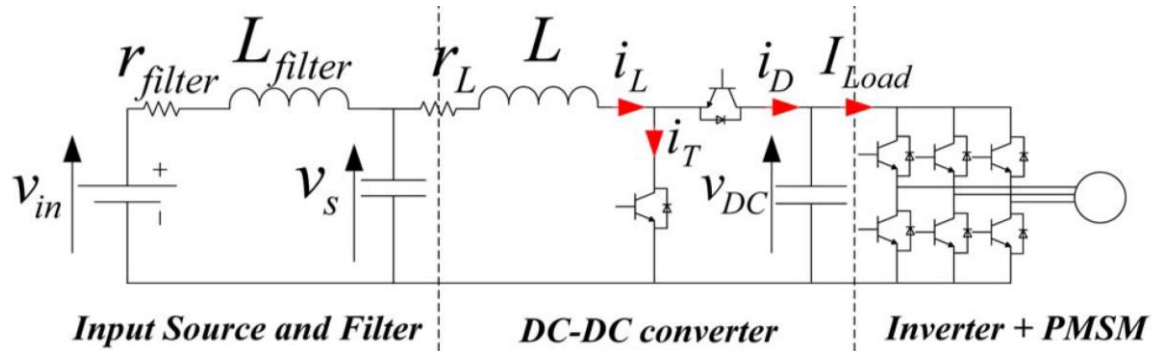
Z-source inverter



Quasi Z-source inverter



Boost + VSI



A. Battiston *et al.*, "A Control Strategy for Electric Traction Systems Using a PM-Motor Fed by a Bidirectional Z-Source Inverter," *IEEE Trans. on Vehicular Technology*, Vol. 63, No. 9, pp. 4178-4191, Nov. 2014.

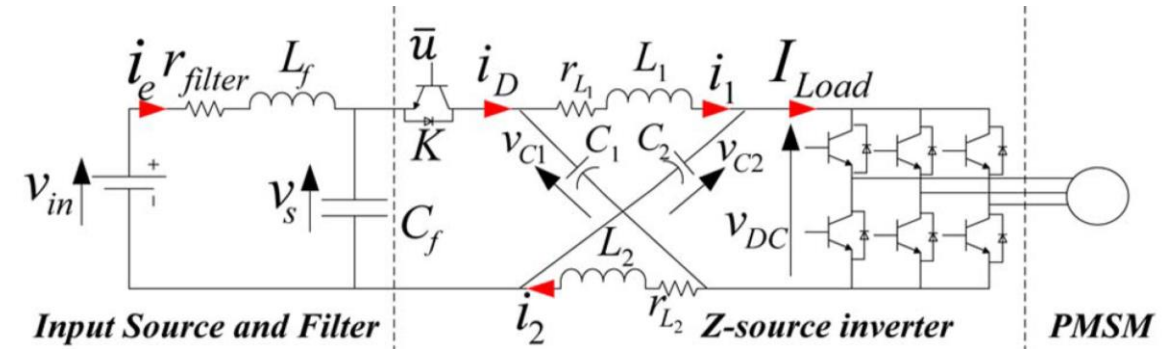
# Motor Drives for Speed Range Extension

DC-link voltage adaptation for speed range extension:

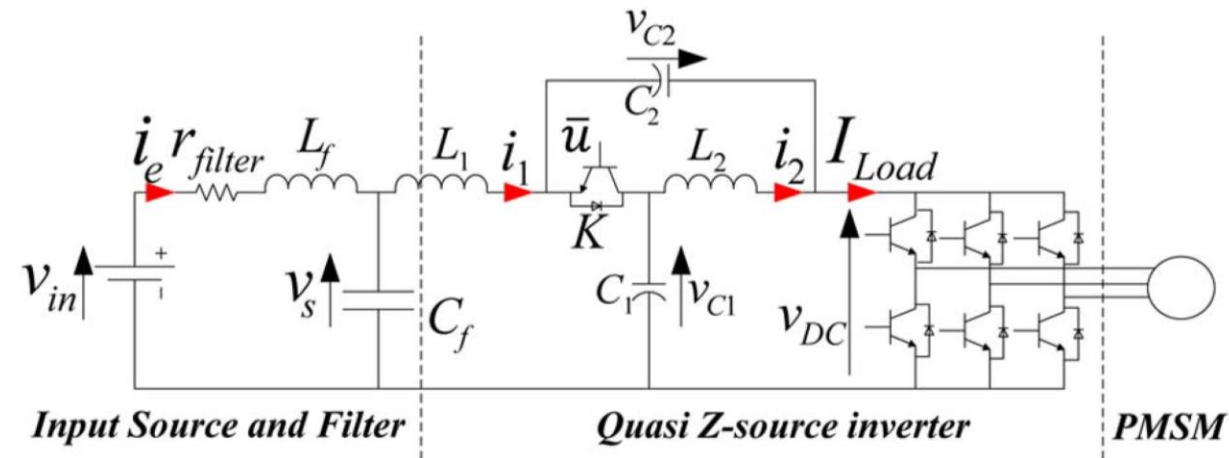
Drawbacks:

- High stress on components
- Limited voltage stepping-up due to efficiency
- Power density

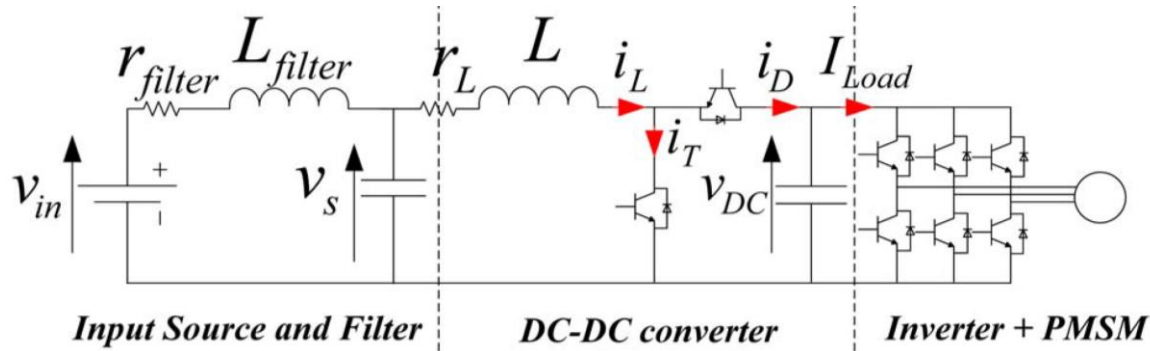
Z-source inverter



Quasi Z-source inverter



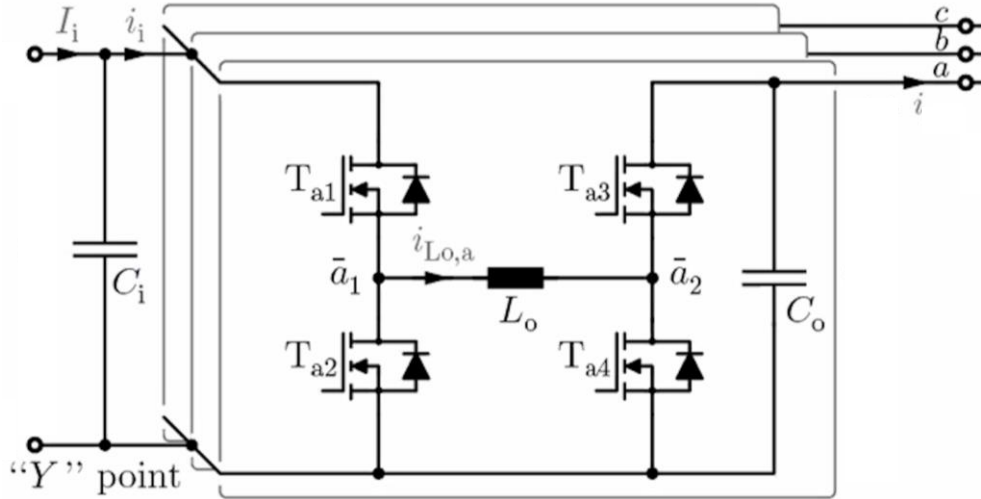
Boost + VSI



A. Battiston *et al.*, "A Control Strategy for Electric Traction Systems Using a PM-Motor Fed by a Bidirectional Z-Source Inverter," *IEEE Trans. on Vehicular Technology*, Vol. 63, No. 9, pp. 4178-4191, Nov. 2014.

# Motor Drives: New Topologies

## Y-inverter:



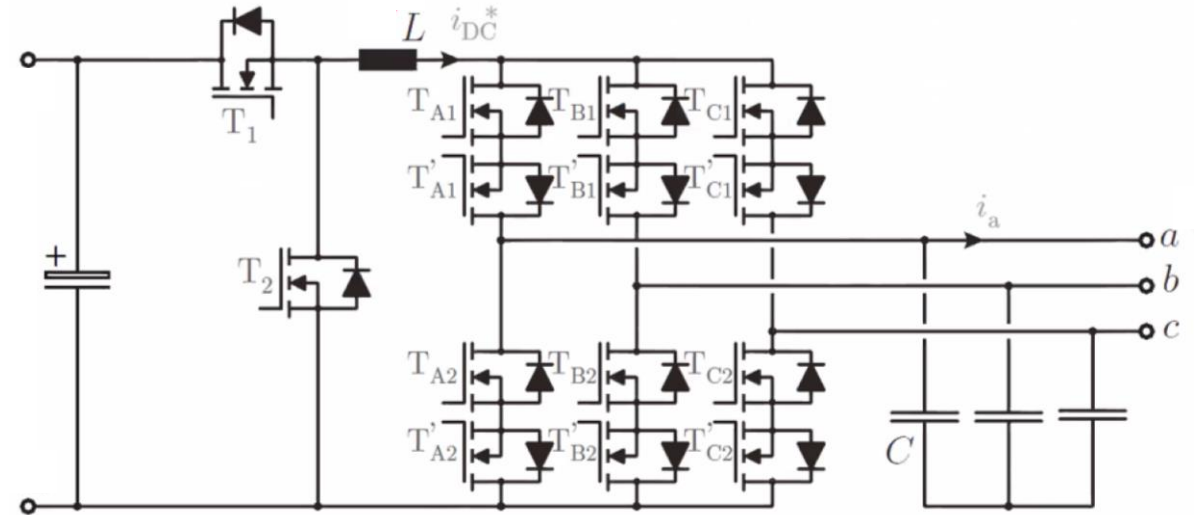
### Features:

- Buck-boost conversion
- Sinusoidal output voltage
- Off-the-shelf legs or bridges

### Challenges:

- Complex control: three-cascaded loops
- Power density

## Current-Source Inverter (CSI):



### Features:

- Single inductor
- Current control for buck stage output current
- Monolithic Bidirectional GaN switches

### Challenges:

- Off-the-shelf legs/inverter
- Motor torque control over wide speed range

# Motor Drives: Trends and Challenges

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- **Multi-level inverters:** higher voltage motors
- **Sinus-inverter:** low high frequency components, longer useful lifetime, lower losses in motor, wide voltage and frequency range
- **Smaller/lighter inverters and Motor-integrated inverters**
- **Challenges with WBG devices (SiC and GaN):** packaging, EMI, motor insulation, shaft (bearing) currents
- **Challenges at high-power motor drives:** parallel interleaving for large currents sharing
- **Challenges with EMI filters:** higher influence of parasitic elements, couplings between components
- **Effect of long cables:** output filter to be added

## Conclusion

# Motor Control for Electrified Transportation: Trends and Challenges

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- **Wide speed range operation:** maintaining the control over wide range variation of speed with a given DC voltage (maximum DC-link voltage utilization)
- **Efficiency:** high efficiency operation over wide speed range (extension of battery range)
- **Optimal design of ASD:** impact of control on optimization of ASD (system level) in terms of weight and volume (power density in  $kg/kW$  and  $l/kW$ )
- **Reliability and maintenance:** improving reliability by design, partial/full parallel redundancy, fast/cost effective maintainability
- **Cost reduction:** reducing cost while improving/keeping same performances
- **Noise and vibration reduction:** reducing torque ripples, noise and vibration using more effective control laws
- **Accurate torque control:** torque estimation, adaptive MTPA, effect of temperature

# Motor Control for Electrified Transportation: Trends and Challenges

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- **Current control under OVM and SSO:** THDi reduction under OVM, torque ripple reduction, smooth transition between OVM and SSO
- **Fault-tolerant capability:** fault diagnosis and prognosis, health-monitoring, remaining useful lifetime (RUL) estimation, fault-tolerant control
- **Multi-phase motors:** power and torque splitting under normal and fault conditions, reducing current harmonics using either current controllers or tailored PWM techniques
- **Current control techniques:** development of control laws for new motor drives and multi-phase motors
- **Motor-integrated inverters:** high efficiency, high power density, better EMI immunity, “non-expert” installation

**A good motor is one that can be forgotten!**





**Thank you!**

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